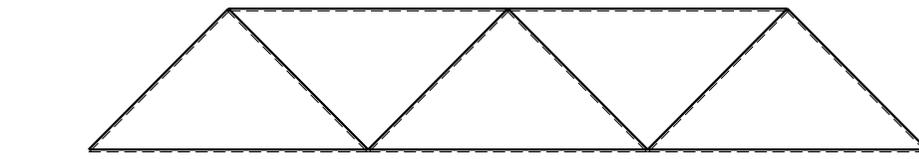
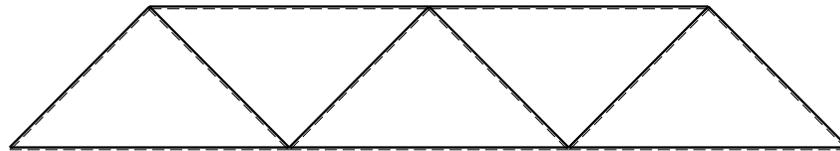


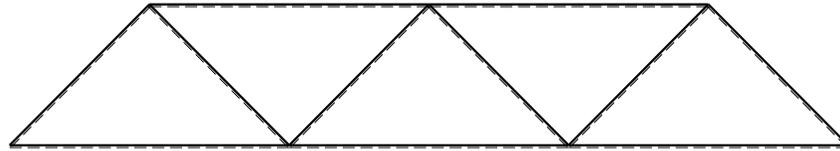
- | | | | |
|--|-----------------|----------------|----------------|
| $V_E = -2F$ | $v_F = ?$ | $EA_{EF} = EA$ | $EA_{BF} = EA$ |
| $V_G = 2F$ | $EA_{AB} = EA$ | $EA_{FG} = EA$ | $EA_{FC} = EA$ |
| $\varepsilon_{BC} = 2\alpha T = 2F/EA$ | $EA_{BC} = 2EA$ | $EA_{AE} = EA$ | $EA_{CG} = EA$ |
| $u_F = ?$ | $EA_{CD} = EA$ | $EA_{EB} = EA$ | $EA_{GD} = EA$ |



