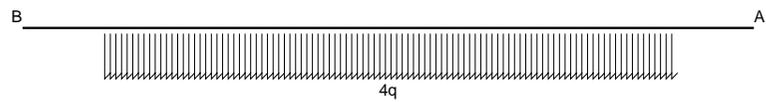


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 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_B =$

$H_C =$

$W_B =$

$V_C =$

$H_{AB} =$

$H_{CA} =$

$V_{AB} =$

$V_{CA} =$

$W_{AB} =$

$W_{CA} =$

$H_{BA} =$

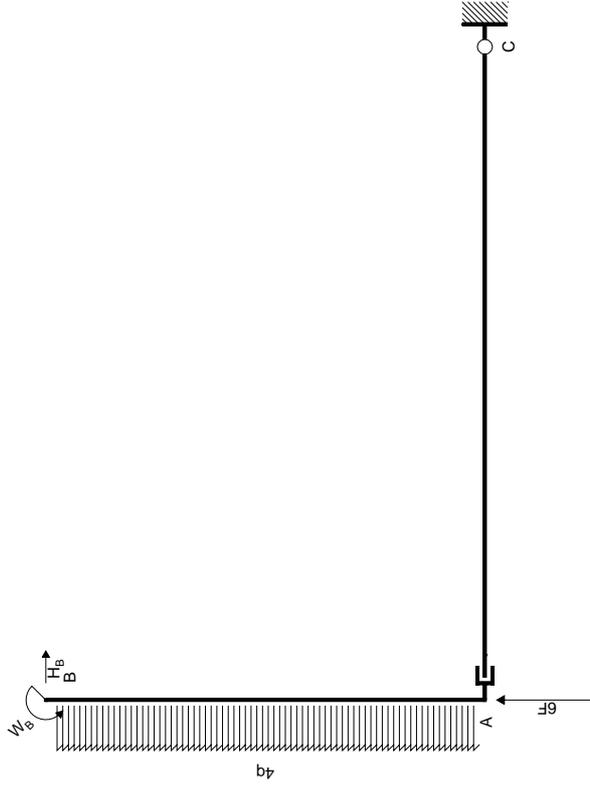
$H_{AC} =$

$V_{BA} =$

$V_{AC} =$

$W_{BA} =$

$W_{AC} =$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$-2H_{Bb} + W_B = 18Fb - 8qb^2$$

Traslazione orizzontale: aste AB

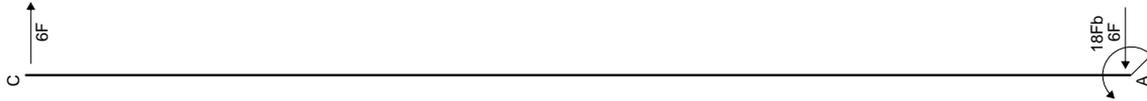
$$H_B = 8qb$$

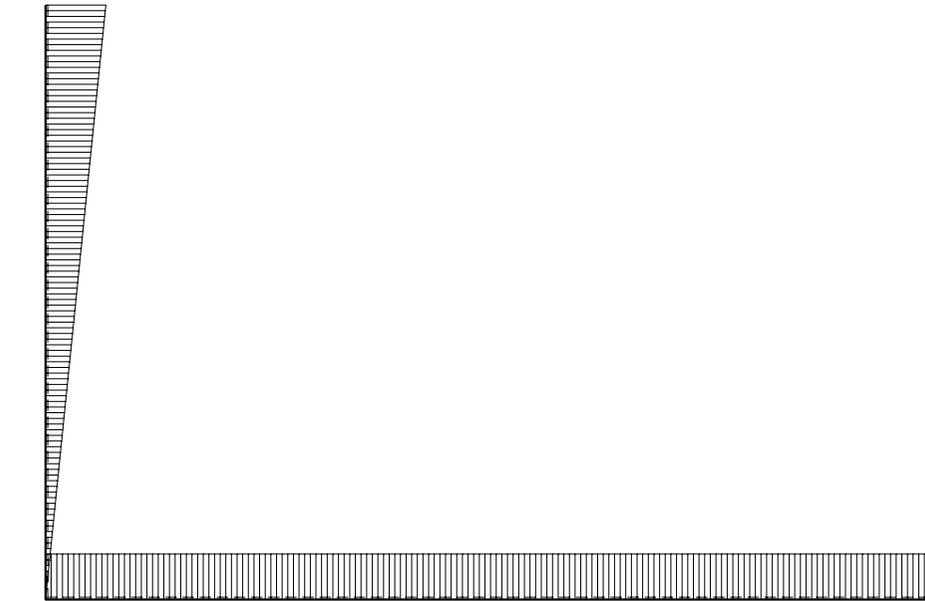
Matrice di equilibrio

$$\begin{bmatrix} H_{Bb} & W_B \end{bmatrix} \begin{bmatrix} Fb & qb^2 \\ 18 & -8 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_{Bb} \\ W_B \end{bmatrix} = \begin{bmatrix} 0 & 8 \\ 18 & 8 \end{bmatrix}$$





↑ + ↓
|——| 10 F

REAZIONI

$$H_B = 8qb = 8F$$

$$W_B = 18Fb + 8qb^2 = 26Fb$$

$$H_C = 0$$

$$V_C = -6F = -6F$$

$$H_{AB} = 0$$

$$V_{AB} = 0$$

$$W_{AB} = -18Fb = -18Fb$$

$$H_{BA} = 8qb = 8F$$

$$V_{BA} = 0$$

$$W_{BA} = 18Fb + 8qb^2 = 26Fb$$

$$H_{CA} = 0$$

$$V_{CA} = -6F = -6F$$

$$W_{CA} = 0$$

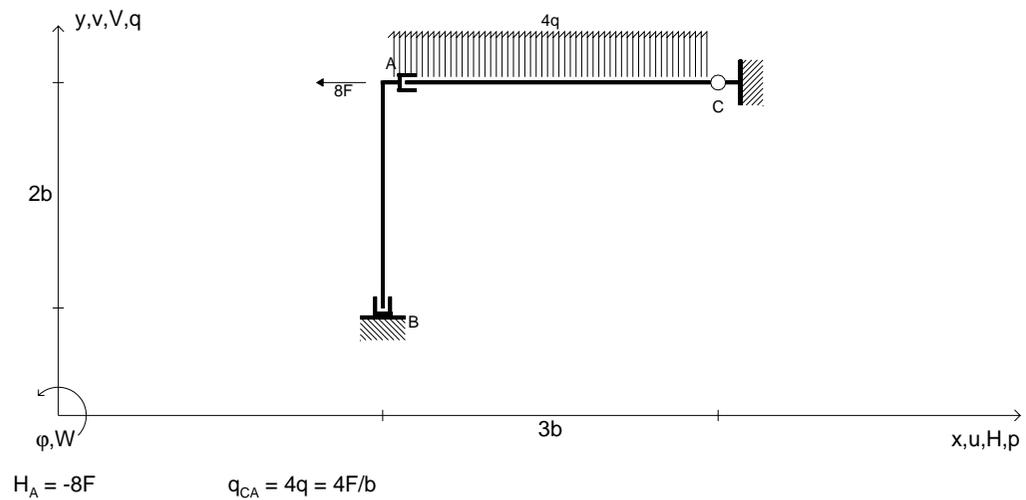
$$H_{AC} = 0$$

$$V_{AC} = 6F = 6F$$

$$W_{AC} = 18Fb = 18Fb$$

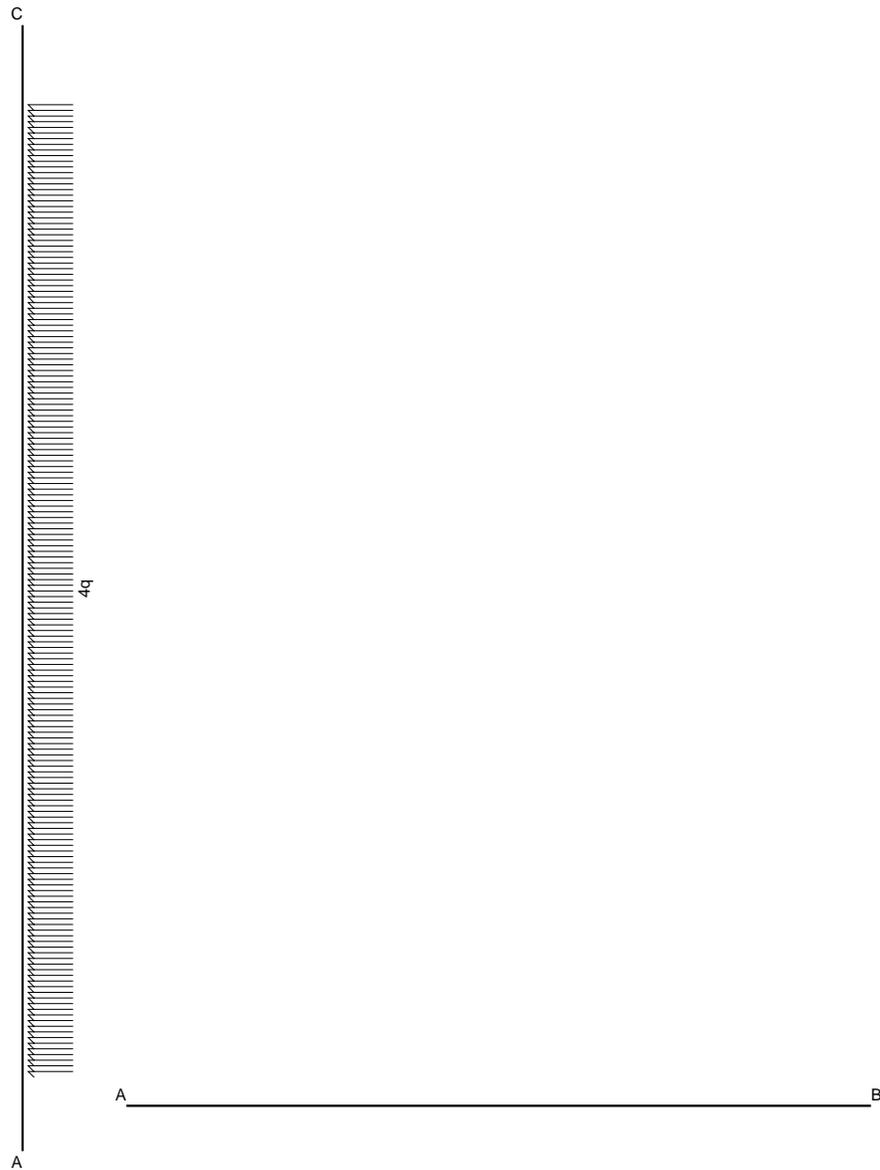


↺ + ↻
|——| 30 Fb



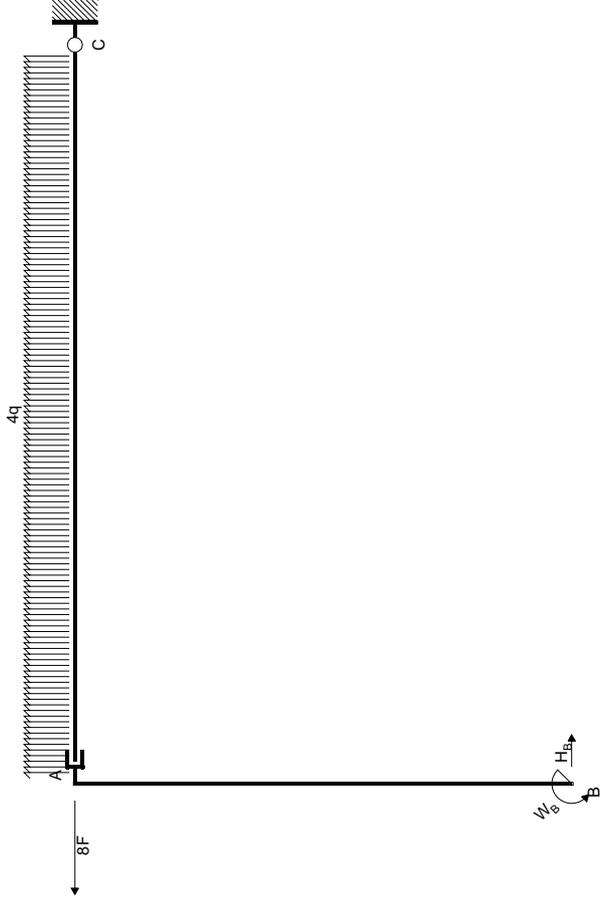
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REAZIONI

