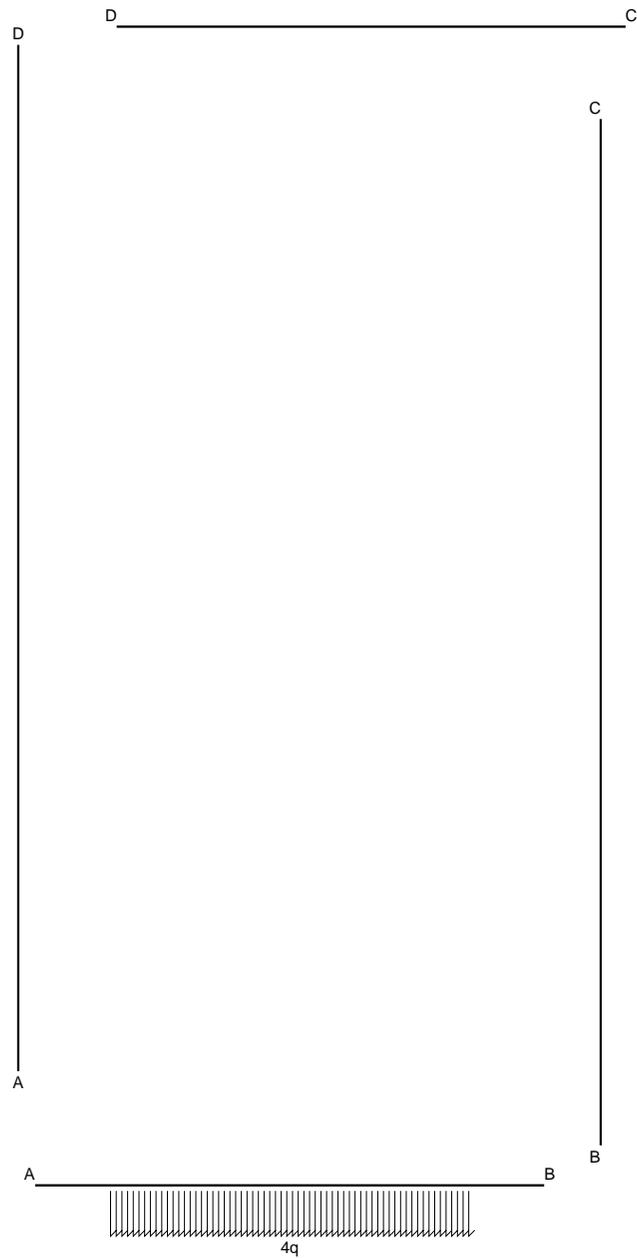


Svolgere l'analisi cinematica.
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 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $H_C =$ $V_C =$

$N_{DA} =$

$H_{AB} =$

$H_{BC} =$

$H_{CD} =$

$V_{AB} =$

$V_{BC} =$

$V_{CD} =$

$W_{AB} =$

$W_{BC} =$

$W_{CD} =$

$H_{BA} =$

$H_{CB} =$

$H_{DC} =$

$V_{BA} =$

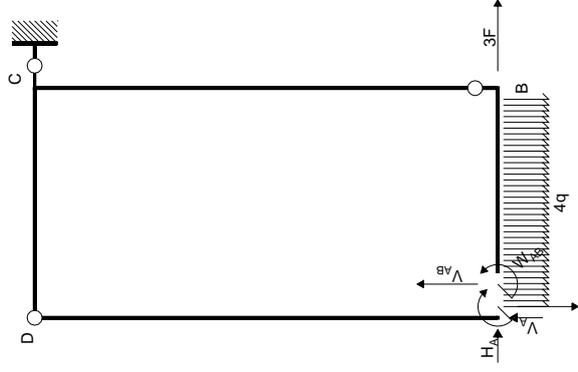
$V_{CB} =$

$V_{DC} =$

$W_{BA} =$

$W_{CB} =$

$W_{DC} =$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_A b - V_A b = -6Fb - 2qb^2$$

Rotazione intorno a B: aste BA

$$-V_{AB} b + W_{AB} = -2qb^2$$

Rotazione intorno a D: aste DA

$$2H_A b - W_{AB} = 0$$

Rapporto tra componenti nodo ZA

$$-W_{AB} = 0$$

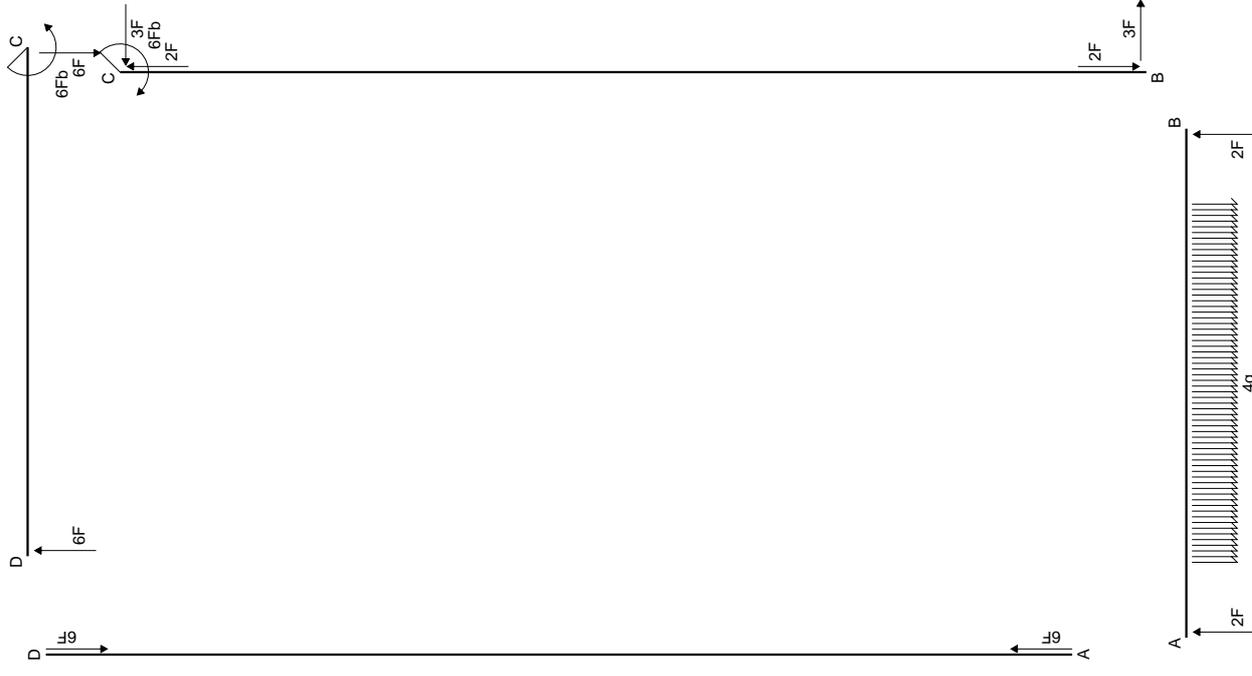
Matrice di equilibrio

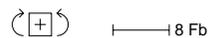
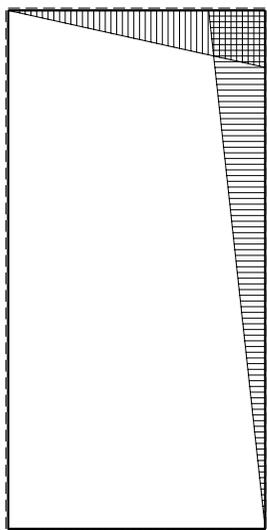
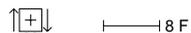
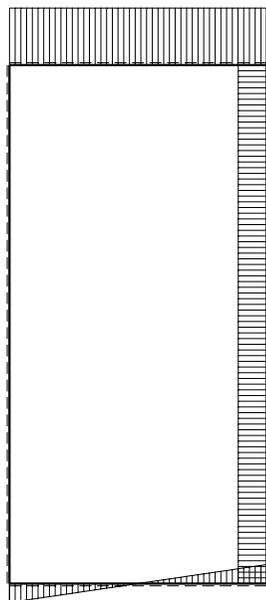
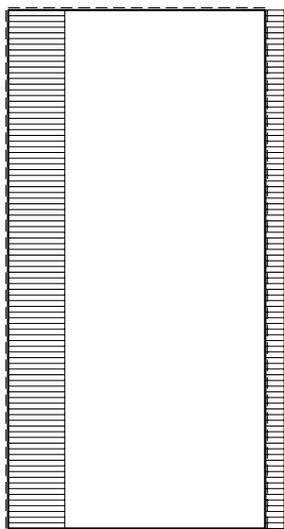
$$\begin{bmatrix} H_A b & V_A b & V_{AB} b & W_{AB} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \\ -6 & -2 \\ 0 & -2 \\ 0 & 0 \end{bmatrix}$$

$$\varphi_C \begin{bmatrix} 2 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 2 & 0 & 0 & -1 \\ 0 & 0 & 0 & -1 \end{bmatrix} = \begin{bmatrix} -6 & -2 \\ 0 & -2 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_{AB} b \\ V_A b \\ W_{AB} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 6 & 2 \\ 0 & 0 \end{bmatrix}$$