← ⊕ →

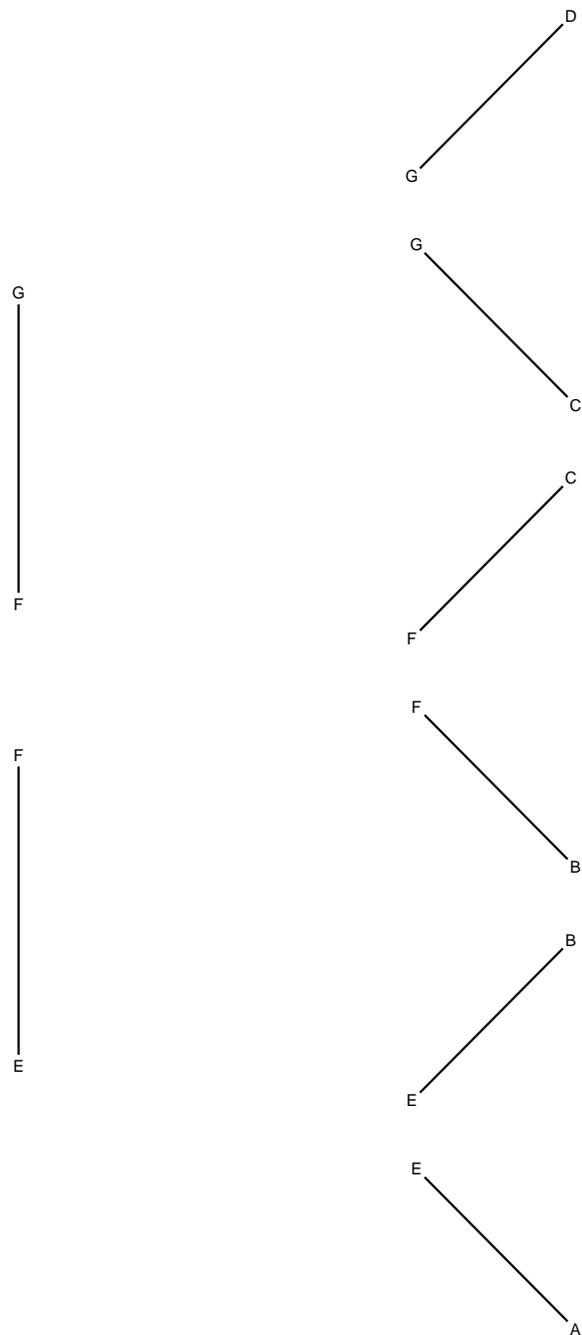


↑ ⊕ ↓



⊕ ↻

Svolgere l'analisi cinematica.
 Riportare la soluzione su questo foglio.
 Carichi e deformazioni date hanno verso efficace in disegno.
 Calcolare reazioni vincolari della struttura e delle aste.
 Tracciare i diagrammi delle azioni interne nelle aste.
 $A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.
 Allungamento termico assegnato ε su asta BC.
 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$$H_A = \quad V_A = \quad V_D =$$

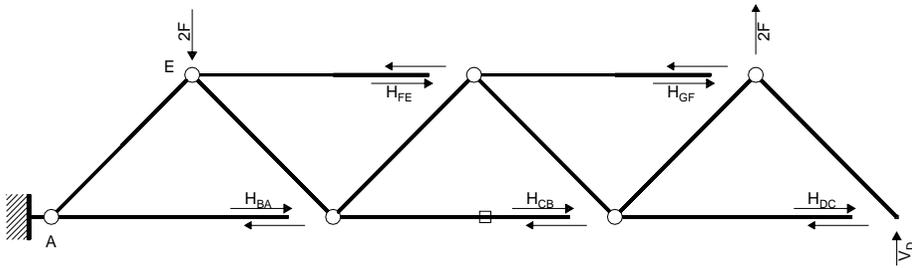
$$N_{AB} = \quad N_{BC} = \quad N_{CD} = \quad N_{EF} = \quad N_{FG} = \quad N_{AE} =$$

$$N_{EB} = \quad N_{BF} = \quad N_{FC} = \quad N_{CG} = \quad N_{GD} =$$

SPOSTAMENTI ASSOLUTI

$$u_F =$$

$$v_F =$$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -8Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -8Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -6Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = -4Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = -2Fb$$