- | | |
|------------|------------|
| $H_B =$ | $H_C =$ |
| $W_B =$ | $V_C =$ |
| $H_{AB} =$ | $H_{CA} =$ |
| $V_{AB} =$ | $V_{CA} =$ |
| $W_{AB} =$ | $W_{CA} =$ |
| $H_{BA} =$ | $H_{AC} =$ |
| $V_{BA} =$ | $V_{AC} =$ |
| $W_{BA} =$ | $W_{AC} =$ |



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_B b + W_B = 18qb^2$$

Traslazione orizzontale: aste AB

$$H_B = 8F$$

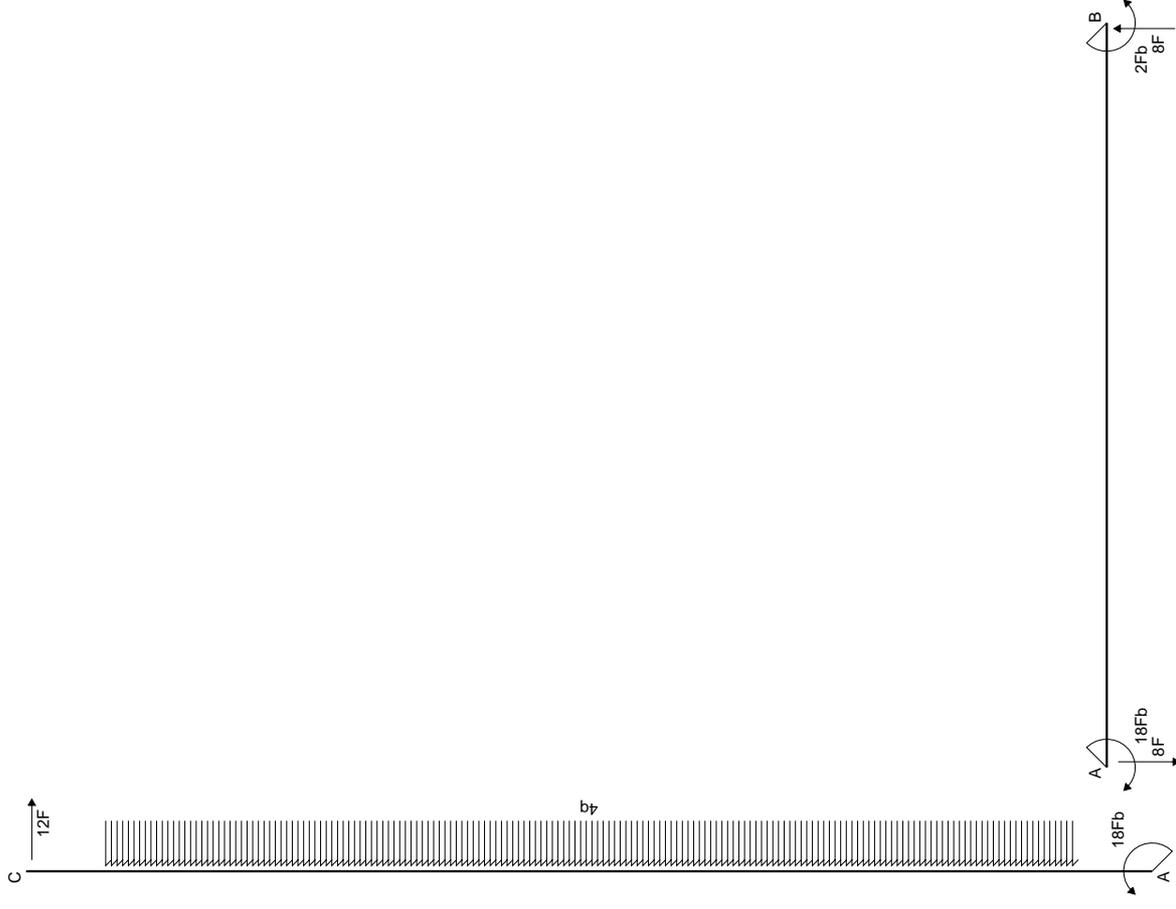
Matrice di equilibrio

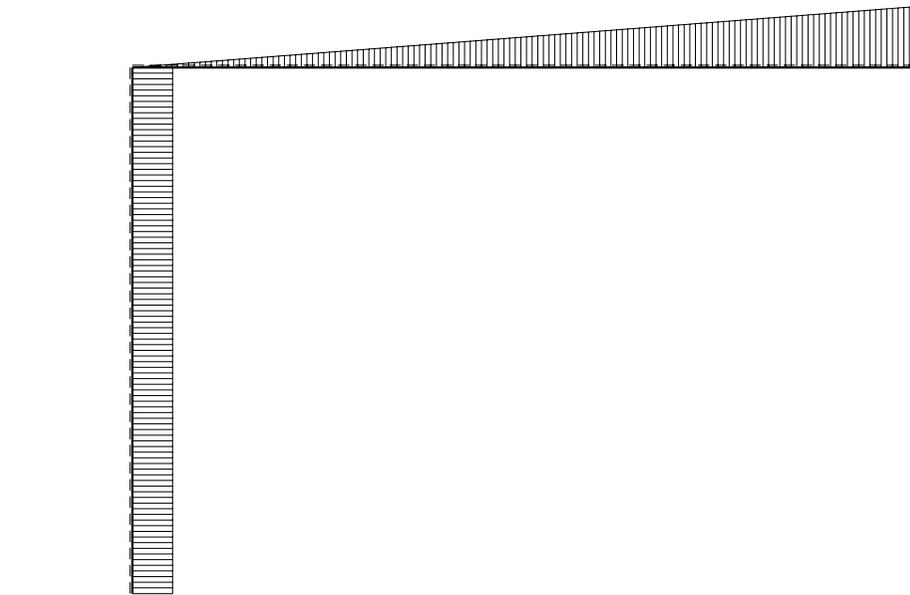
$$\begin{bmatrix} H_B b & W_B \end{bmatrix} \begin{bmatrix} Fb & qb^2 \\ 8 & 18 \end{bmatrix} = \begin{bmatrix} 0 & 18 \\ 8 & 0 \end{bmatrix}$$

$$u_{AC} \begin{bmatrix} 1 & 0 \end{bmatrix} = \begin{bmatrix} 8 & 0 \end{bmatrix}$$

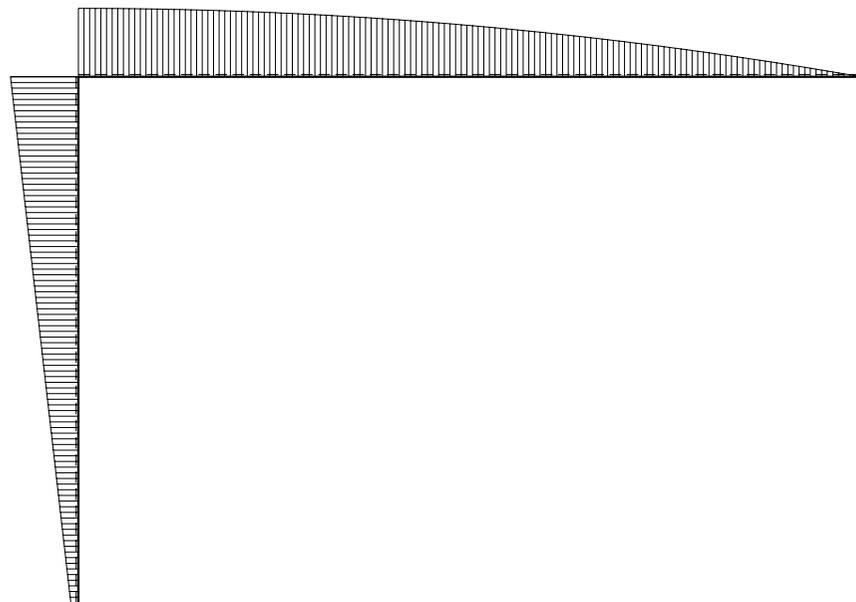
Soluzione del sistema

$$\begin{bmatrix} H_B b \\ W_B \end{bmatrix} = \begin{bmatrix} 8 & 0 \\ -16 & 18 \end{bmatrix}$$