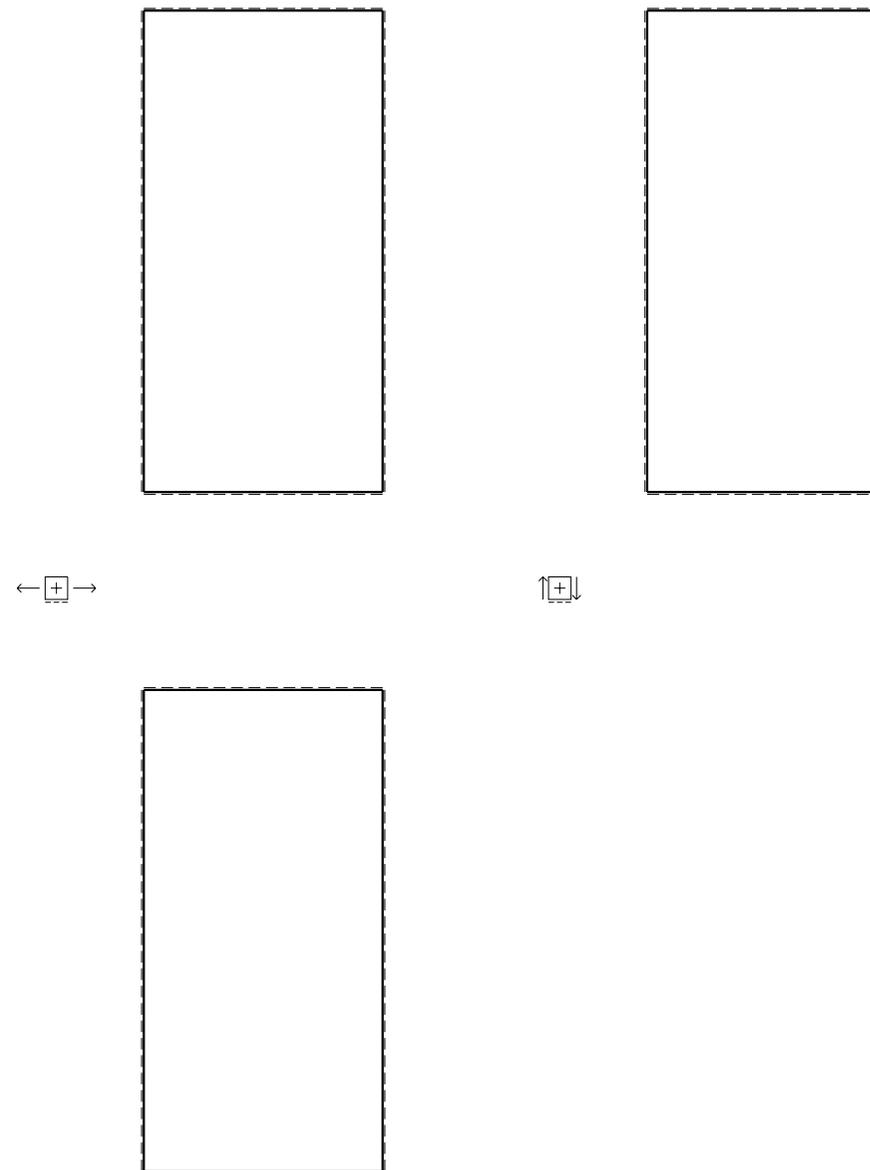
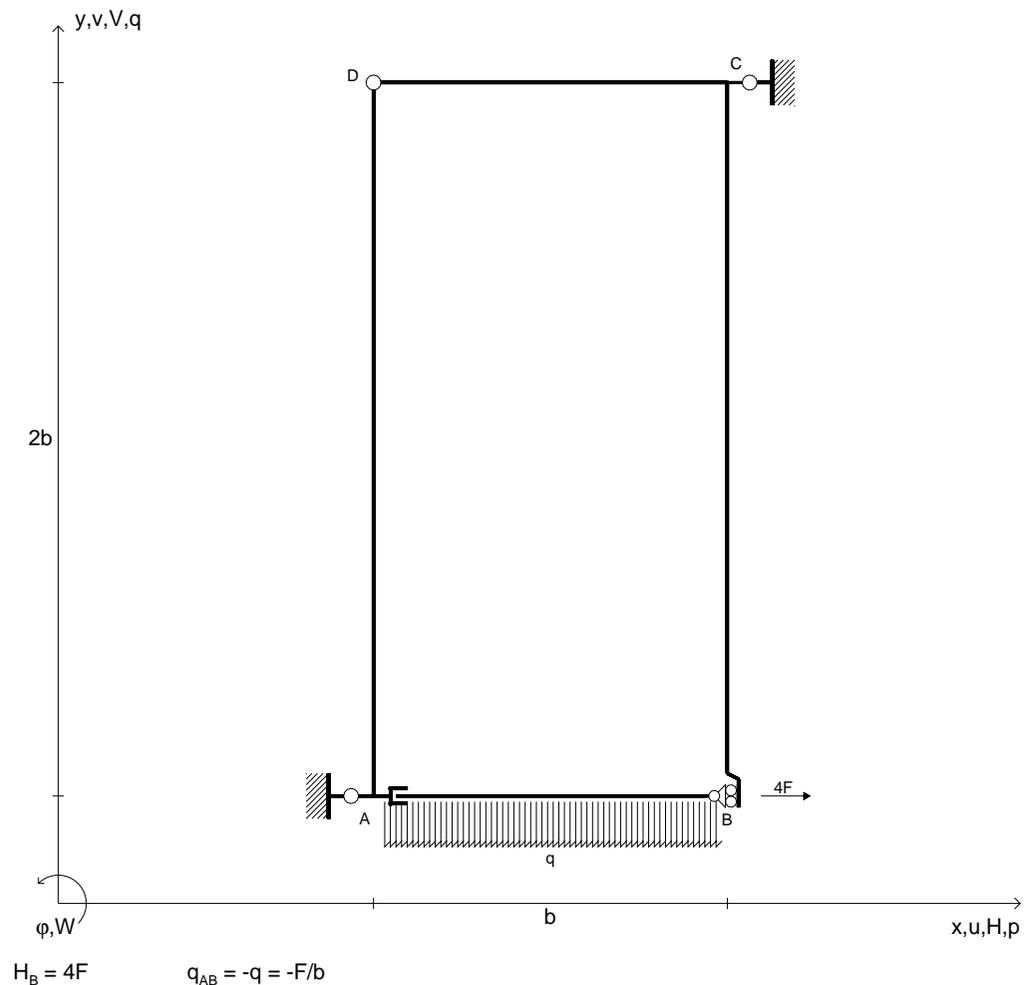


REAZIONI

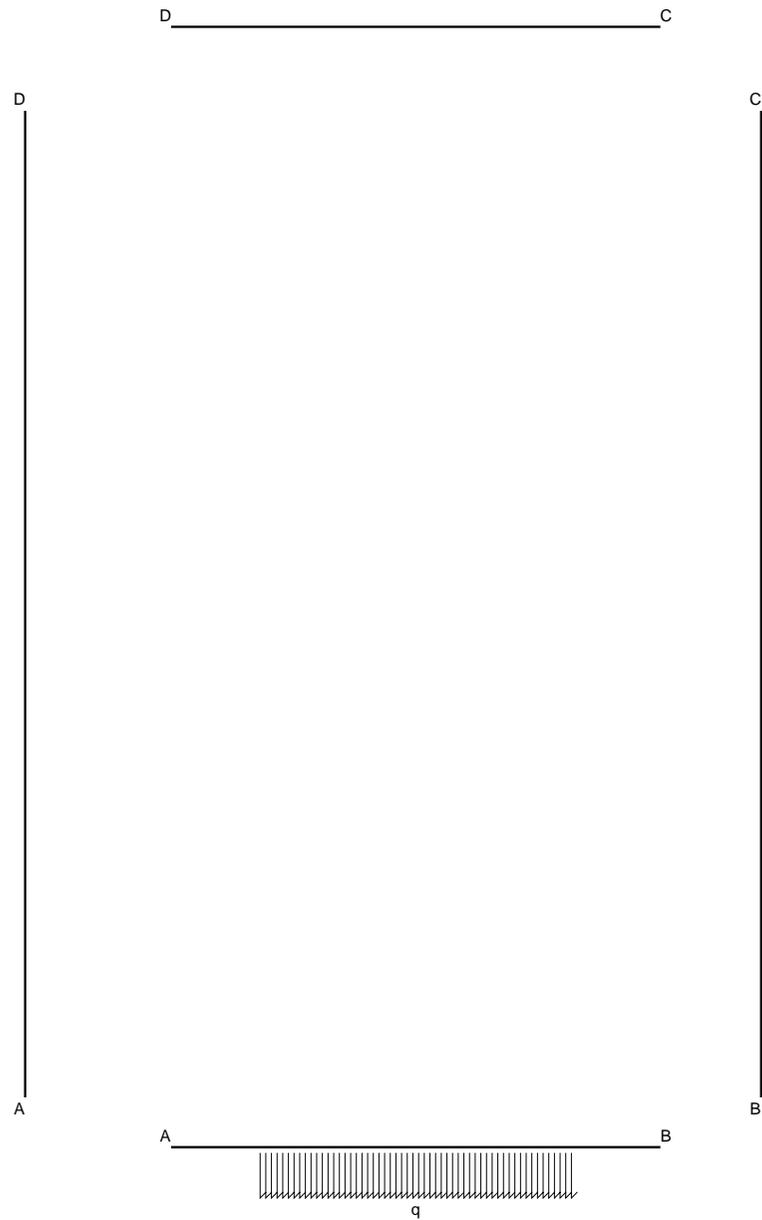
$$H_A = 0 \qquad V_A = 6F + 2qb = 8F \qquad H_C = -3F = -3F \qquad V_C = -6F + 2qb = -4F$$

$$N_{DA} = -6F = -6F$$

$H_{AB} = 0$	$H_{BC} = 3F = 3F$	$H_{CD} = 0$
$V_{AB} = 2qb = 2F$	$V_{BC} = -2qb = -2F$	$V_{CD} = -6F = -6F$
$W_{AB} = 0$	$W_{BC} = 0$	$W_{CD} = 6Fb = 6Fb$
$H_{BA} = 0$	$H_{CB} = -3F = -3F$	$H_{DC} = 0$
$V_{BA} = 2qb = 2F$	$V_{CB} = 2qb = 2F$	$V_{DC} = 6F = 6F$
$W_{BA} = 0$	$W_{CB} = -6Fb = -6Fb$	$W_{DC} = 0$



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REAZIONI

$H_A =$
 $V_A =$

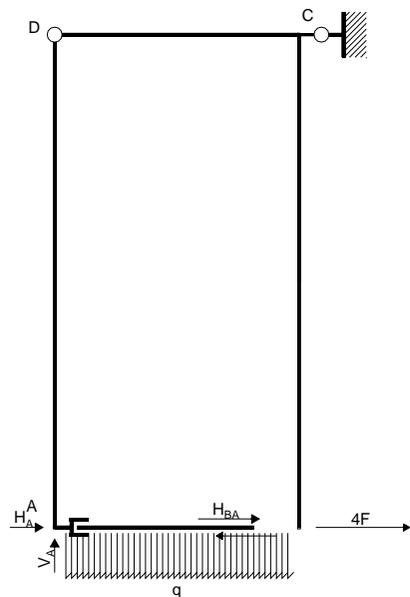
$H_C =$
 $V_C =$

$H_{AB} =$
 $V_{AB} =$
 $W_{AB} =$
 $H_{BA} =$
 $V_{BA} =$
 $W_{BA} =$

$H_{BC} =$
 $V_{BC} =$
 $W_{BC} =$
 $H_{CB} =$
 $V_{CB} =$
 $W_{CB} =$

$H_{CD} =$
 $V_{CD} =$
 $W_{CD} =$
 $H_{DC} =$
 $V_{DC} =$
 $W_{DC} =$

$H_{DA} =$
 $V_{DA} =$
 $W_{DA} =$
 $H_{AD} =$
 $V_{AD} =$
 $W_{AD} =$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_A b - V_A b = -8Fb - 1/2qb^2$$