Rotazione intorno a G: aste GD

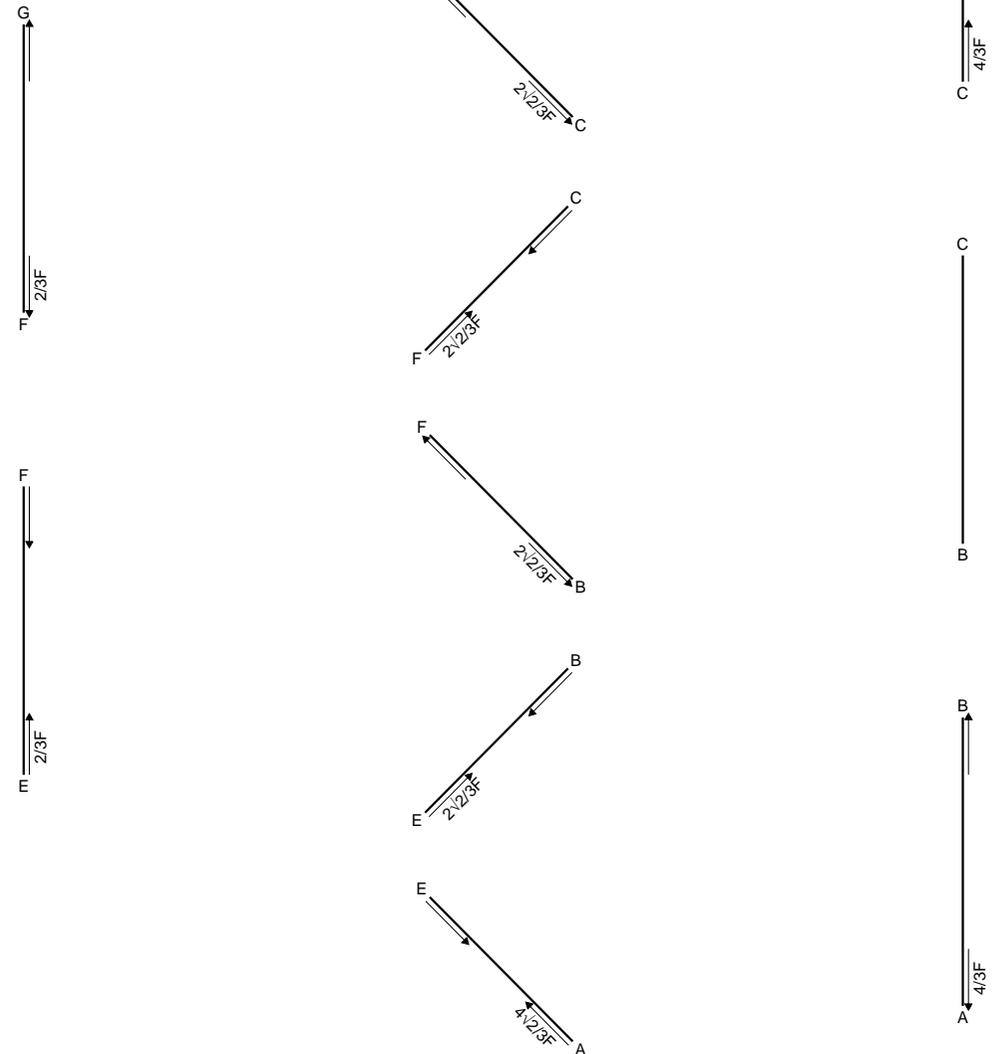
$$V_D b - H_{DC} b = 0$$

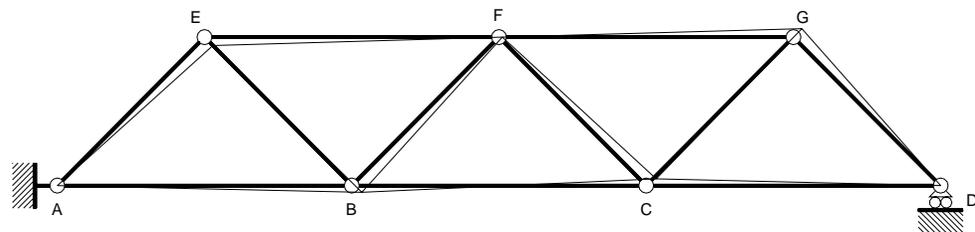
Matrice di equilibrio

$$\begin{matrix} \varphi_{AE} \\ \varphi_{EB} \\ \varphi_{BF} \\ \varphi_{FC} \\ \varphi_{CG} \\ \varphi_{GD} \end{matrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \\ 6 & 0 & 0 & 0 & 0 & 0 \\ 5 & -1 & 0 & 0 & 0 & 0 \\ 4 & 0 & 0 & 0 & 1 & 0 \\ 3 & 0 & -1 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & -1 & 0 & 0 \end{bmatrix} = \begin{bmatrix} -8 \\ -8 \\ -6 \\ -4 \\ -2 \\ 0 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -4/3 \\ 4/3 \\ -2/3 \\ 0 \\ 2/3 \\ -4/3 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$





REAZIONI

$$H_A = 0 \quad V_A = 4/3F \quad V_D = -4/3F$$

$$N_{AB} = 4/3F \quad N_{BC} = 0 \quad N_{CD} = -4/3F \quad N_{EF} = -2/3F \quad N_{FG} = 2/3F \quad N_{AE} = -4\sqrt{2}/3F$$