$\uparrow + \downarrow$ $\longleftarrow 15 F$



$\curvearrowright + \curvearrowleft$ $\longleftarrow 20 Fb$

REAZIONI

$$H_B = 8F = 8F$$

$$W_B = -16Fb + 18qb^2 = 2Fb$$

$$H_{AB} = -8F = -8F$$

$$V_{AB} = 0$$

$$W_{AB} = -18qb^2 = -18Fb$$

$$H_{BA} = 8F = 8F$$

$$V_{BA} = 0$$

$$W_{BA} = -16Fb + 18qb^2 = 2Fb$$

$$H_C = 0$$

$$V_C = -12qb = -12F$$

$$H_{CA} = 0$$

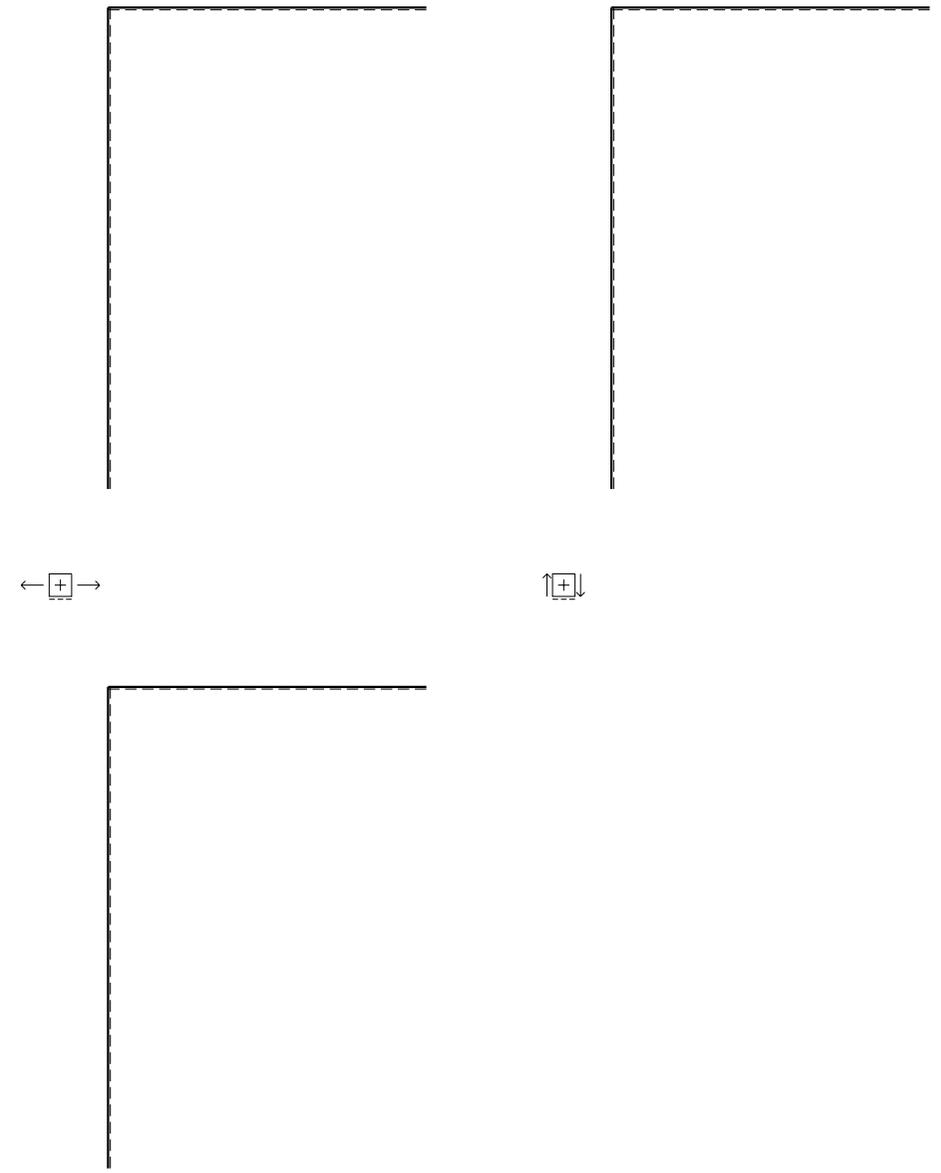
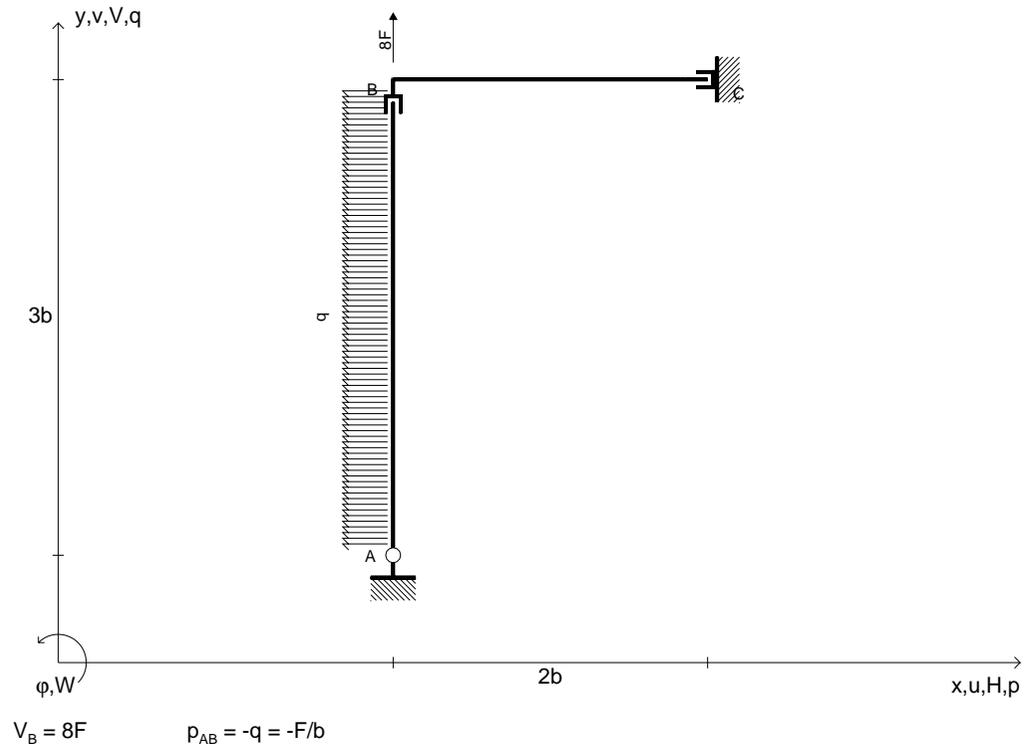
$$V_{CA} = -12qb = -12F$$

$$W_{CA} = 0$$

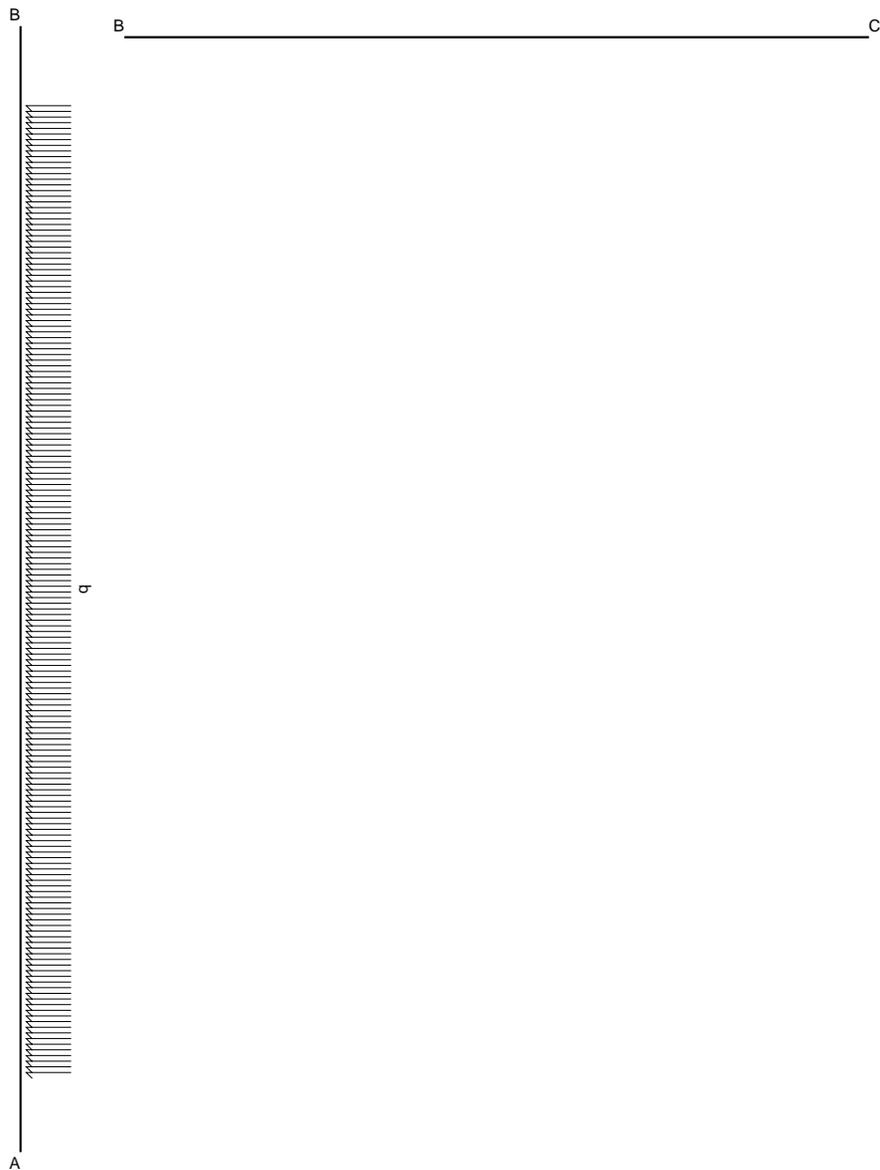
$$H_{AC} = 0$$

$$V_{AC} = 0$$

$$W_{AC} = 18qb^2 = 18Fb$$

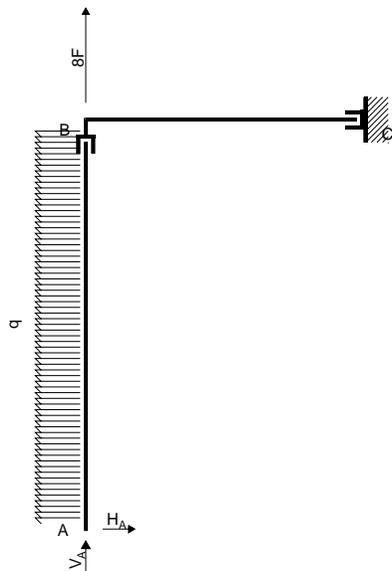


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REAZIONI

$H_A =$	$V_C =$
$V_A =$	$W_C =$
$H_{AB} =$	$H_{BC} =$
$V_{AB} =$	$V_{BC} =$
$W_{AB} =$	$W_{BC} =$
$H_{BA} =$	$H_{CB} =$
$V_{BA} =$	$V_{CB} =$
$W_{BA} =$	$W_{CB} =$