Rotazione intorno a D: aste DA AB

$$2H_A b + 2H_{BA} b = 1/2qb^2$$

Traslazione orizzontale: aste AB

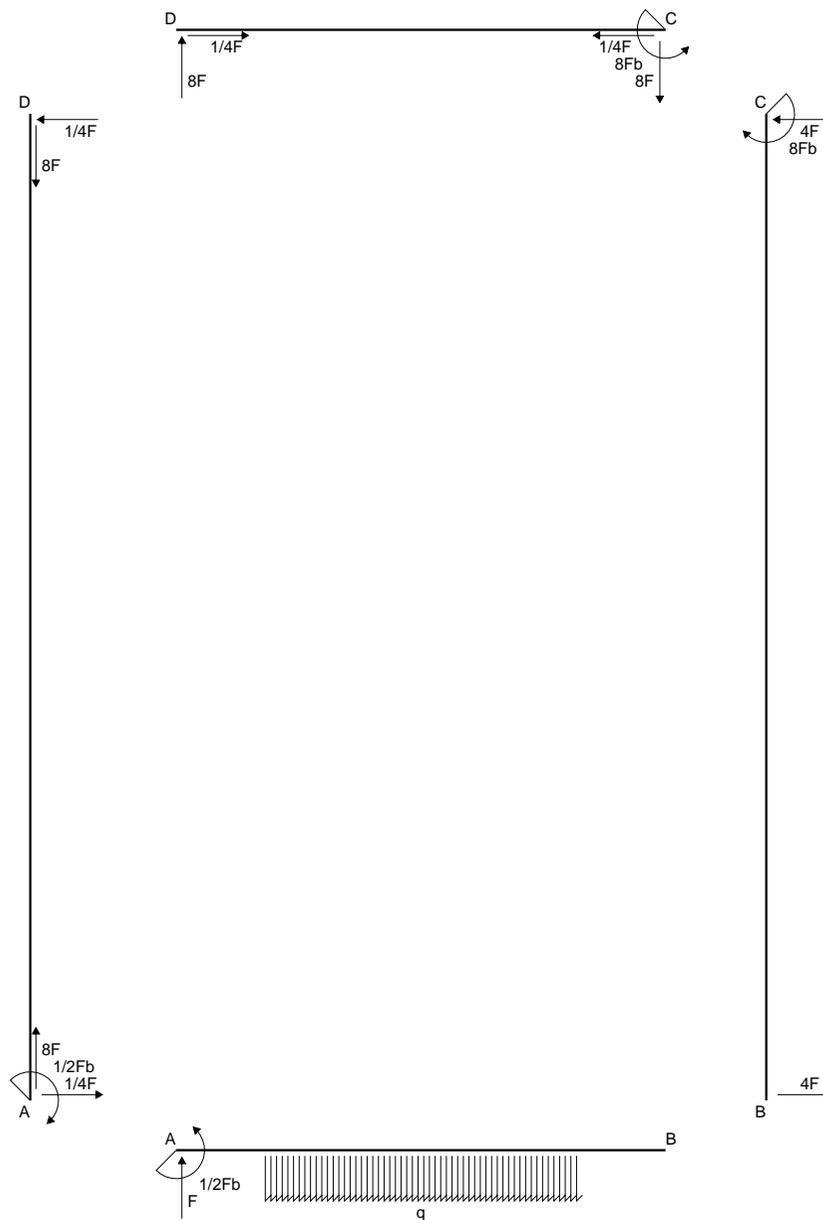
$$H_{BA} = 0$$

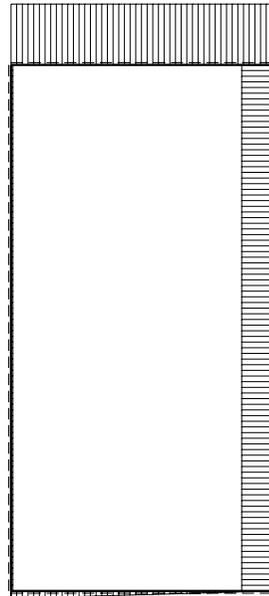
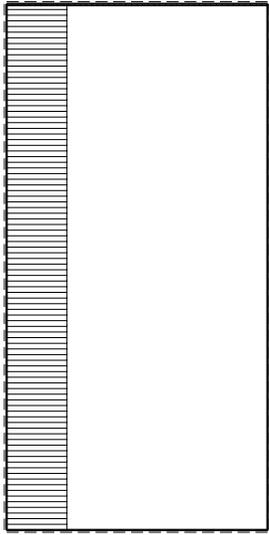
Matrice di equilibrio

$$\begin{matrix} \varphi_C \\ \varphi_{DA} \\ u_{AB} \end{matrix} \begin{bmatrix} H_A b & V_A b & H_{BA} b \\ 2 & -1 & 0 \\ 2 & 0 & 2 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -8 & -1/2 \\ 0 & 1/2 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

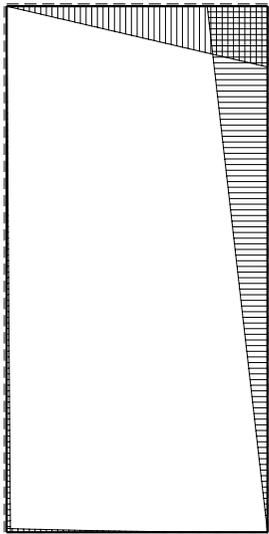
$$\begin{bmatrix} H_A b \\ V_A b \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 1/4 \\ 8 & 1 \\ 0 & 0 \end{bmatrix}$$





← ⊕ → | 10 F

↑ ⊕ ↓ | 10 F



⊕ ↻ | 10 Fb

REAZIONI

$$H_A = 1/4qb = 1/4F$$

$$V_A = 8F + qb = 9F$$

$$H_C = -4F - 1/4qb = -17/4F$$

$$V_C = -8F = -8F$$

$$H_{AB} = 0$$

$$V_{AB} = qb = F$$

$$W_{AB} = 1/2qb^2 = 1/2Fb$$

$$H_{BA} = 0$$

$$V_{BA} = 0$$

$$W_{BA} = 0$$

$$H_{BC} = 4F = 4F$$

$$V_{BC} = 0$$

$$W_{BC} = 0$$

$$H_{CB} = -4F = -4F$$

$$V_{CB} = 0$$

$$W_{CB} = -8Fb = -8Fb$$

$$H_{CD} = -1/4qb = -1/4F$$

$$V_{CD} = -8F = -8F$$

$$W_{CD} = 8Fb = 8Fb$$

$$H_{DC} = 1/4qb = 1/4F$$

$$V_{DC} = 8F = 8F$$

$$W_{DC} = 0$$

$$H_{DA} = -1/4qb = -1/4F$$

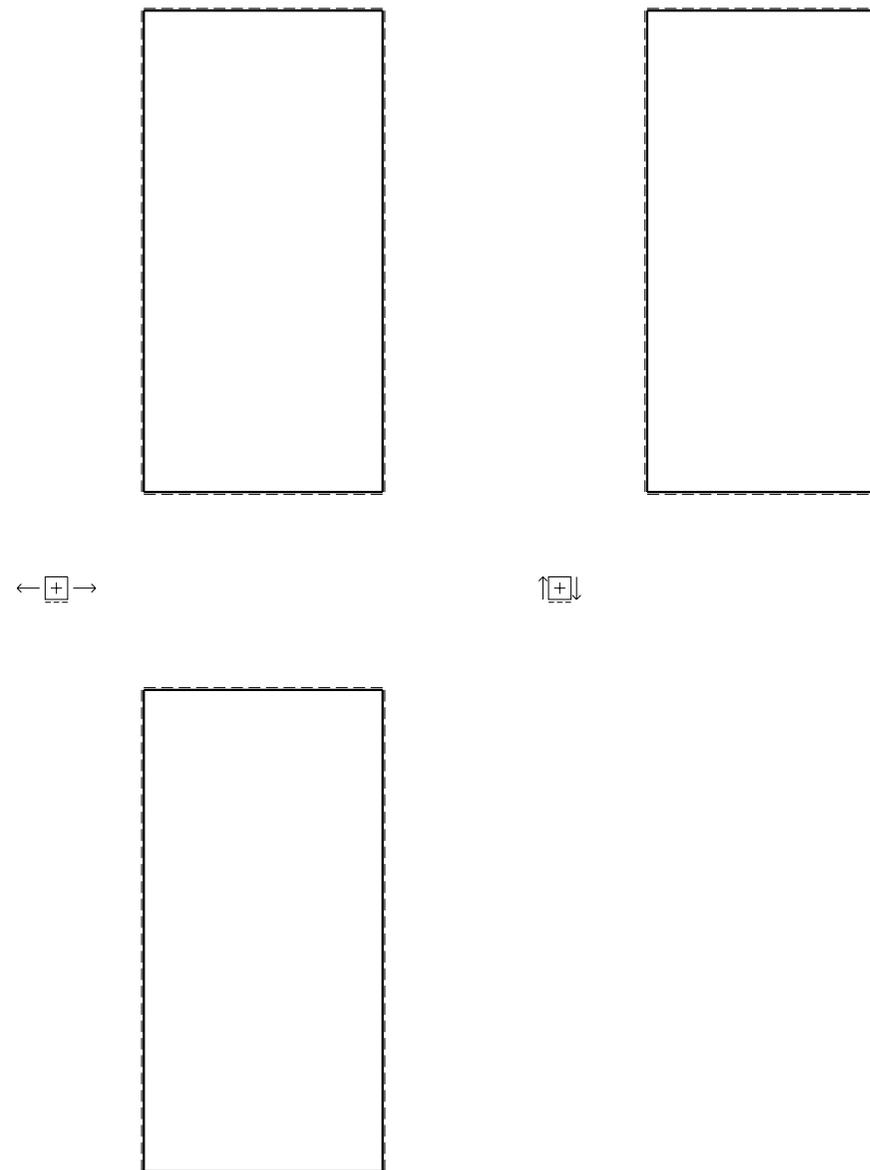
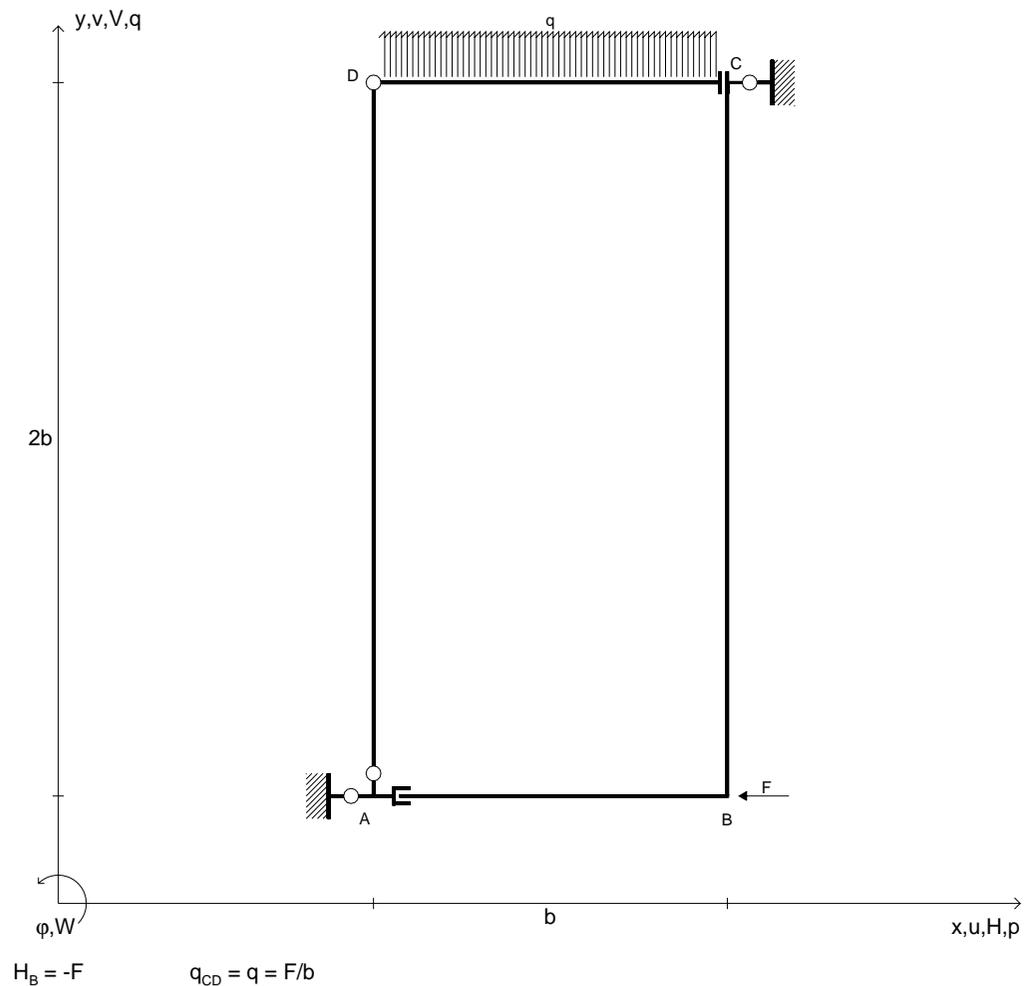
$$V_{DA} = -8F = -8F$$