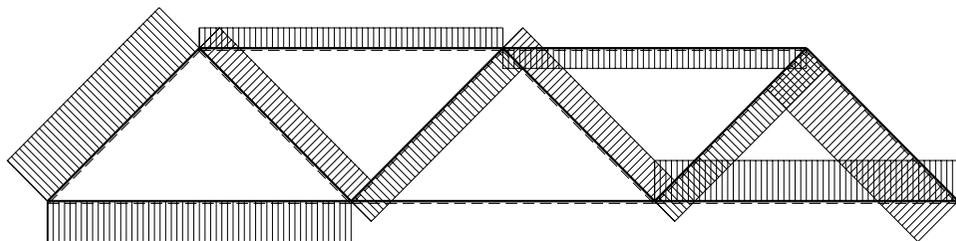
$$N_{EB} = -2\sqrt{2}/3F \quad N_{BF} = 2\sqrt{2}/3F \quad N_{FC} = -2\sqrt{2}/3F \quad N_{CG} = 2\sqrt{2}/3F \quad N_{GD} = 4\sqrt{2}/3F$$

SPOSTAMENTI ASSOLUTI

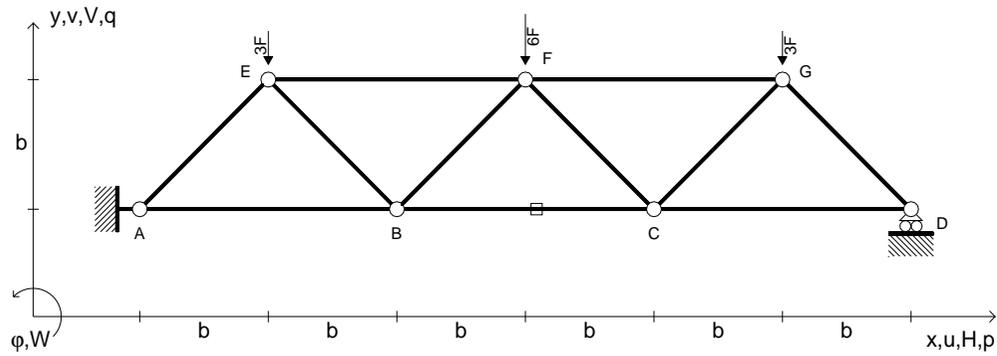
$$u_F = 26/9(Fb/EA)$$

$$v_F = -6(Fb/EA)$$

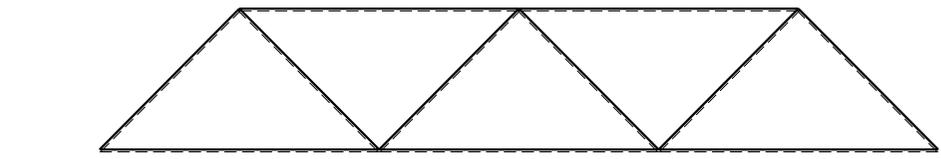
1 → 20 Fb/EA



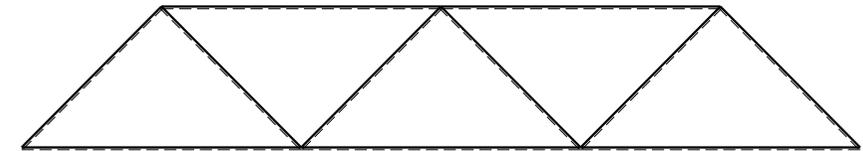
← ⊕ → 1 → 2.5 F



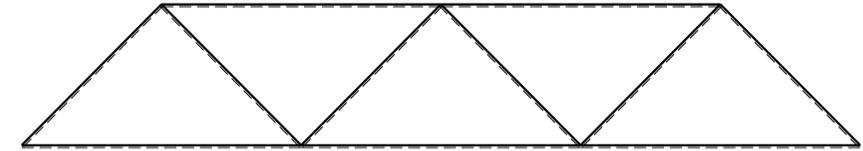
- | | | | |
|--|-----------------|----------------|----------------|
| $V_E = -3F$ | $v_F = ?$ | $EA_{FG} = EA$ | $EA_{CG} = EA$ |
| $V_F = -6F$ | $EA_{AB} = EA$ | $EA_{AE} = EA$ | $EA_{GD} = EA$ |
| $V_G = -3F$ | $EA_{BC} = 3EA$ | $EA_{EB} = EA$ | |
| $\varepsilon_{BC} = 2\alpha T = 2F/EA$ | $EA_{CD} = EA$ | $EA_{BF} = EA$ | |
| $u_F = ?$ | $EA_{EF} = EA$ | $EA_{FC} = EA$ | |