EQUAZIONI DI EQUILIBRIO

Traslazione orizzontale globale

$$H_A = 3qb$$

Traslazione verticale: aste BA

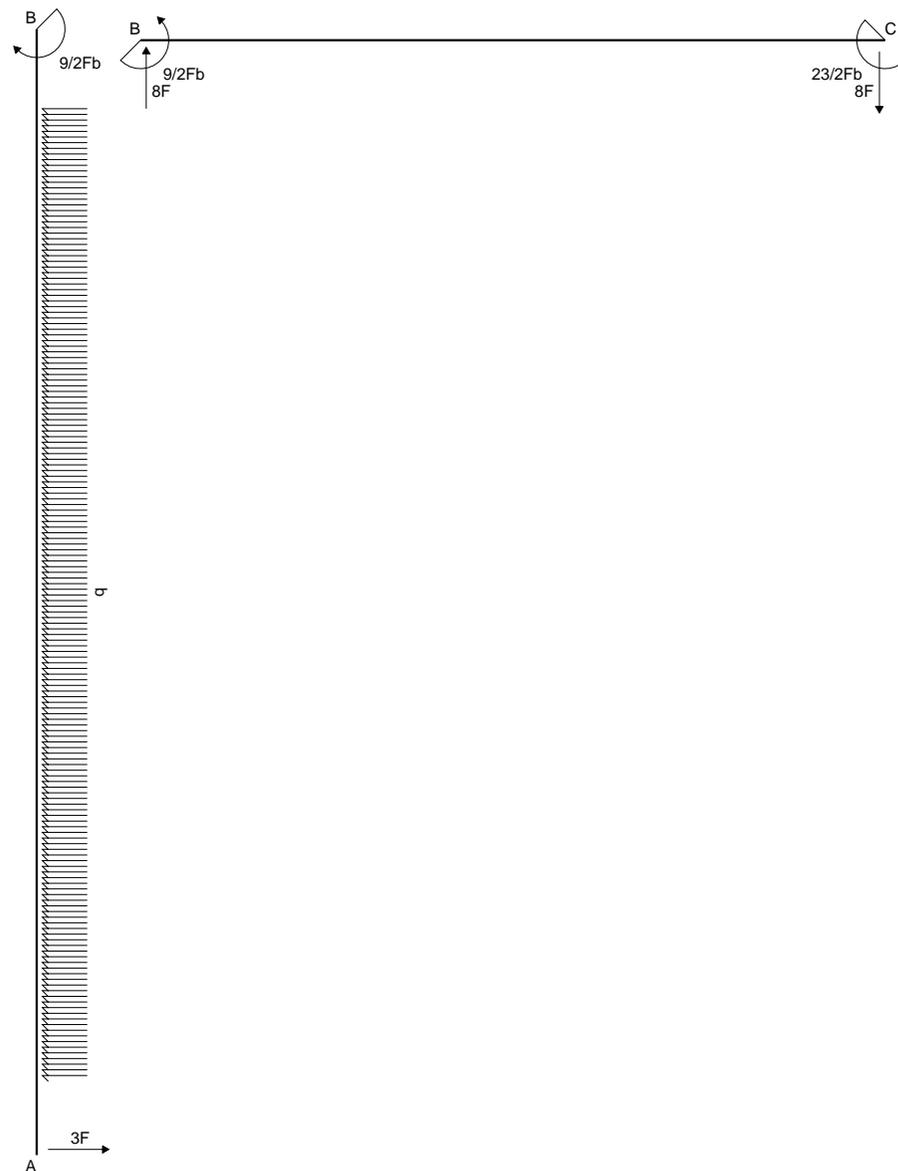
$$V_A = 0$$

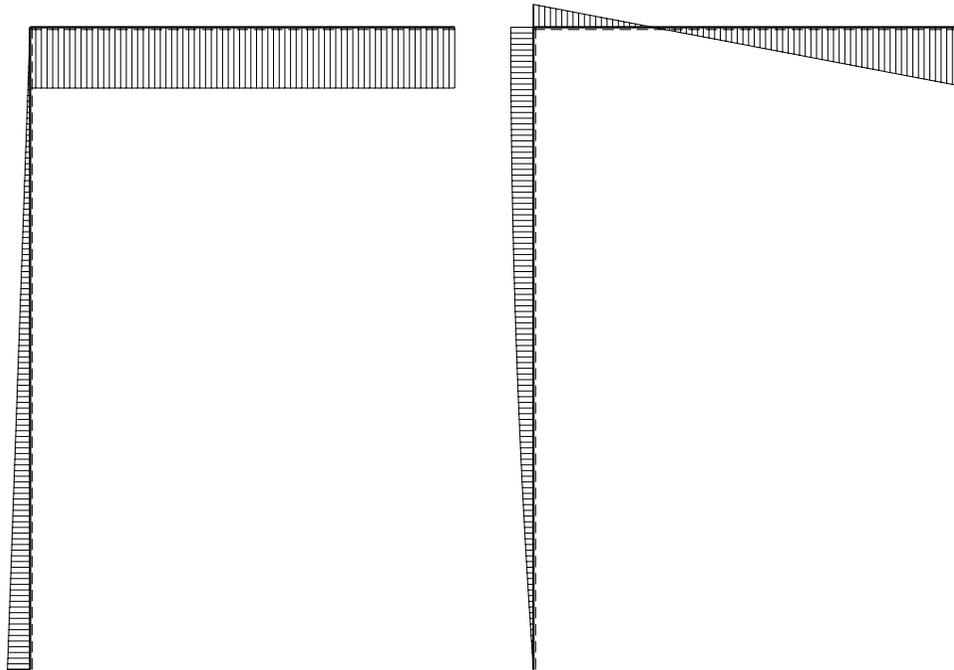
Matrice di equilibrio

$$u_C \begin{bmatrix} H_A b & V_A b \\ 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 3 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 3 \\ 0 & 0 \end{bmatrix}$$





REAZIONI

$$H_A = 3qb = 3F$$

$$V_A = 0$$

$$H_{AB} = 3qb = 3F$$

$$V_{AB} = 0$$

$$W_{AB} = 0$$

$$H_{BA} = 0$$

$$V_{BA} = 0$$

$$W_{BA} = -9/2qb^2 = -9/2Fb$$

$$V_C = -8F = -8F$$

$$W_C = 16Fb - 9/2qb^2 = 23/2Fb$$

$$H_{BC} = 0$$

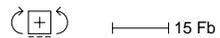
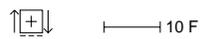
$$V_{BC} = 8F = 8F$$

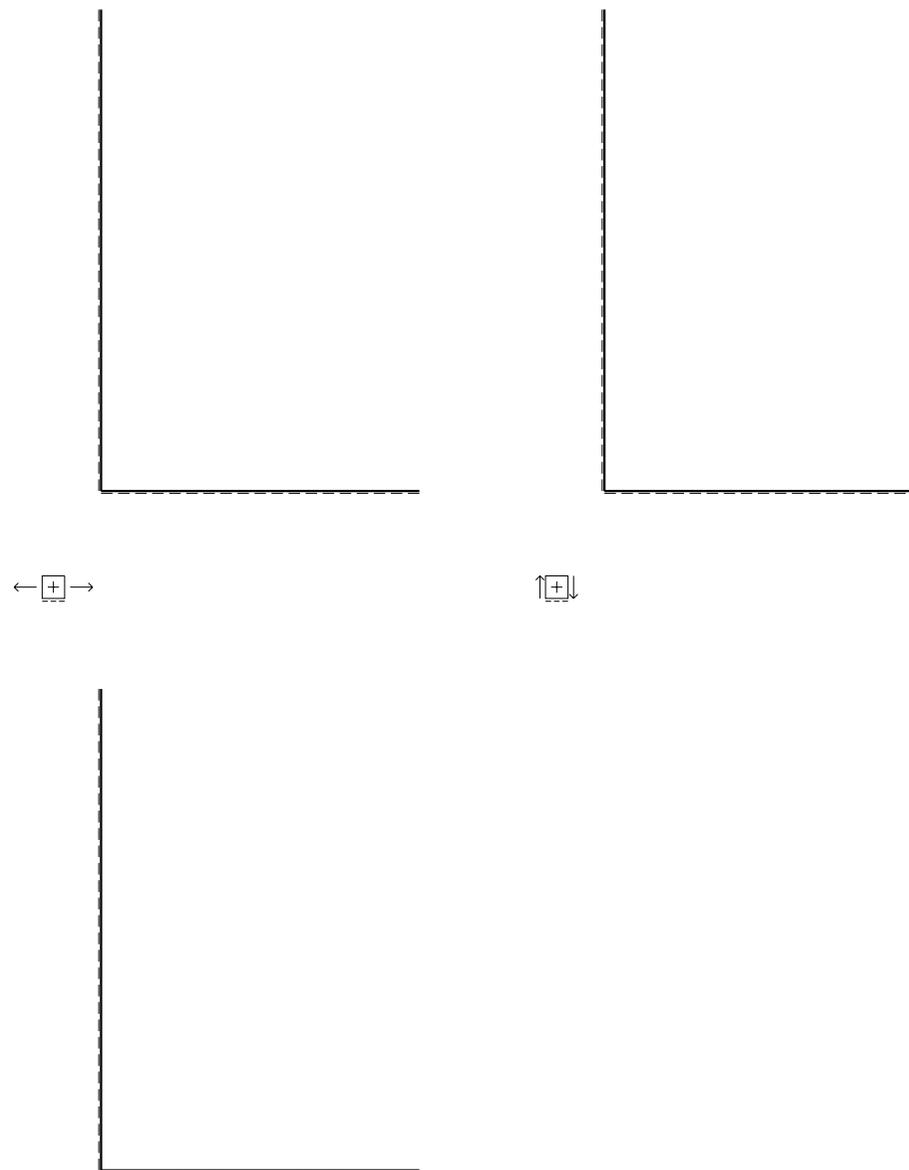
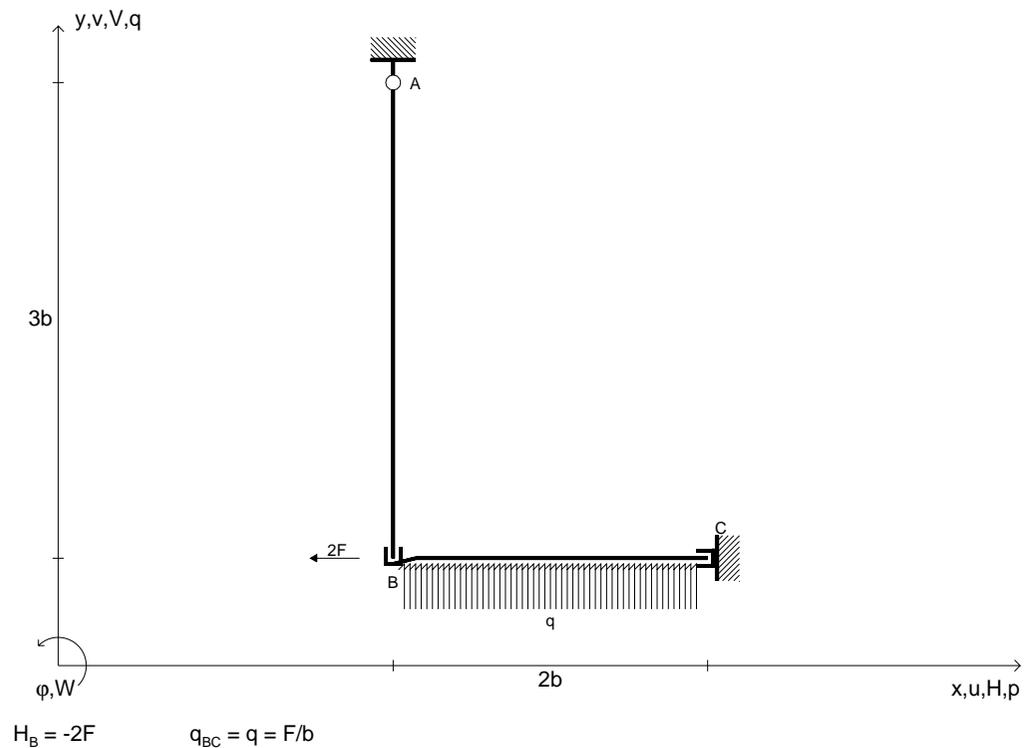
$$W_{BC} = 9/2qb^2 = 9/2Fb$$