$$W_{DA} = 0$$

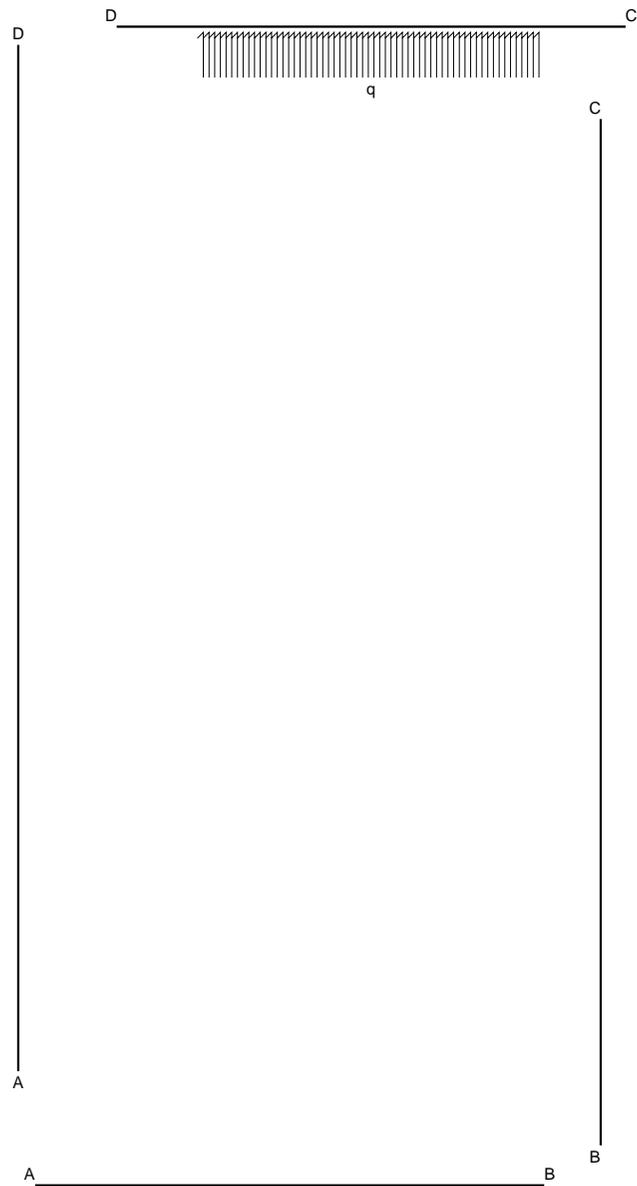
$$H_{AD} = 1/4qb = 1/4F$$

$$V_{AD} = 8F = 8F$$

$$W_{AD} = -1/2qb^2 = -1/2Fb$$



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REAZIONI

$H_A =$ $V_A =$ $H_C =$ $V_C =$

$N_{DA} =$

$H_{AB} =$

$H_{BC} =$

$H_{CD} =$

$V_{AB} =$

$V_{BC} =$

$V_{CD} =$

$W_{AB} =$

$W_{BC} =$

$W_{CD} =$

$H_{BA} =$

$H_{CB} =$

$H_{DC} =$

$V_{BA} =$

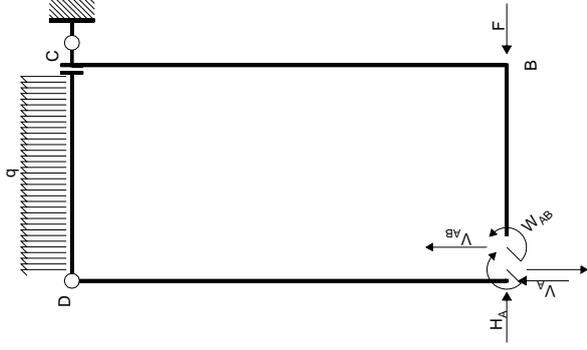
$V_{CB} =$

$V_{DC} =$

$W_{BA} =$

$W_{CB} =$

$W_{DC} =$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_{A,b} - V_{A,b} = 2Fb + 1/2qb^2$$

Traslazione verticale: aste CD DA

$$V_A - V_{AB} = -qb$$

Rotazione intorno a D: aste DA

$$2H_{A,b} - W_{AB} = 0$$

Rapporto tra componenti nodo ZA

$$-W_{AB} = 0$$

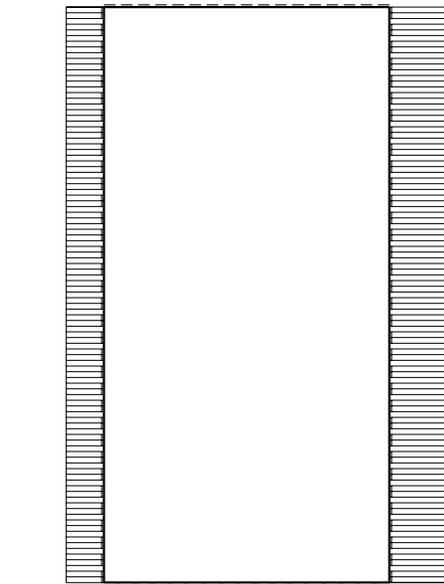
Matrice di equilibrio

$$\begin{bmatrix} H_{A,b} & V_{A,b} & V_{AB,b} & W_{AB} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \\ 2 & 1/2 \\ 0 & 0 \\ 0 & -1 \end{bmatrix} = \begin{bmatrix} 2 & 1/2 \\ 0 & -1 \\ 2 & 0 \\ 0 & -1 \end{bmatrix}$$

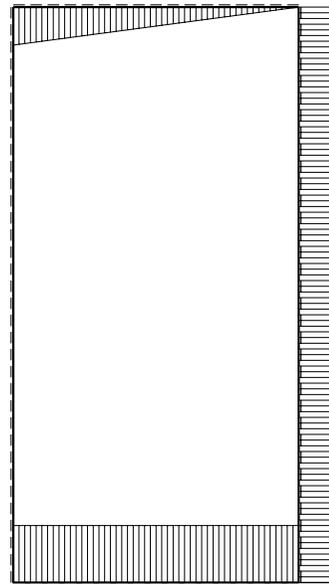
Soluzione del sistema

$$\begin{bmatrix} H_{A,b} \\ V_{A,b} \\ V_{AB,b} \\ W_{AB} \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 0 \\ -2 & -1/2 \\ -2 & 1/2 \\ 0 & 0 \end{bmatrix}$$

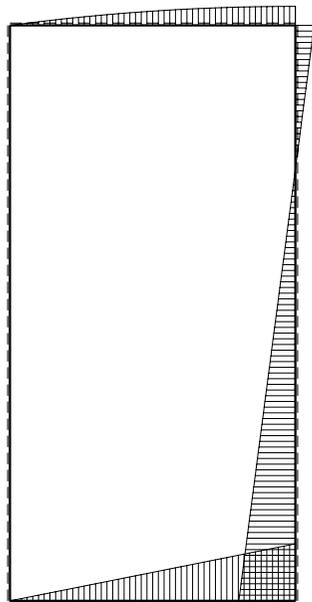




← ⊕ → | 2 F



↑ ⊕ ↓ | 2 F



⊕ ↻ | 2 Fb

REAZIONI

$H_A = 0$

$V_A = -2F - 1/2qb = -5/2F$ $H_C = F = F$

$V_C = 2F - 1/2qb = 3/2F$

$N_{DA} = qb = F$

$H_{AB} = 0$

$V_{AB} = -2F + 1/2qb = -3/2F$

$W_{AB} = 0$

$H_{BA} = 0$

$V_{BA} = 2F - 1/2qb = 3/2F$

$W_{BA} = -2Fb + 1/2qb^2 = -3/2Fb$

$H_{BC} = -F = -F$

$V_{BC} = -2F + 1/2qb = -3/2F$

$W_{BC} = 2Fb - 1/2qb^2 = 3/2Fb$

$H_{CB} = F = F$

$V_{CB} = 2F - 1/2qb = 3/2F$

$W_{CB} = 1/2qb^2 = 1/2Fb$

$H_{CD} = 0$

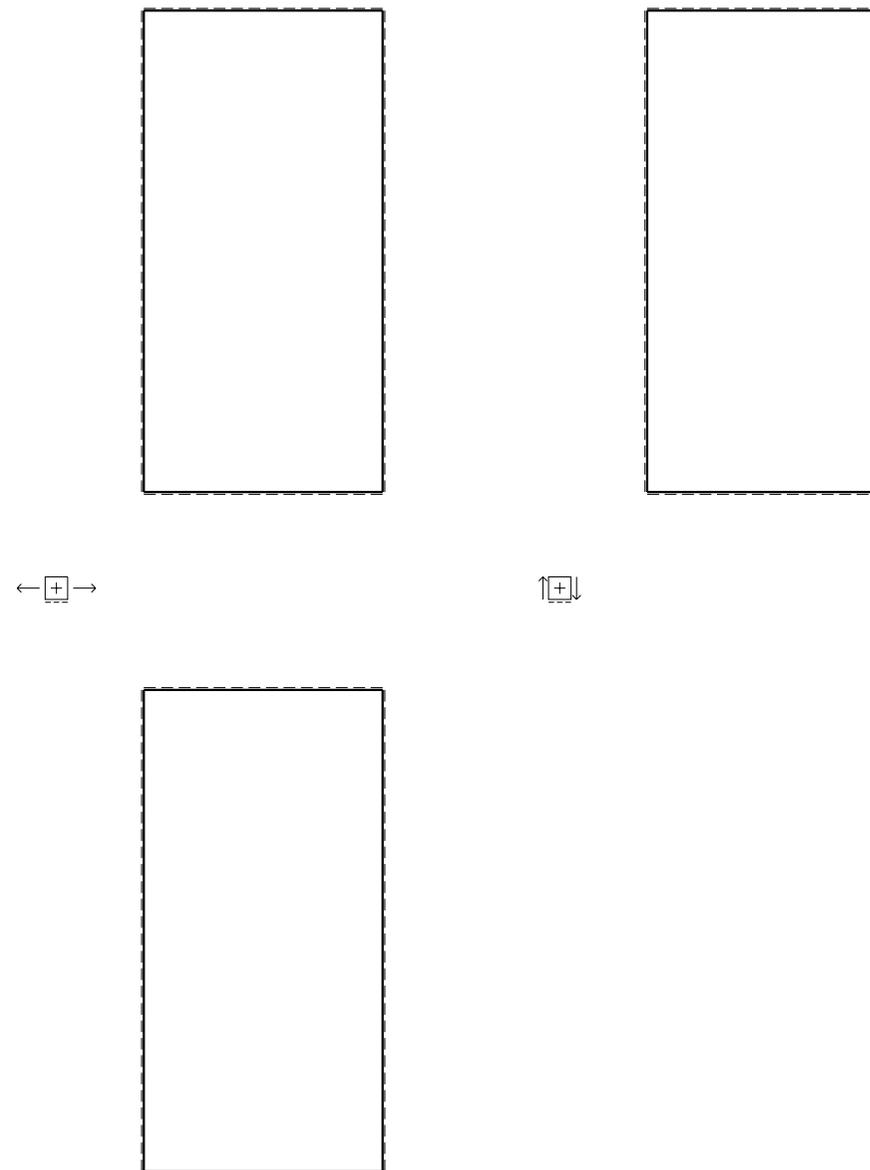
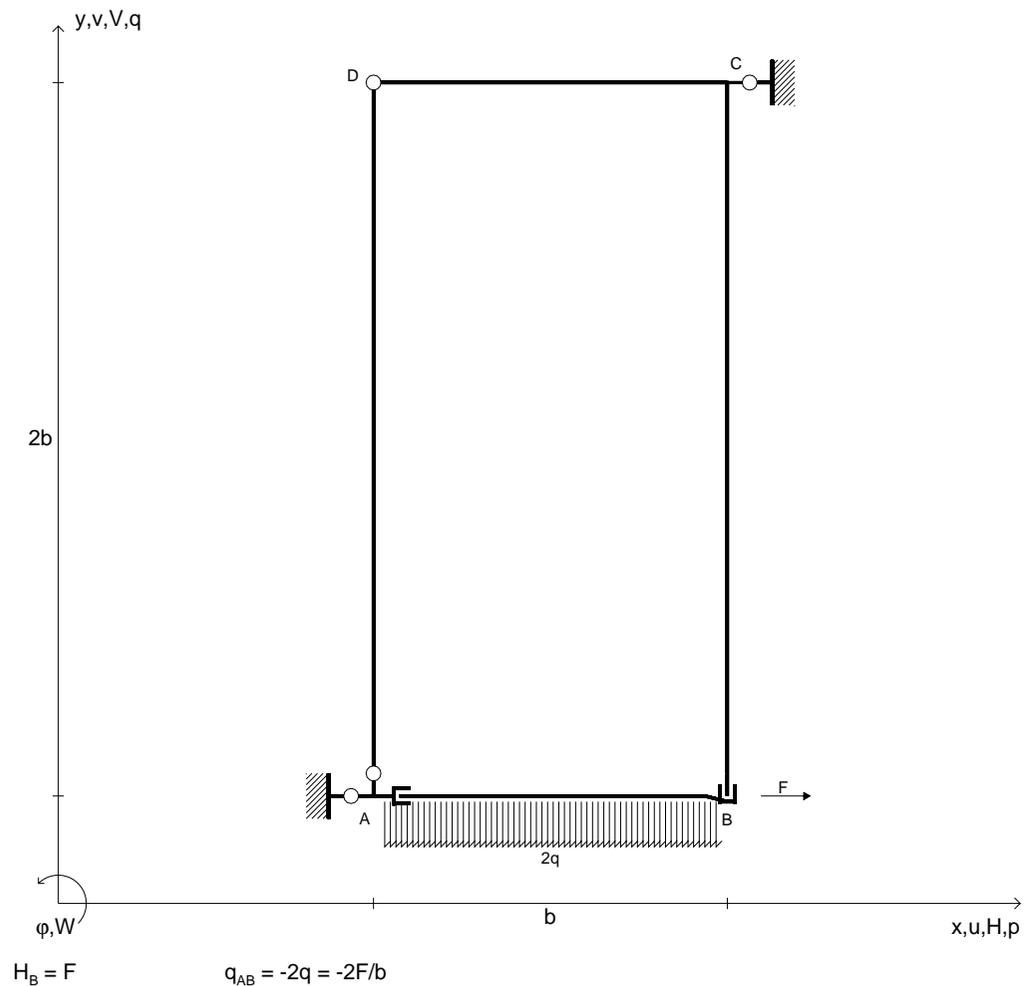
$V_{CD} = 0$