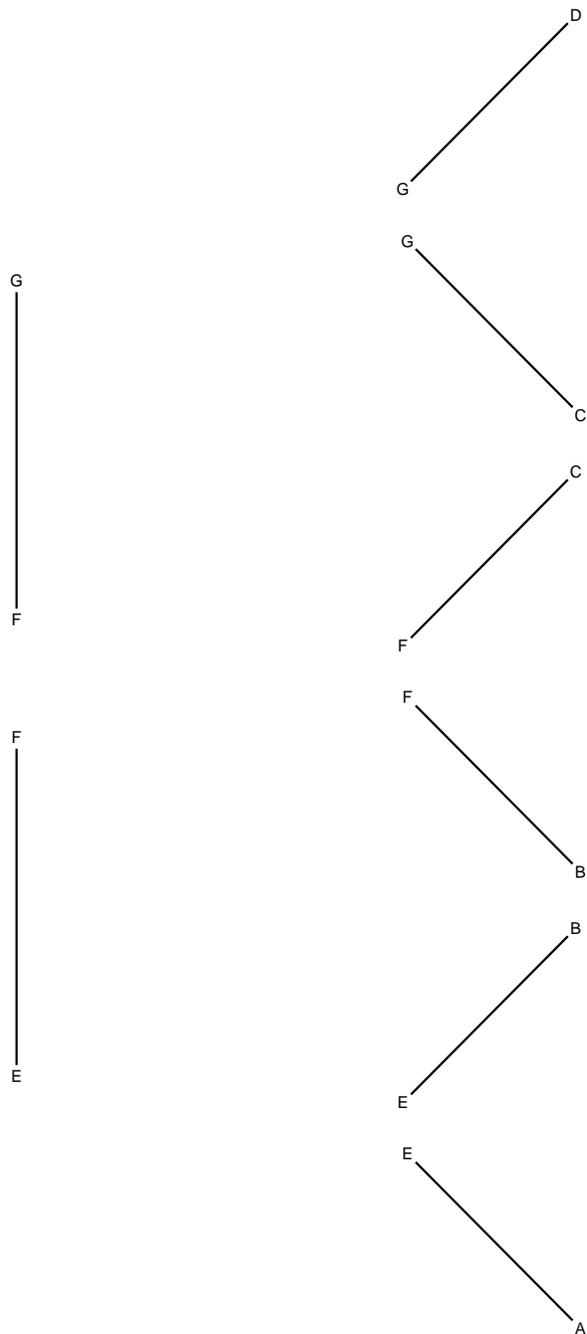
← ⊕ →



⊕ ⊖



Svolgere l'analisi cinematica.
 Riportare la soluzione su questo foglio.
 Carichi e deformazioni date hanno verso efficace in disegno.
 Calcolare reazioni vincolari della struttura e delle aste.
 Tracciare i diagrammi delle azioni interne nelle aste.
 $A_{vz} - x_{vz} - \theta_{vz}$ riferimento locale asta YZ con origine in Y.
 Allungamento termico assegnato ε su asta BC.
 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $V_D =$

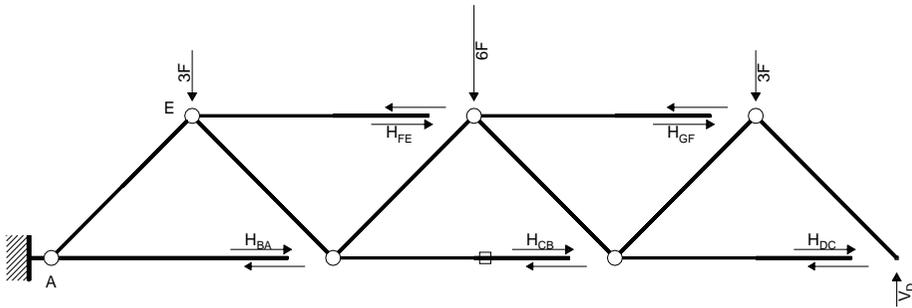
$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 36Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 24Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 15Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 6Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 3Fb$$