$$H_{CB} = 0$$

$$V_{CB} = -8F = -8F$$

$$W_{CB} = 16Fb - 9/2qb^2 = 23/2Fb$$





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REAZIONI

$H_A =$ $V_A =$ $V_C =$ $W_C =$

$H_{AB} =$ $H_{BC} =$

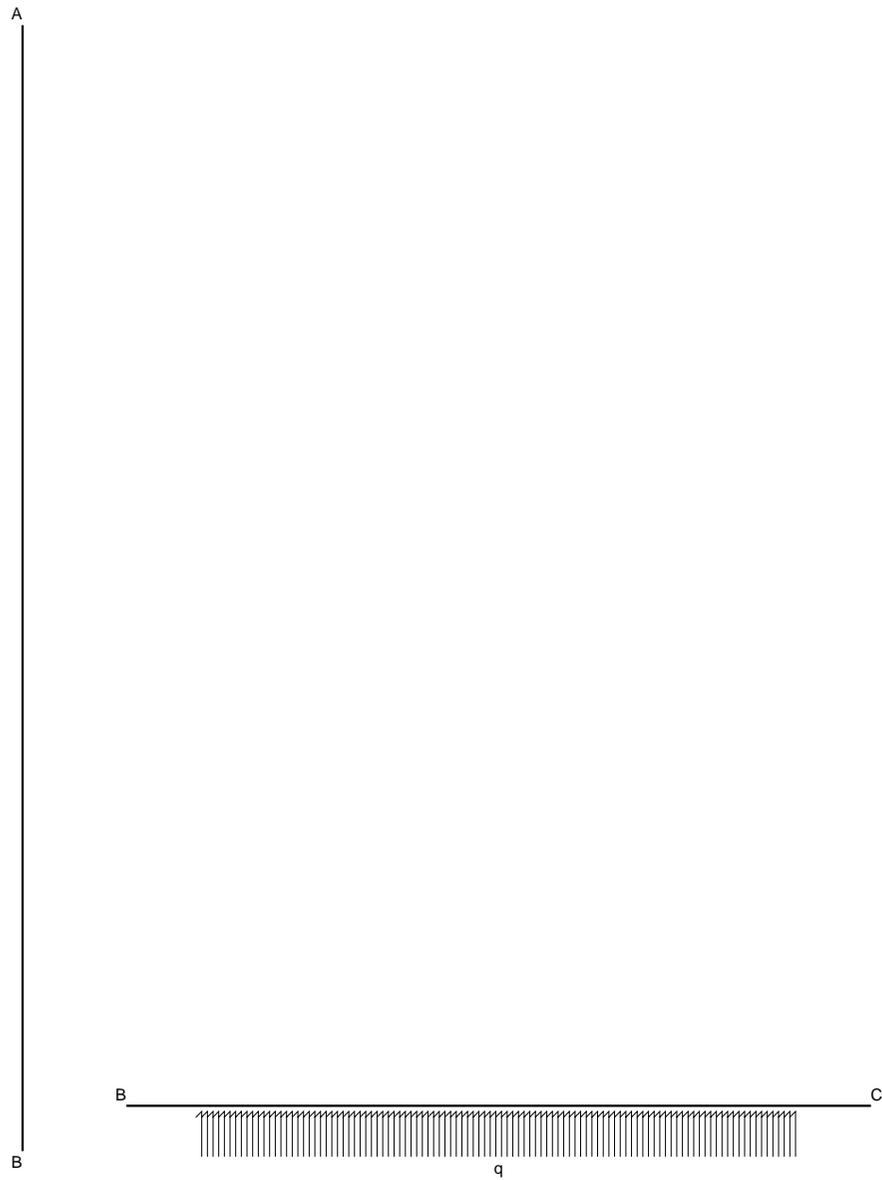
$V_{AB} =$ $V_{BC} =$

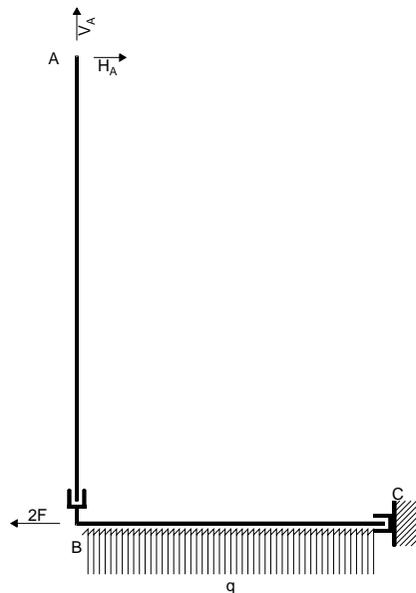
$W_{AB} =$ $W_{BC} =$

$H_{BA} =$ $H_{CB} =$

$V_{BA} =$ $V_{CB} =$

$W_{BA} =$ $W_{CB} =$





EQUAZIONI DI EQUILIBRIO

Traslazione orizzontale globale

$$H_A = 2F$$

Traslazione verticale: aste BA

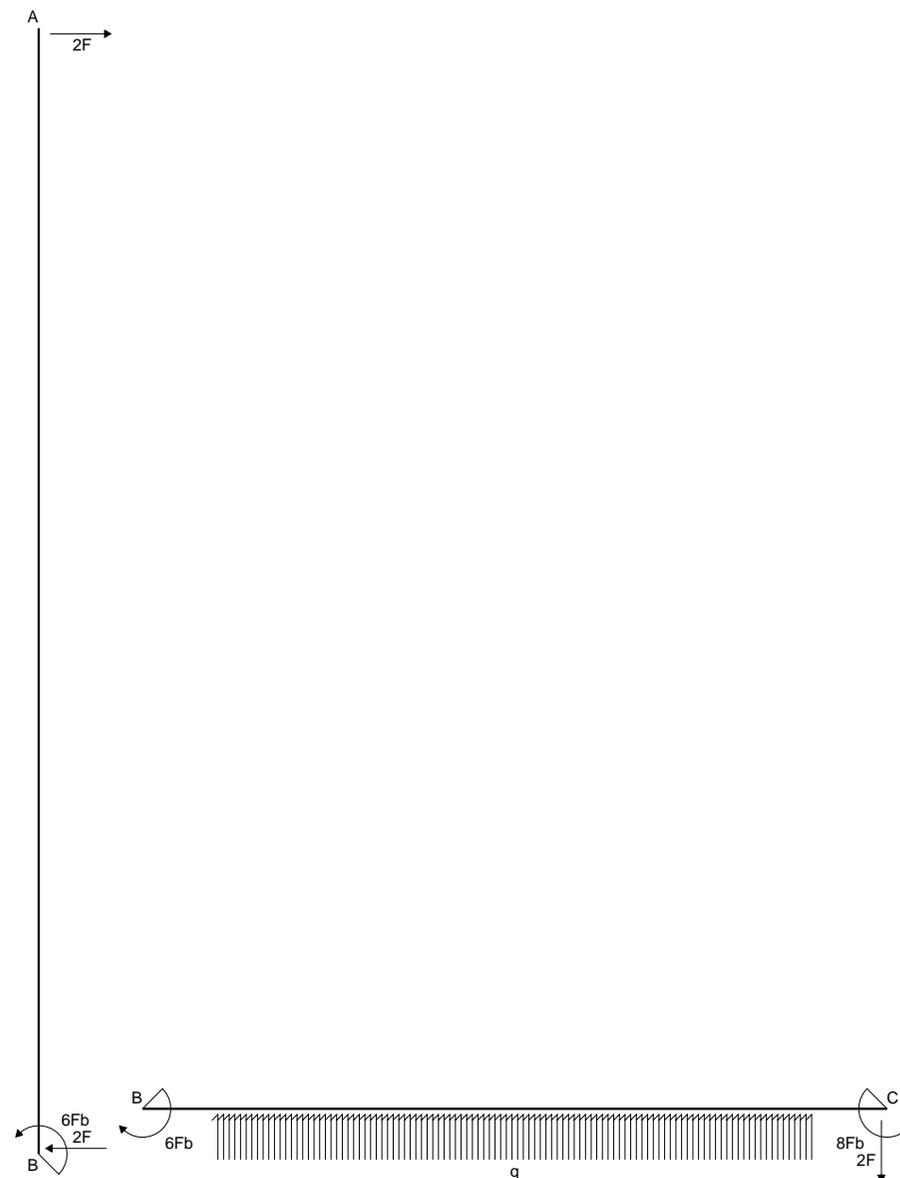
$$V_A = 0$$

Matrice di equilibrio

$$u_C \begin{bmatrix} H_A b & V_A b \\ 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & 0 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & 0 \\ 0 & 0 \end{bmatrix}$$