$W_{CD} = -1/2qb^2 = -1/2Fb$

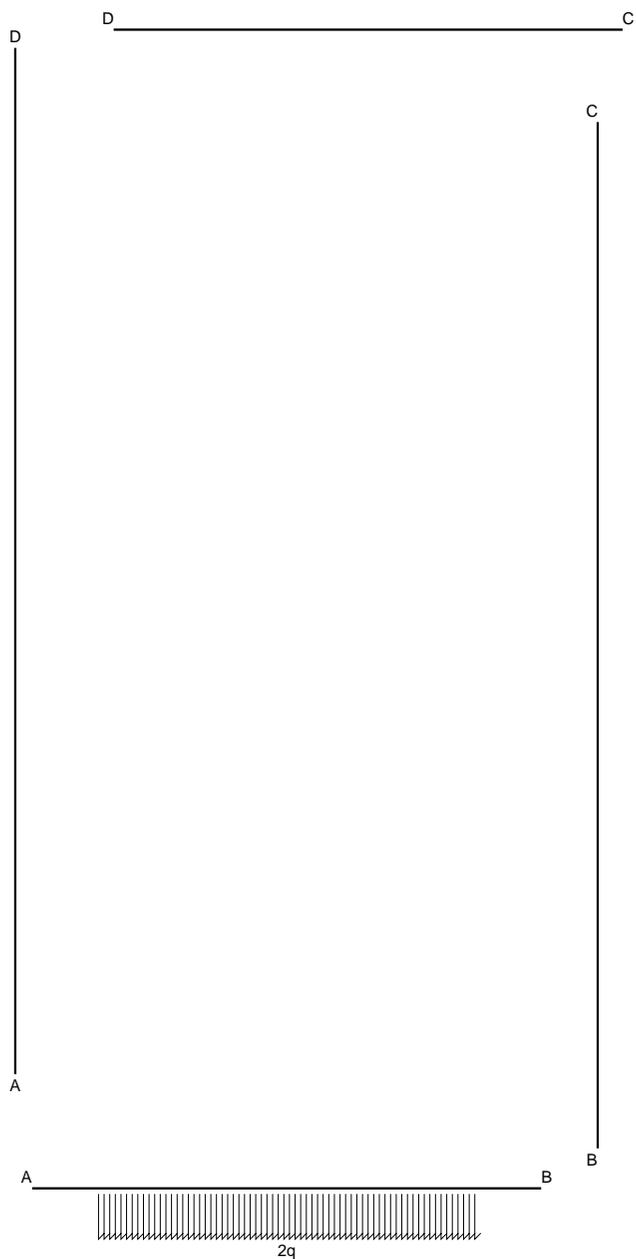
$H_{DC} = 0$

$V_{DC} = -qb = -F$

$W_{DC} = 0$



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REAZIONI

$H_A =$ $V_A =$ $H_C =$ $V_C =$

$N_{DA} =$

$H_{AB} =$	$H_{BC} =$	$H_{CD} =$
$V_{AB} =$	$V_{BC} =$	$V_{CD} =$
$W_{AB} =$	$W_{BC} =$	$W_{CD} =$
$H_{BA} =$	$H_{CB} =$	$H_{DC} =$
$V_{BA} =$	$V_{CB} =$	$V_{DC} =$
$W_{BA} =$	$W_{CB} =$	$W_{DC} =$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_A b - V_A b = -2Fb - qb^2$$

Rotazione intorno a D: aste DA AB

$$2H_A b + 2H_{BA} b + W_{BA} = qb^2$$

Rotazione intorno a A: aste AB

$$W_{BA} = qb^2$$

Traslazione orizzontale: aste AB

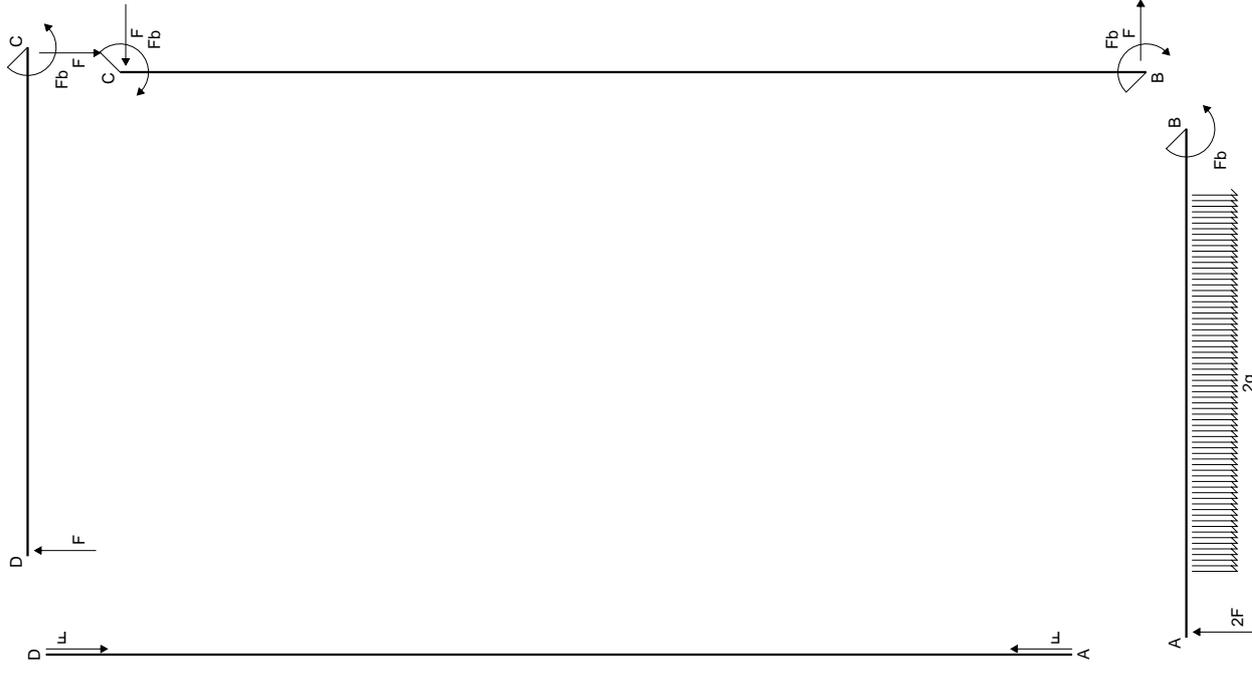
$$H_{BA} = 0$$

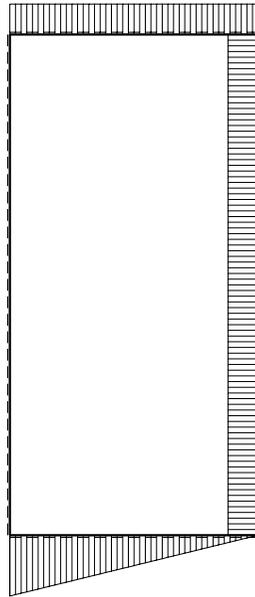
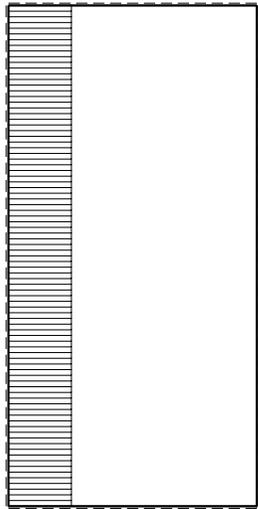
Matrice di equilibrio

$$\begin{bmatrix} H_A b & V_A b & H_{BA} b & W_{BA} \\ \varphi_C & 2 & -1 & 0 & 0 \\ \varphi_{DA} & 2 & 0 & 2 & 1 \\ \varphi_{AD} & 0 & 0 & 0 & 1 \\ U_{AB} & 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} Fb \\ qb^2 \\ -2 \\ 0 \\ 1 \end{bmatrix}$$

Soluzione del sistema

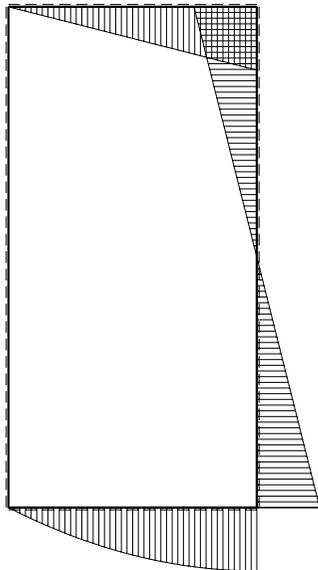
$$\begin{bmatrix} H_A b \\ V_A b \\ W_{BA} \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 2 & 1 \\ 0 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} Fb \\ qb^2 \end{bmatrix}$$