Rotazione intorno a G: aste GD

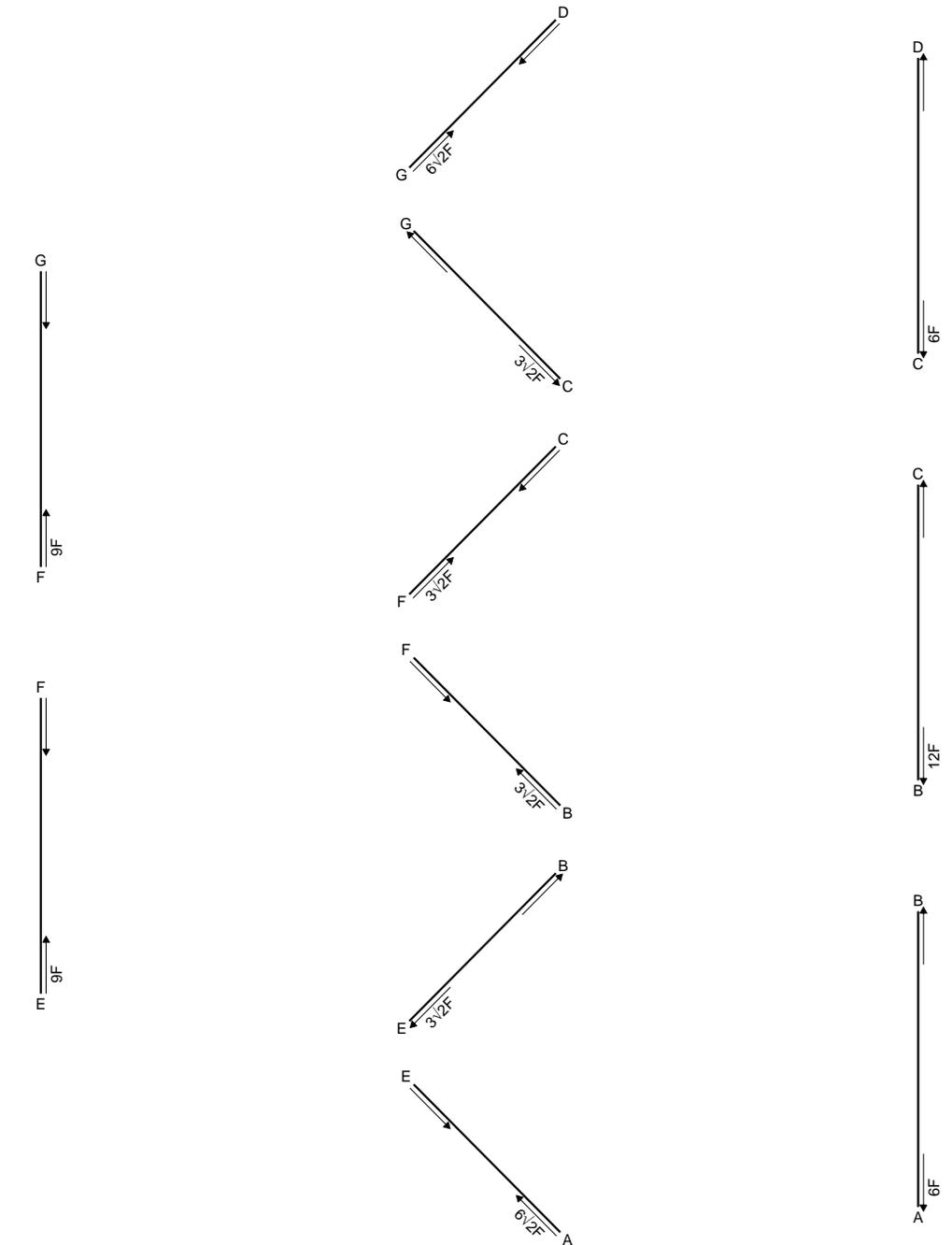
$$V_D b - H_{DC} b = 0$$

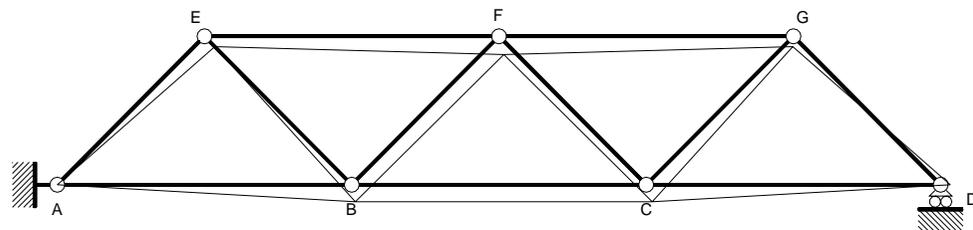
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 36 \\ 24 \\ 15 \\ 6 \\ 3 \\ 0 \end{bmatrix} Fb$$

Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 6 \\ 6 \\ -9 \\ 12 \\ -9 \\ 6 \end{bmatrix} Fb$$





REAZIONI

$$H_A = 0 \quad V_A = 6F \quad V_D = 6F$$