REAZIONI

$$H_A = 2F = 2F$$

$$V_A = 0$$

$$V_C = -2qb = -2F$$

$$W_C = 6Fb + 2qb^2 = 8Fb$$

$$H_{AB} = 2F = 2F$$

$$H_{BC} = 0$$

$$V_{AB} = 0$$

$$V_{BC} = 0$$

$$W_{AB} = 0$$

$$W_{BC} = -6Fb = -6Fb$$

$$H_{BA} = -2F = -2F$$

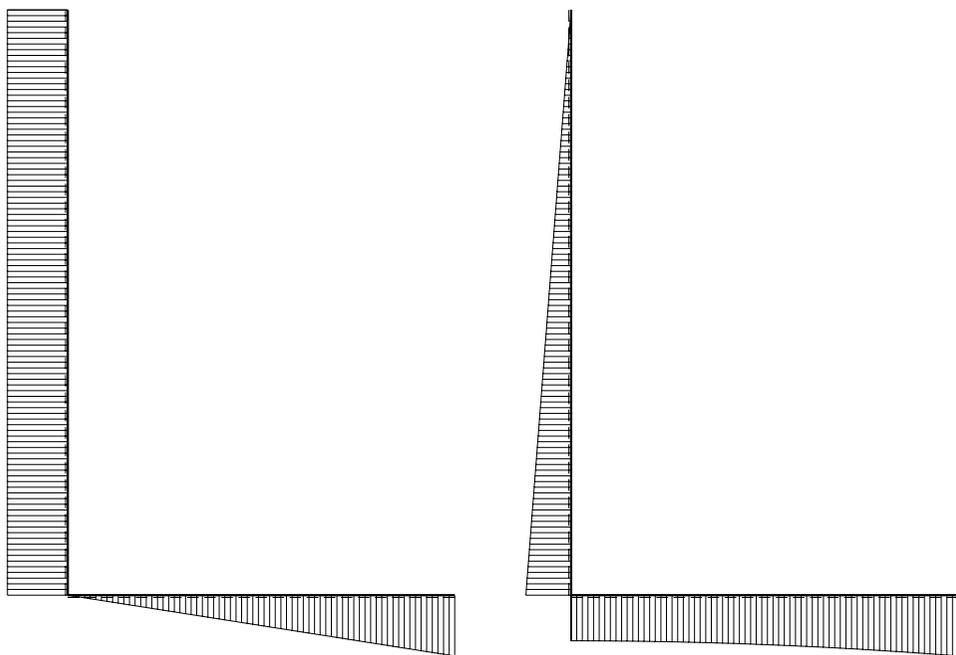
$$H_{CB} = 0$$

$$V_{BA} = 0$$

$$V_{CB} = -2qb = -2F$$

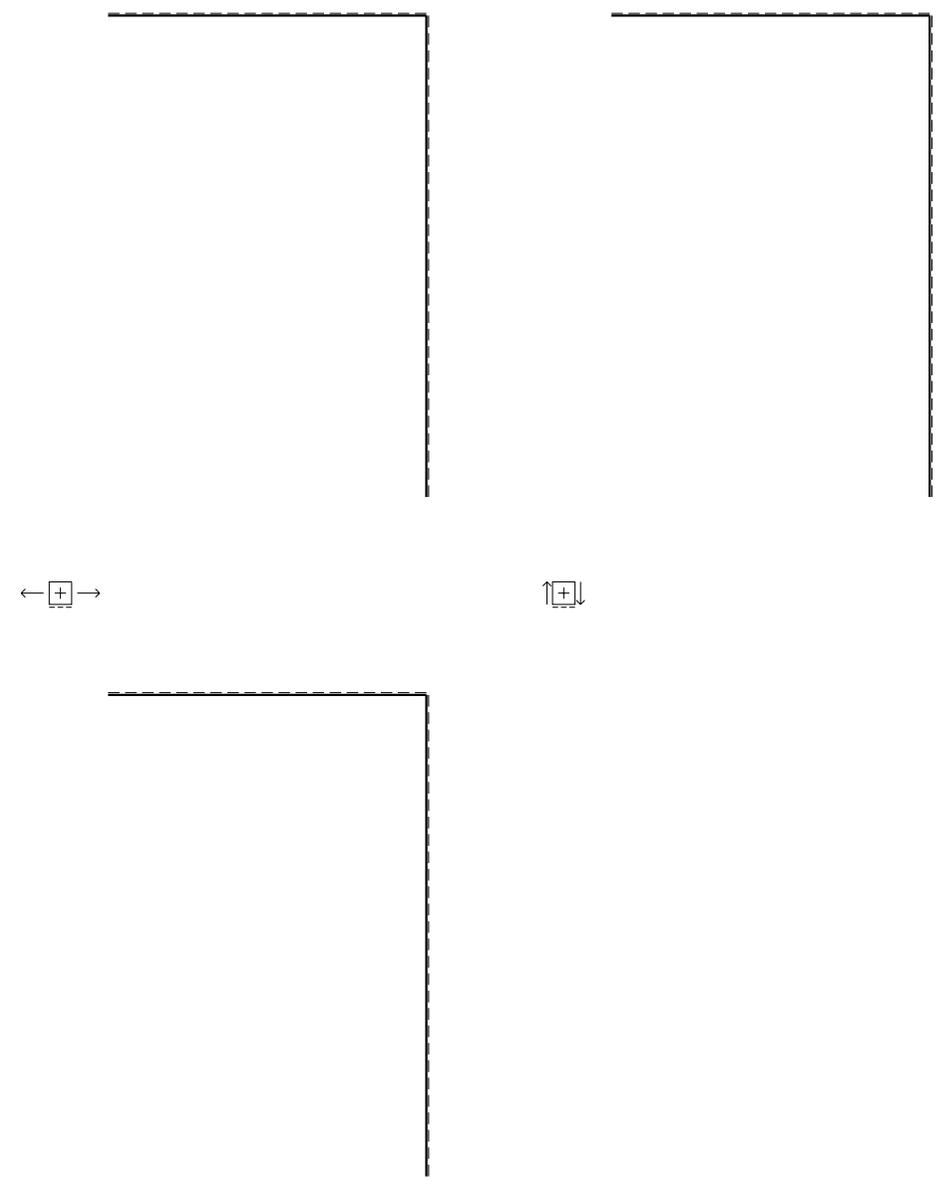
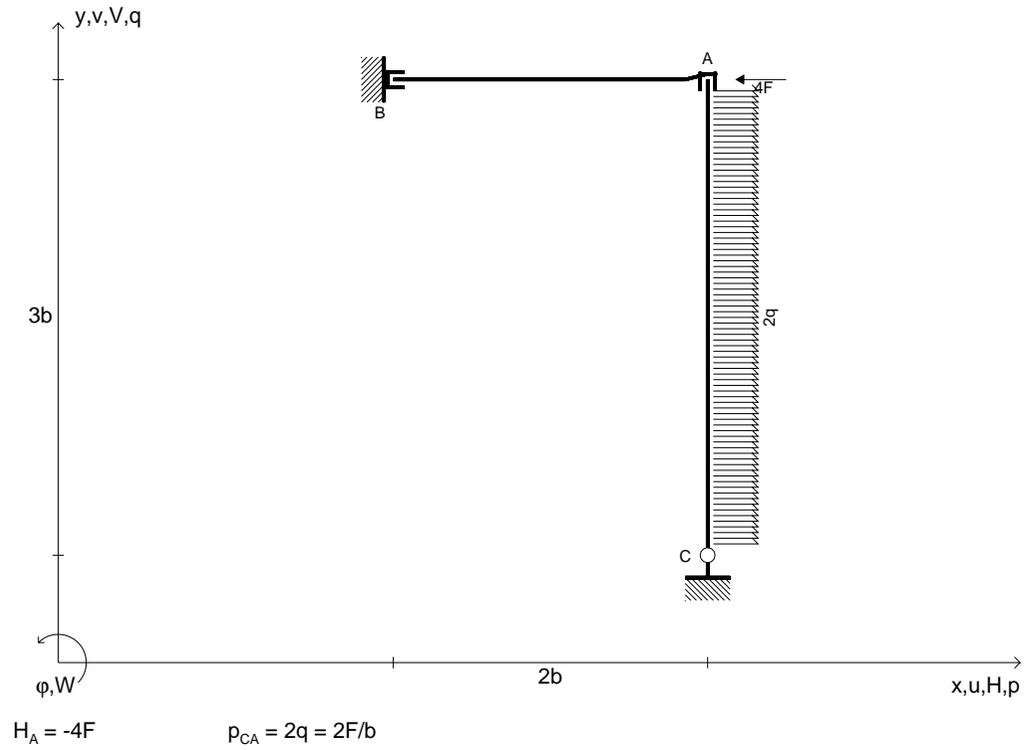
$$W_{BA} = 6Fb = 6Fb$$

$$W_{CB} = 6Fb + 2qb^2 = 8Fb$$

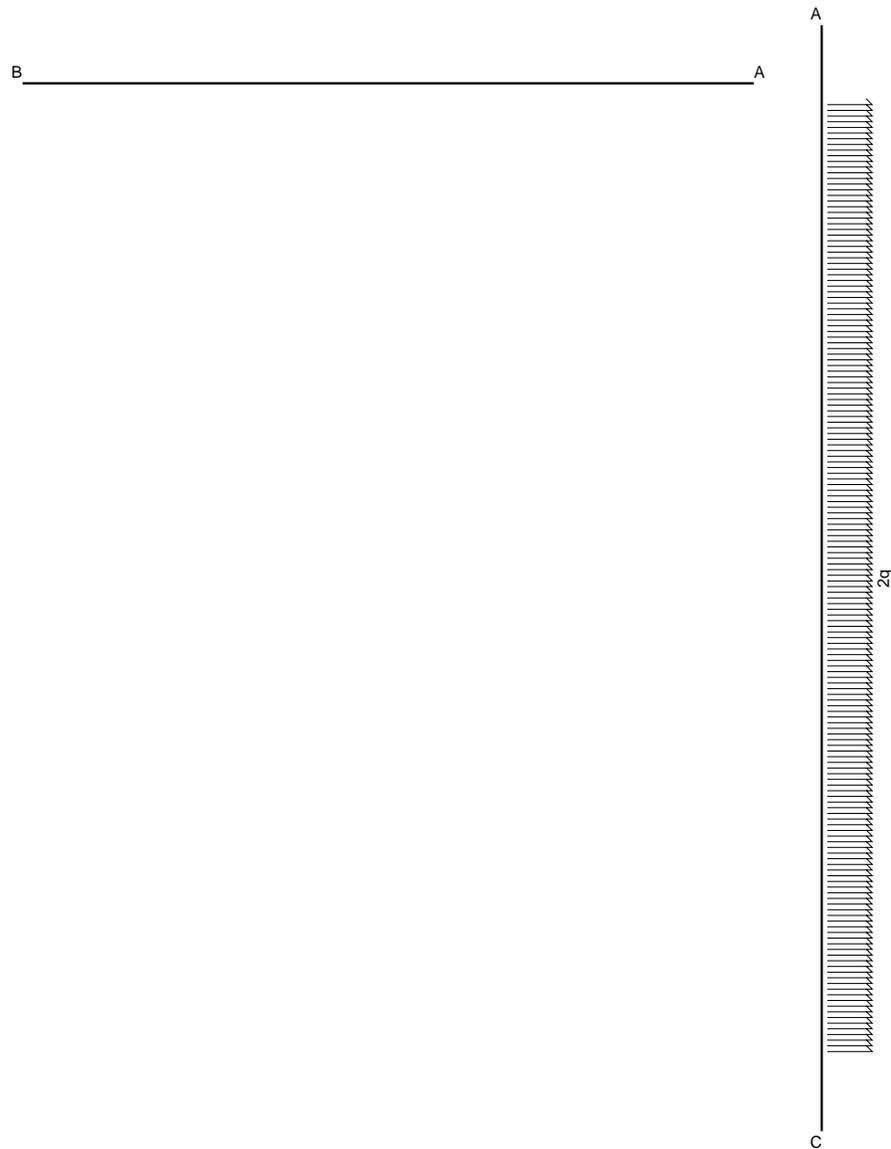


↑+↓ | 2.5 F

↺+↻ | 10 Fb

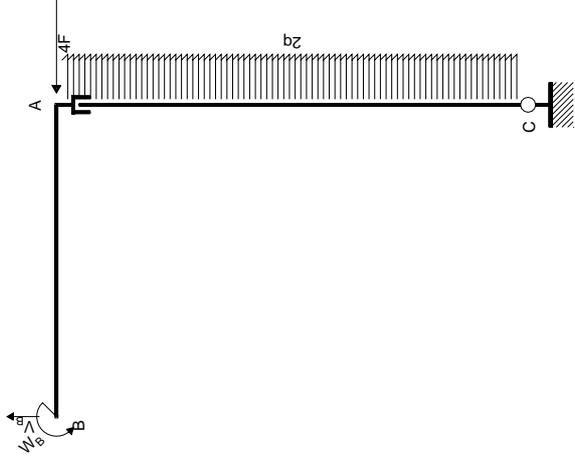


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REAZIONI

- | | |
|------------|------------|
| $V_B =$ | $H_C =$ |
| $W_B =$ | $V_C =$ |
| $H_{AB} =$ | $H_{CA} =$ |
| $V_{AB} =$ | $V_{CA} =$ |
| $W_{AB} =$ | $W_{CA} =$ |
| $H_{BA} =$ | $H_{AC} =$ |
| $V_{BA} =$ | $V_{AC} =$ |
| $W_{BA} =$ | $W_{AC} =$ |