← ⊕ → | 1.2 F

↑ ⊕ ↓ | 2.5 F



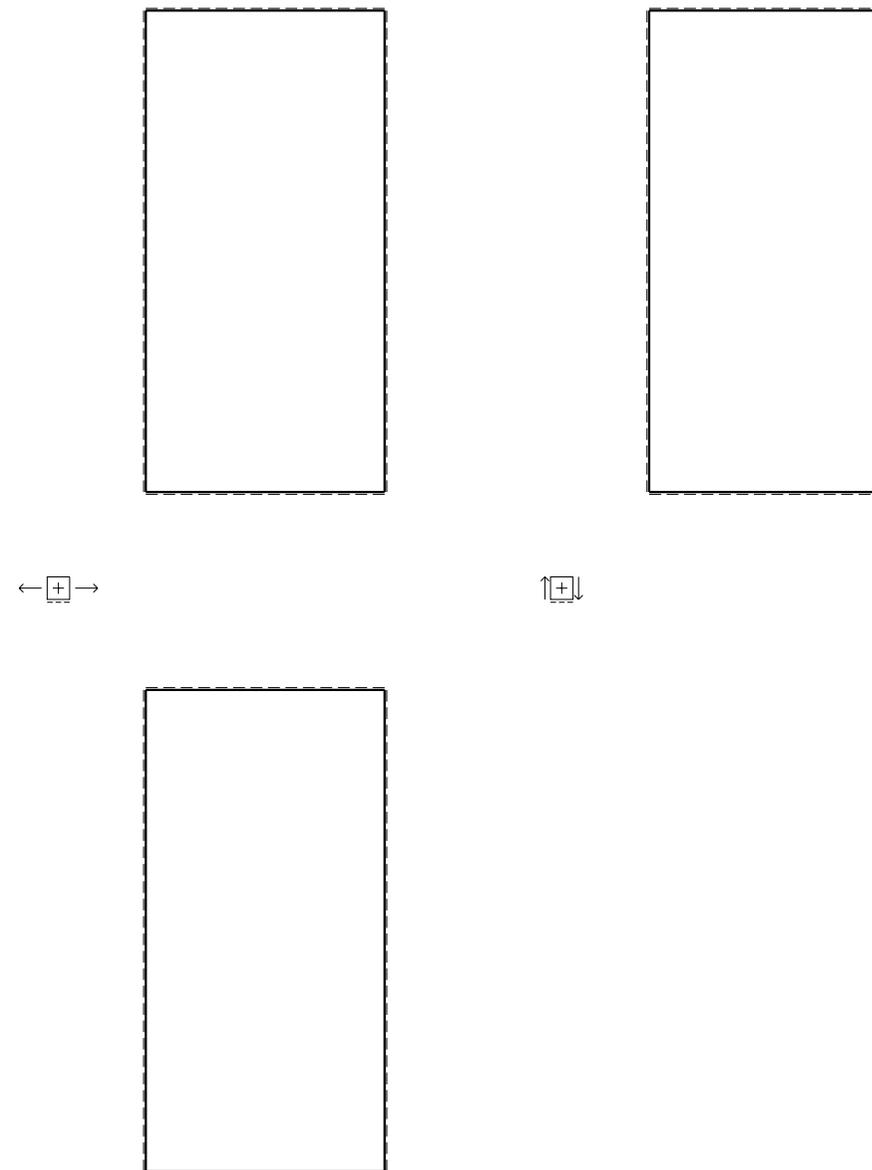
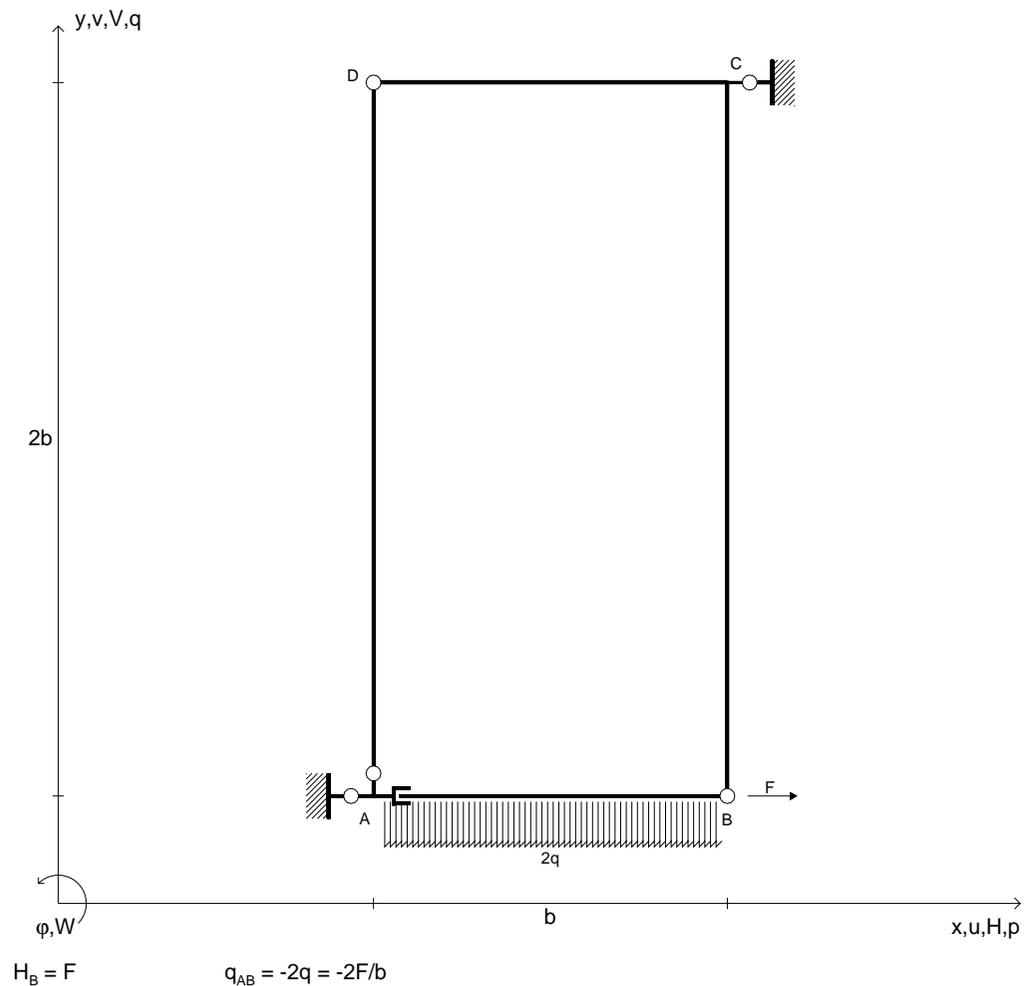
⊕ ↻ | 1.2 Fb

REAZIONI

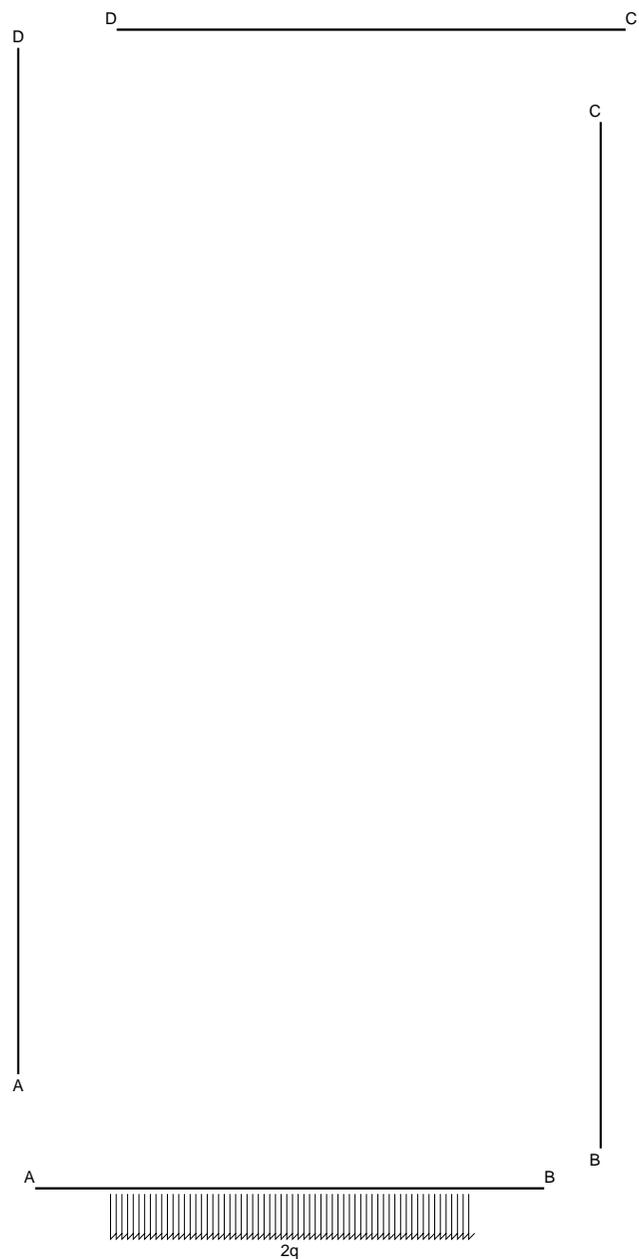
$H_A = 0$ $V_A = 2F + qb = 3F$ $H_C = -F = -F$ $V_C = -2F + qb = -F$

$N_{DA} = -2F + qb = -F$

$H_{AB} = 0$	$H_{BC} = F = F$	$H_{CD} = 0$
$V_{AB} = 2qb = 2F$	$V_{BC} = 0$	$V_{CD} = -2F + qb = -F$
$W_{AB} = 0$	$W_{BC} = -qb^2 = -Fb$	$W_{CD} = 2Fb - qb^2 = Fb$
$H_{BA} = 0$	$H_{CB} = -F = -F$	$H_{DC} = 0$
$V_{BA} = 0$	$V_{CB} = 0$	$V_{DC} = 2F - qb = F$
$W_{BA} = qb^2 = Fb$	$W_{CB} = -2Fb + qb^2 = -Fb$	$W_{DC} = 0$



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REAZIONI

$H_A =$ $V_A =$ $H_C =$ $V_C =$

$N_{DA} =$

$H_{AB} =$

$H_{BC} =$

$H_{CD} =$

$V_{AB} =$

$V_{BC} =$

$V_{CD} =$

$W_{AB} =$

$W_{BC} =$

$W_{CD} =$

$H_{BA} =$

$H_{CB} =$

$H_{DC} =$

$V_{BA} =$

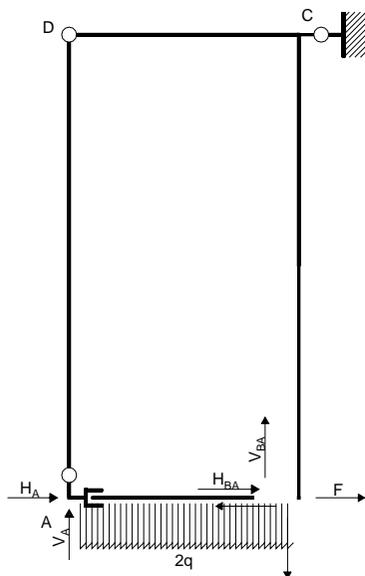
$V_{CB} =$

$V_{DC} =$

$W_{BA} =$

$W_{CB} =$

$W_{DC} =$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

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Rotazione intorno a D: aste DA AB