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$-2V_{Bb} + W_B = -12Fb + 9qb^2$$

Traslazione verticale: aste AB

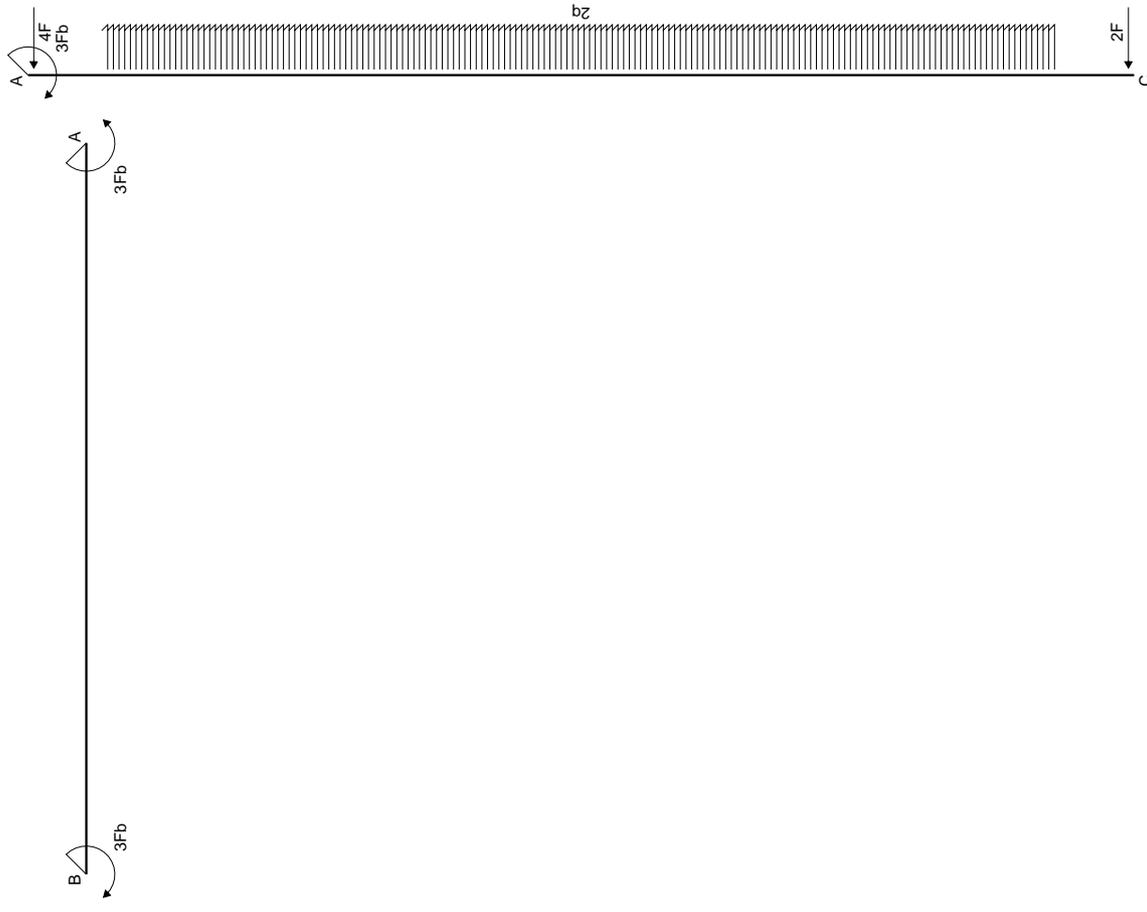
$$V_B = 0$$

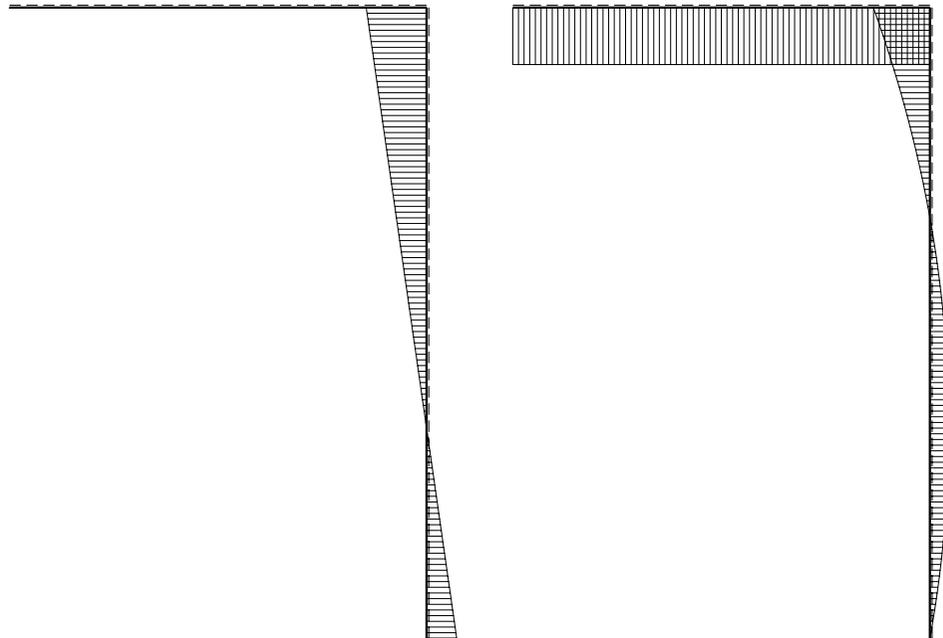
Matrice di equilibrio

$$\begin{bmatrix} V_{Bb} & W_B \end{bmatrix} \begin{bmatrix} Fb & qb^2 \\ -2 & 1 \end{bmatrix} = \begin{bmatrix} -12 & 9 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_{Bb} \\ W_B \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ -12 & 9 \end{bmatrix}$$





REAZIONI

$$V_B = 0$$

$$W_B = -12Fb + 9qb^2 = -3Fb$$

$$H_{AB} = 0$$

$$V_{AB} = 0$$

$$W_{AB} = 12Fb - 9qb^2 = 3Fb$$

$$H_{BA} = 0$$

$$V_{BA} = 0$$

$$W_{BA} = -12Fb + 9qb^2 = -3Fb$$

$$H_C = 4F - 6qb = -2F$$

$$V_C = 0$$

$$H_{CA} = 4F - 6qb = -2F$$

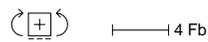
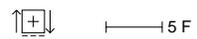
$$V_{CA} = 0$$

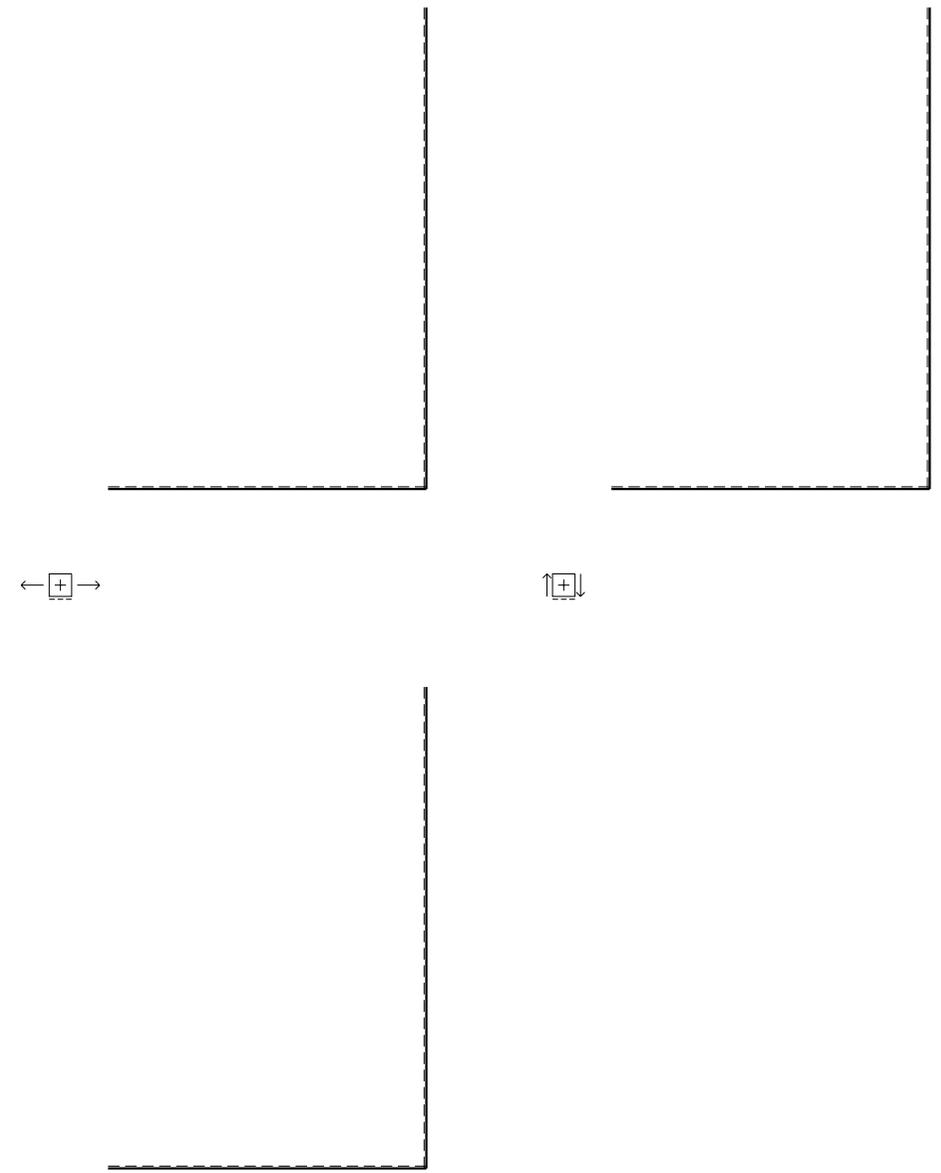
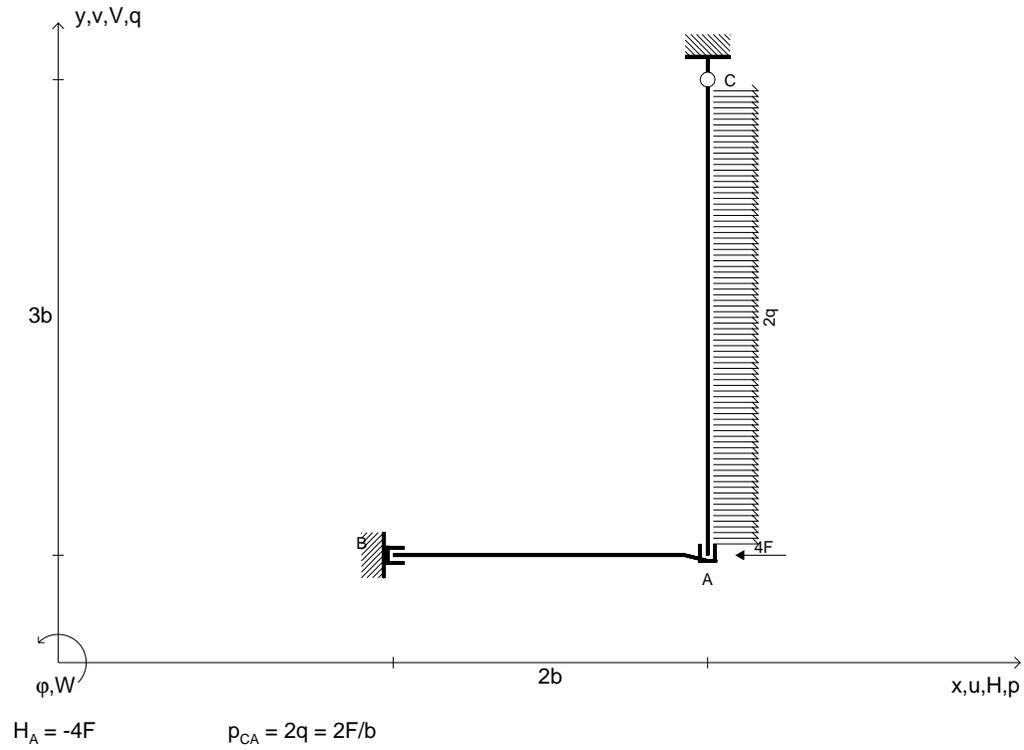
$$W_{CA} = 0$$