$$2H_A b + 2H_{BA} b + V_{BA} b = qb^2$$

Rotazione intorno a A: aste AB

$$V_{BA} b = qb^2$$

Traslazione orizzontale: aste AB

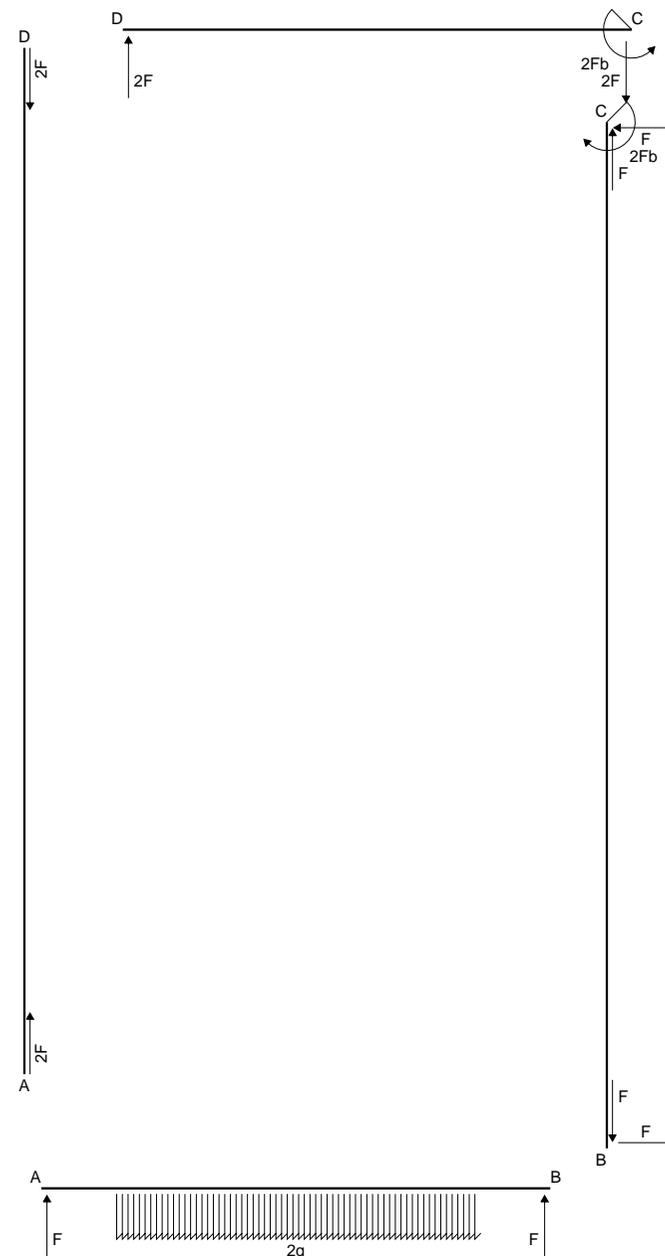
$$H_{BA} = 0$$

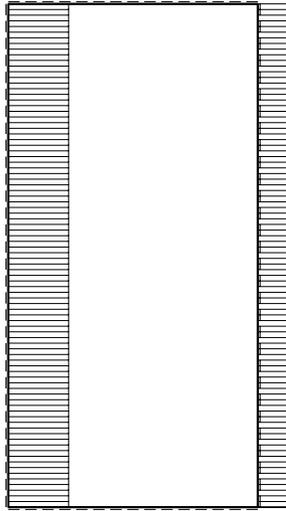
Matrice di equilibrio

$$\begin{matrix} \varphi_C \\ \varphi_{DA} \\ \varphi_{AD} \\ u_{AB} \end{matrix} \begin{bmatrix} H_A b & V_A b & H_{BA} b & V_{BA} b \\ 2 & -1 & 0 & 0 \\ 2 & 0 & 2 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -2 & -1 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}$$

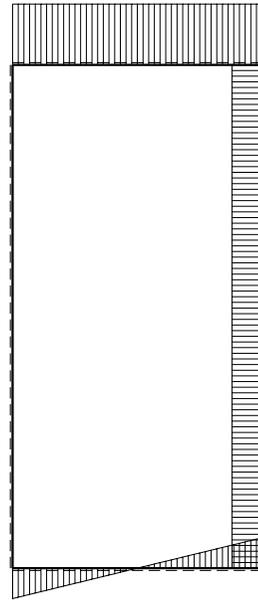
Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \\ V_{BA} b \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 0 \\ 2 & 1 \\ 0 & 0 \end{bmatrix}$$

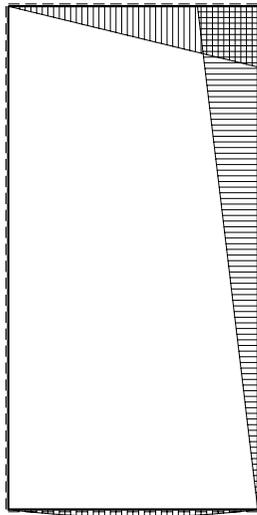




← ⊕ → | 2.5 F



↑ ⊕ ↓ | 2.5 F



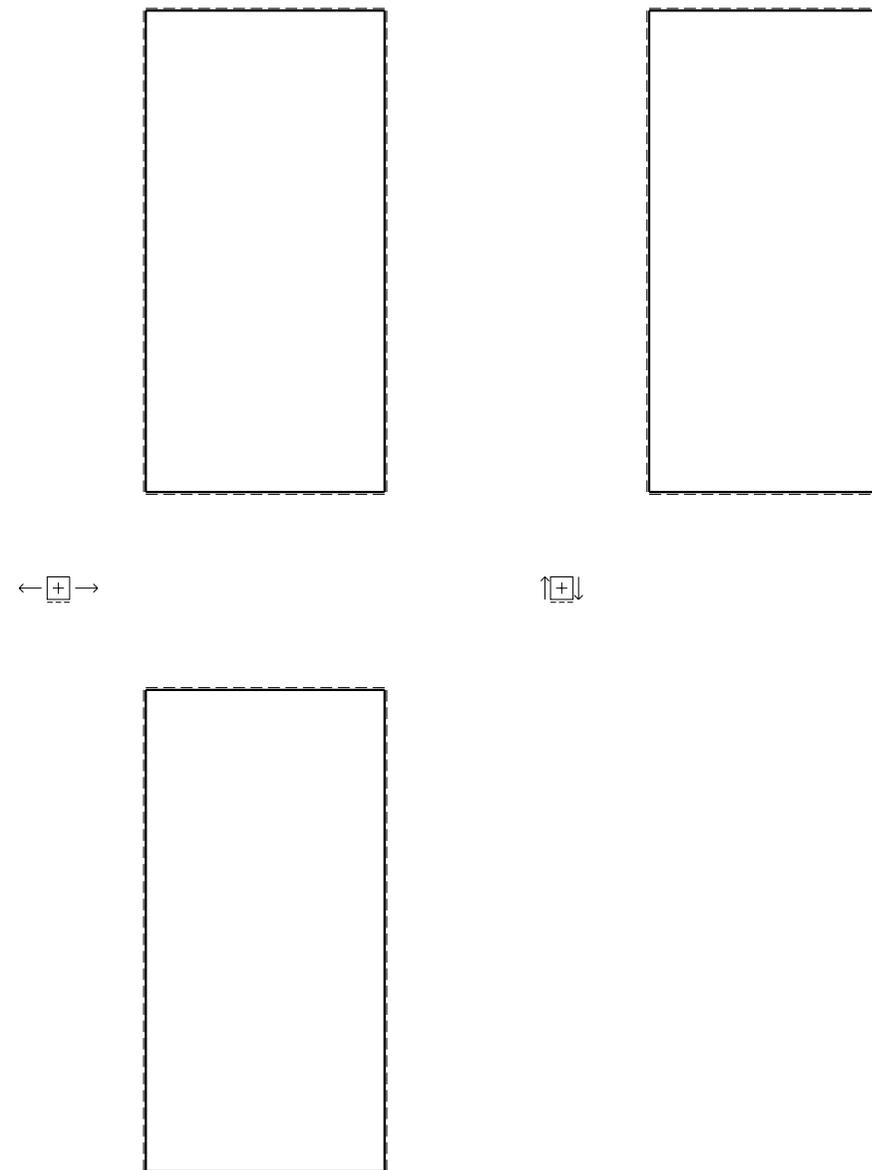
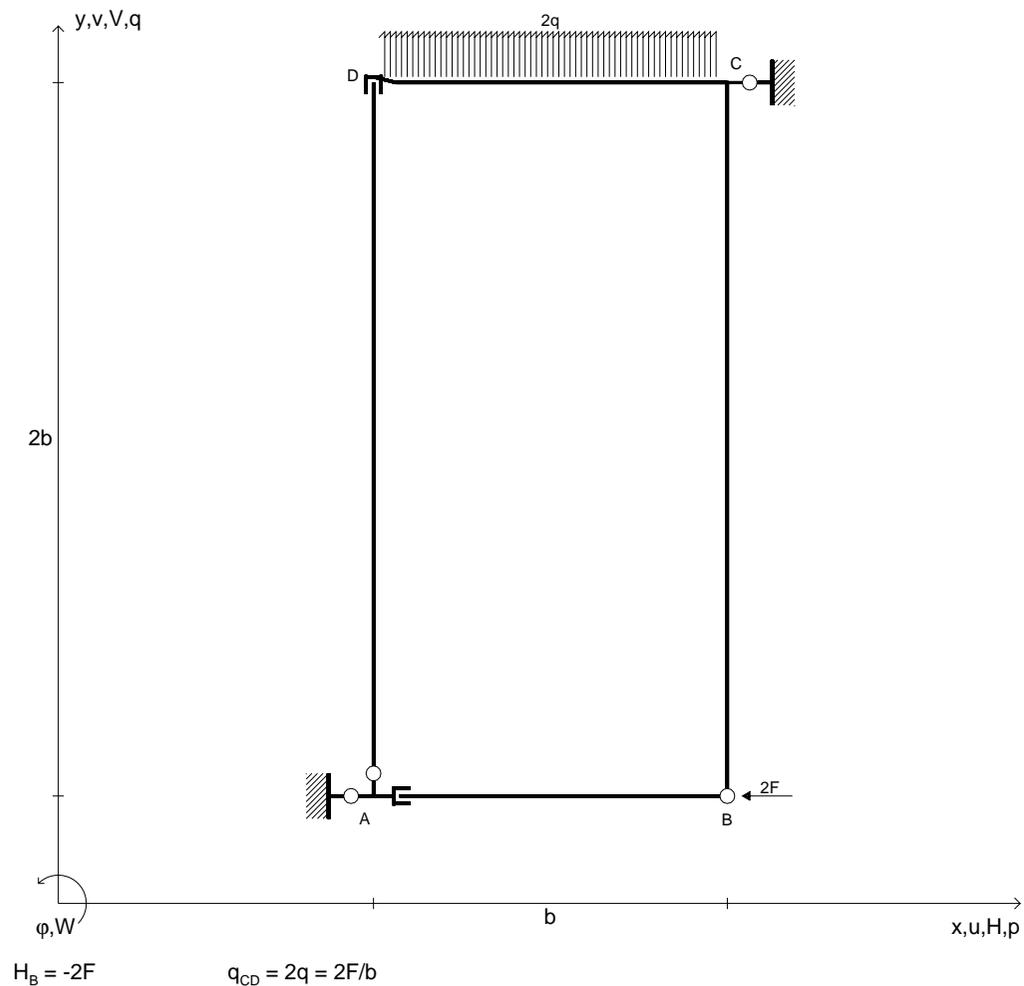
⊕ ↻ | 2.5 Fb

REAZIONI

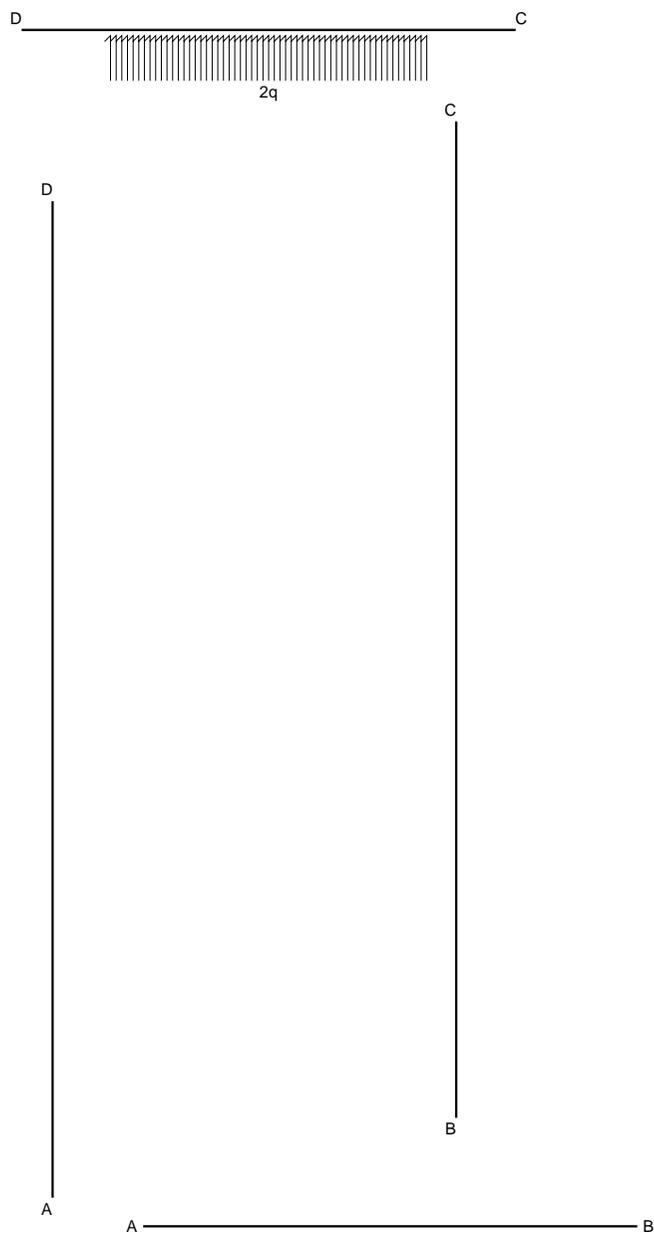
$$H_A = 0 \quad V_A = 2F + qb = 3F \quad H_C = -F = -F \quad V_C = -2F + qb = -F$$

$$N_{DA} = -2F = -2F$$

$H_{AB} = 0$	$H_{BC} = F = F$	$H_{CD} = 0$
$V_{AB} = qb = F$	$V_{BC} = -qb = -F$	$V_{CD} = -2F = -2F$
$W_{AB} = 0$	$W_{BC} = 0$	$W_{CD} = 2Fb = 2Fb$
$H_{BA} = 0$	$H_{CB} = -F = -F$	$H_{DC} = 0$
$V_{BA} = qb = F$	$V_{CB} = qb = F$	$V_{DC} = 2F = 2F$
$W_{BA} = 0$	$W_{CB} = -2Fb = -2Fb$	$W_{DC} = 0$

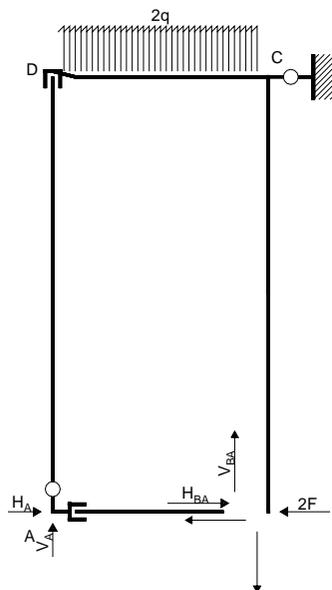


Svolgere l'analisi cinematica.
 Determinare matrice di congruenza e di equilibrio.
 Determinare le reazioni vincolari a terra col PLV ($Le=0$).
 Determinare le azioni interne in C col PLV ($Le=0$).
 Carichi e deformazioni date hanno verso efficace in disegno.
 Calcolare reazioni vincolari della struttura e delle aste.
 Tracciare i diagrammi delle azioni interne nelle aste.
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

- | | | | |
|------------|---------|------------|------------|
| $H_A =$ | $V_A =$ | $H_C =$ | $V_C =$ |
| $H_{AB} =$ | | $H_{BC} =$ | $H_{CD} =$ |
| $V_{AB} =$ | | $V_{BC} =$ | $V_{CD} =$ |
| $W_{AB} =$ | | $W_{BC} =$ | $W_{CD} =$ |
| $H_{BA} =$ | | $H_{CB} =$ | $H_{DC} =$ |
| $V_{BA} =$ | | $V_{CB} =$ | $V_{DC} =$ |
| $W_{BA} =$ | | $W_{CB} =$ | $W_{DC} =$ |
| $H_{DA} =$ | | | |
| $V_{DA} =$ | | | |
| $W_{DA} =$ | | | |
| $H_{AD} =$ | | | |
| $V_{AD} =$ | | | |
| $W_{AD} =$ | | | |



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_A b - V_A b = 4Fb + qb^2$$

Traslazione verticale: aste DA AB

$$V_A + V_{BA} = 0$$

Rotazione intorno a A: aste AB

$$V_{BA} b = 0$$

Traslazione orizzontale: aste AB

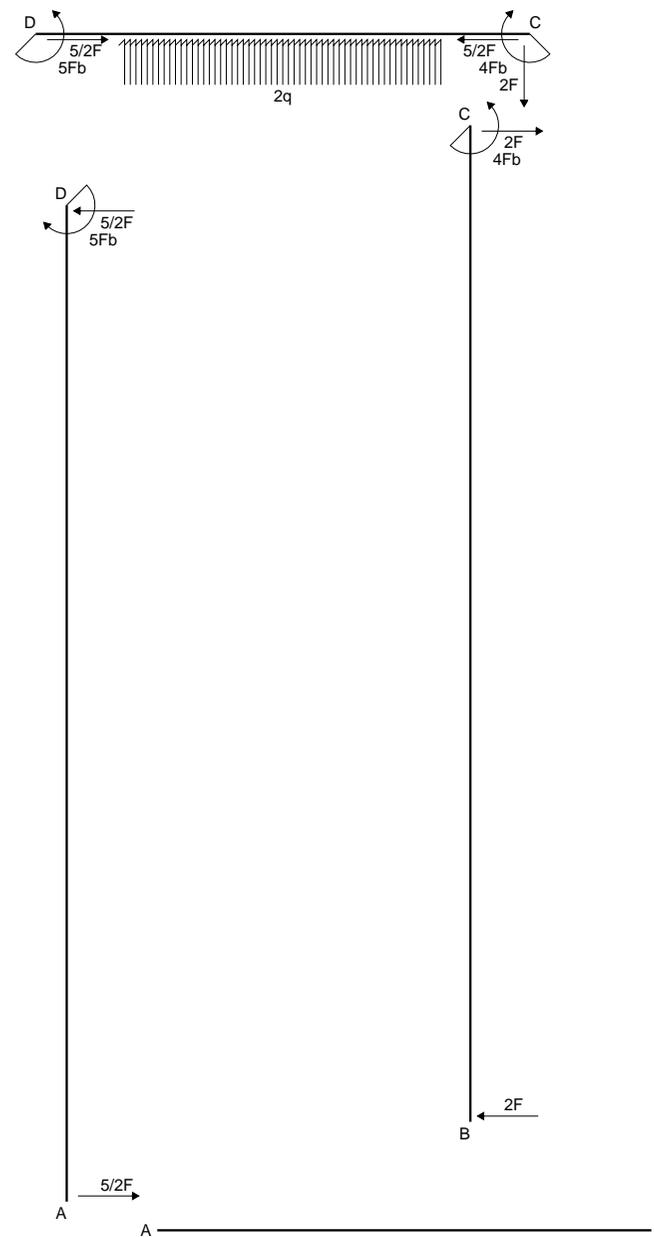
$$H_{BA} = 0$$

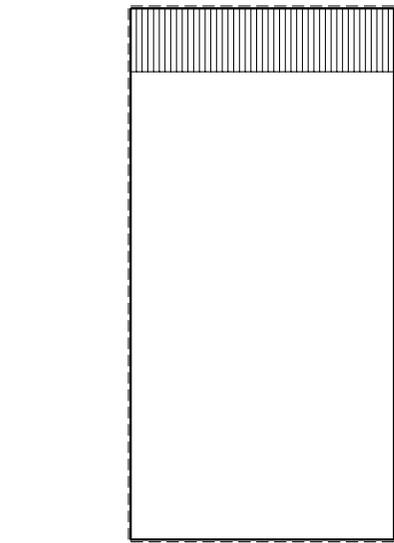
Matrice di equilibrio

$$\begin{bmatrix} \varphi_C \\ V_{DC} \\ \varphi_{AD} \\ u_{AB} \end{bmatrix} \begin{bmatrix} H_A b & V_A b & H_{BA} b & V_{BA} b \\ 2 & -1 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 4 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

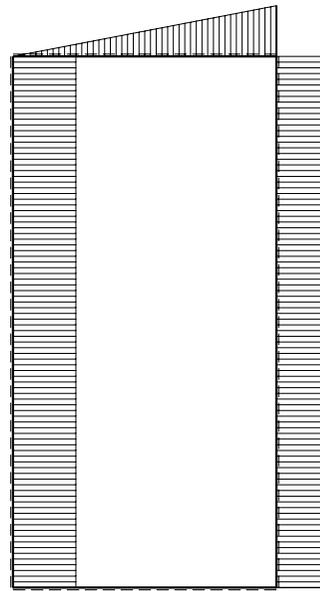
Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \\ V_{BA} b \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & 1/2 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

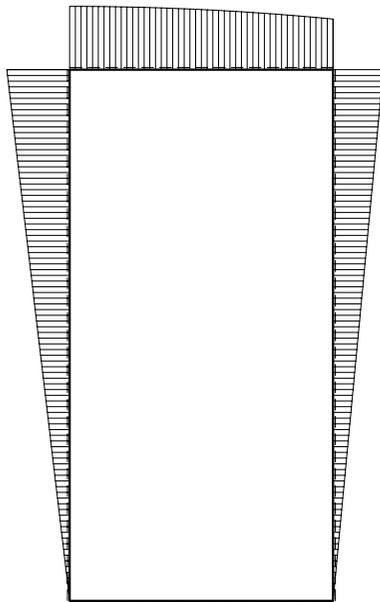




← ⊕ → | 3 F



↑ ⊕ ↓ | 3 F



⊕ ↻ | 6 Fb

REAZIONI

$$H_A = 2F + 1/2qb = 5/2F \quad V_A = 0$$

$$H_C = -1/2qb = -1/2F \quad V_C = -2qb = -2F$$

$$H_{AB} = 0$$

$$H_{BC} = -2F = -2F$$

$$H_{CD} = -2F - 1/2qb = -5/2F$$

$$V_{AB} = 0$$

$$V_{BC} = 0$$

$$V_{CD} = -2qb = -2F$$

$$W_{AB} = 0$$

$$W_{BC} = 0$$

$$W_{CD} = -4Fb = -4Fb$$

$$H_{BA} = 0$$

$$H_{CB} = 2F = 2F$$

$$H_{DC} = 2F + 1/2qb = 5/2F$$

$$V_{BA} = 0$$

$$V_{CB} = 0$$

$$V_{DC} = 0$$

$$W_{BA} = 0$$

$$W_{CB} = 4Fb = 4Fb$$

$$W_{DC} = 4Fb + qb^2 = 5Fb$$

$$H_{DA} = -2F - 1/2qb = -5/2F$$

$$V_{DA} = 0$$

$$W_{DA} = -4Fb - qb^2 = -5Fb$$

$$H_{AD} = 2F + 1/2qb = 5/2F$$

$$V_{AD} = 0$$

$$W_{AD} = 0$$