$$H_{AC} = -4F = -4F$$

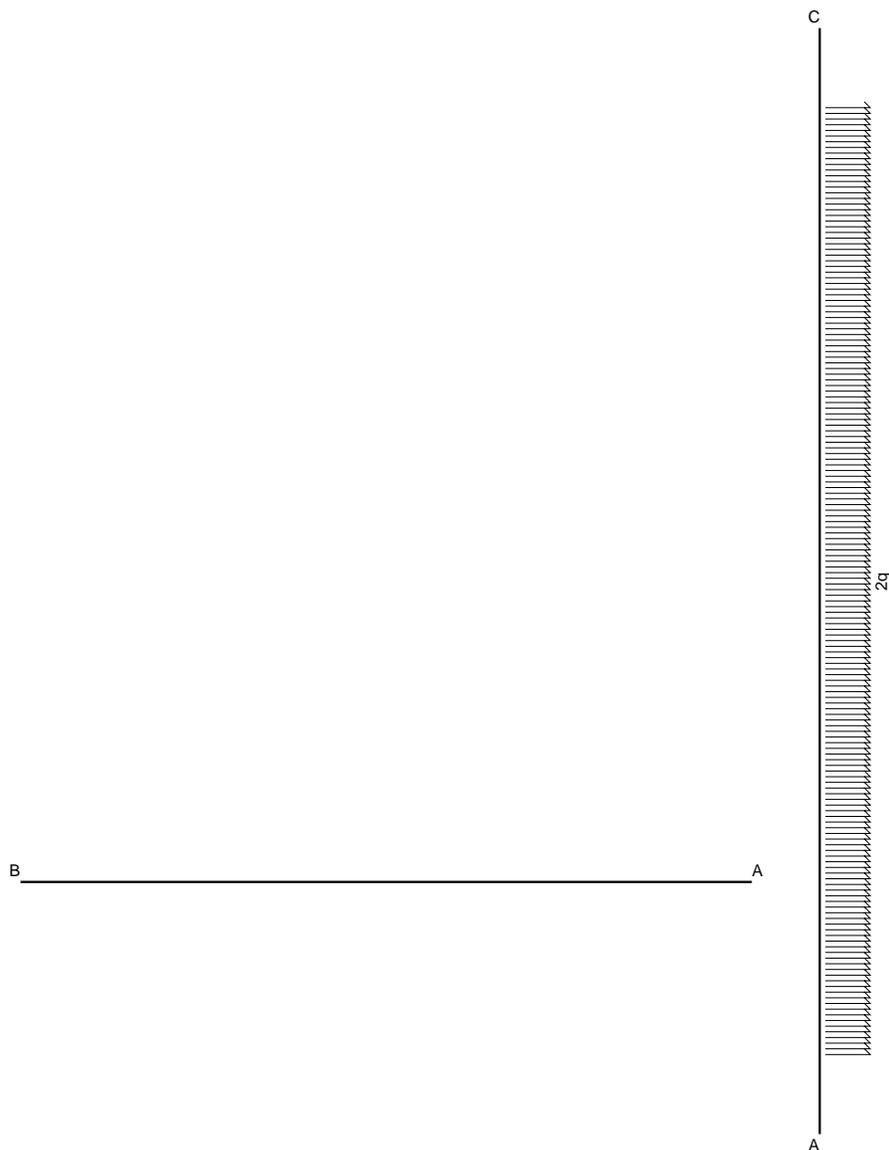
$$V_{AC} = 0$$

$$W_{AC} = -12Fb + 9qb^2 = -3Fb$$





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REAZIONI

$V_B =$

$W_B =$

$H_C =$

$V_C =$

$H_{AB} =$

$H_{CA} =$

$V_{AB} =$

$V_{CA} =$

$W_{AB} =$

$W_{CA} =$

$H_{BA} =$

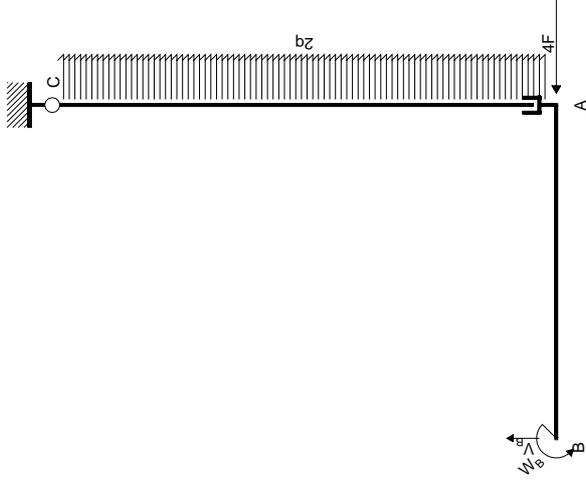
$H_{AC} =$

$V_{BA} =$

$V_{AC} =$

$W_{BA} =$

$W_{AC} =$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$-2V_{Bb} + W_B = 12Fb - 9qb^2$$

Traslazione verticale: aste AB

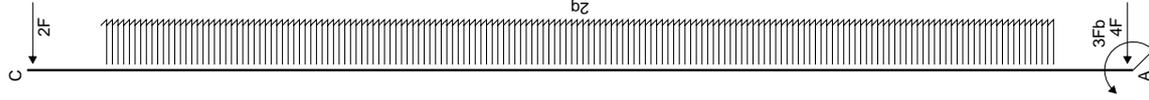
$$V_B = 0$$

Matrice di equilibrio

$$\begin{bmatrix} V_{Bb} & W_B \end{bmatrix} \begin{bmatrix} Fb & qb^2 \\ -2 & 1 \end{bmatrix} = \begin{bmatrix} 12 & -9 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_{Bb} \\ W_B \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 0 \\ 12 & -9 \end{bmatrix}$$



REAZIONI

$$V_B = 0$$

$$W_B = 12Fb - 9qb^2 = 3Fb \quad H_C = 4F - 6qb = -2F \quad V_C = 0$$

$$H_{AB} = 0$$

$$H_{CA} = 4F - 6qb = -2F$$

$$V_{AB} = 0$$

$$V_{CA} = 0$$

$$W_{AB} = -12Fb + 9qb^2 = -3Fb$$

$$W_{CA} = 0$$

$$H_{BA} = 0$$

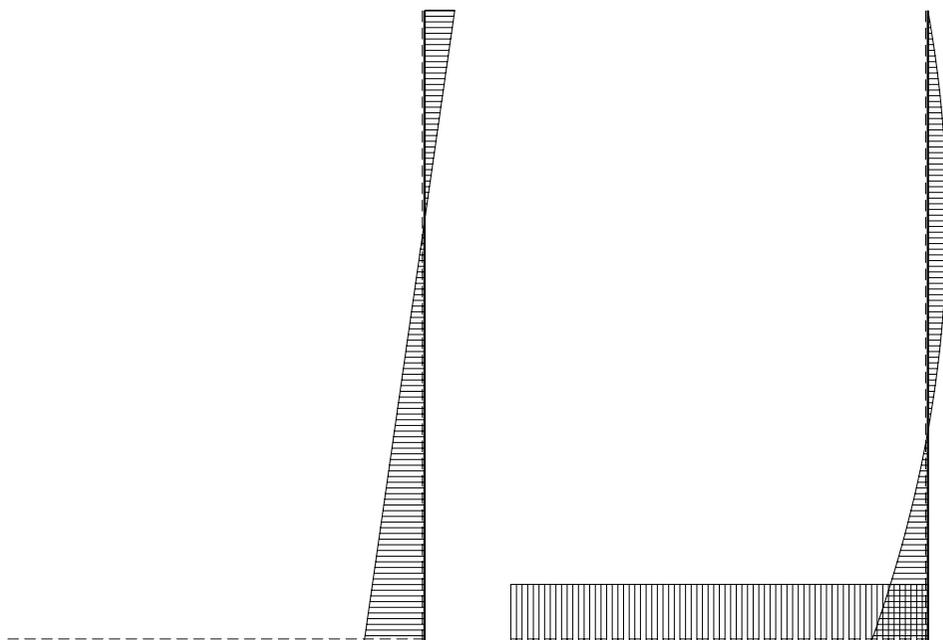
$$H_{AC} = -4F = -4F$$

$$V_{BA} = 0$$

$$V_{AC} = 0$$

$$W_{BA} = 12Fb - 9qb^2 = 3Fb$$

$$W_{AC} = 12Fb - 9qb^2 = 3Fb$$



↑+↓ | 5F

↺+↻ | 4Fb