$$N_{AB} = 6F \quad N_{BC} = 12F \quad N_{CD} = 6F \quad N_{EF} = -9F \quad N_{FG} = -9F \quad N_{AE} = -6\sqrt{2}F$$

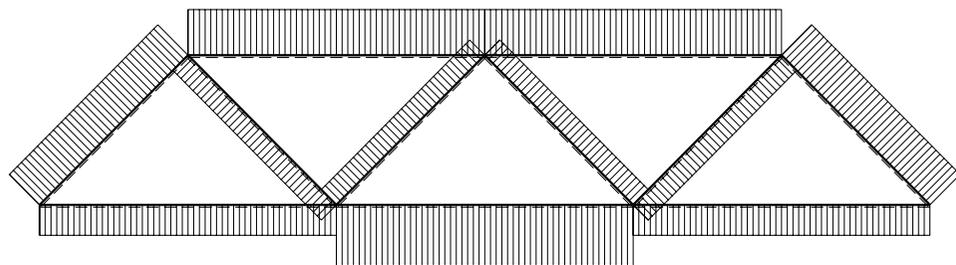
$$N_{EB} = 3\sqrt{2}F \quad N_{BF} = -3\sqrt{2}F \quad N_{FC} = -3\sqrt{2}F \quad N_{CG} = 3\sqrt{2}F \quad N_{GD} = -6\sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

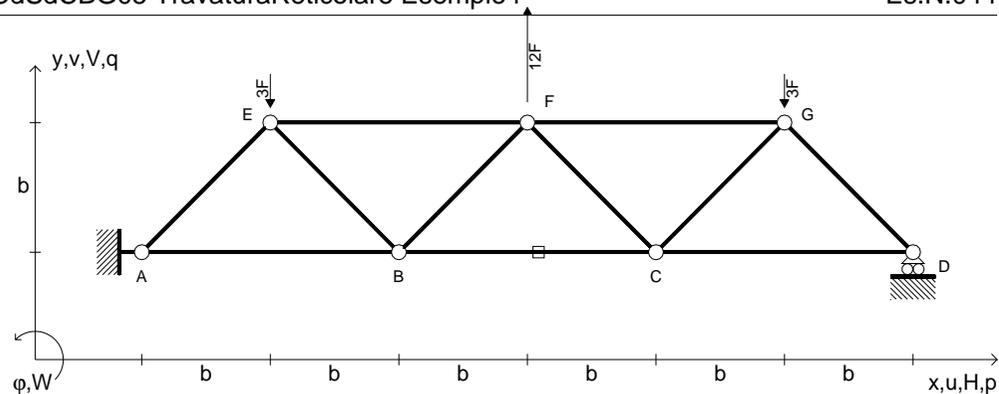
$$u_F = 18(Fb/EA)$$

$$v_F = -(66+24\sqrt{2})(Fb/EA)$$

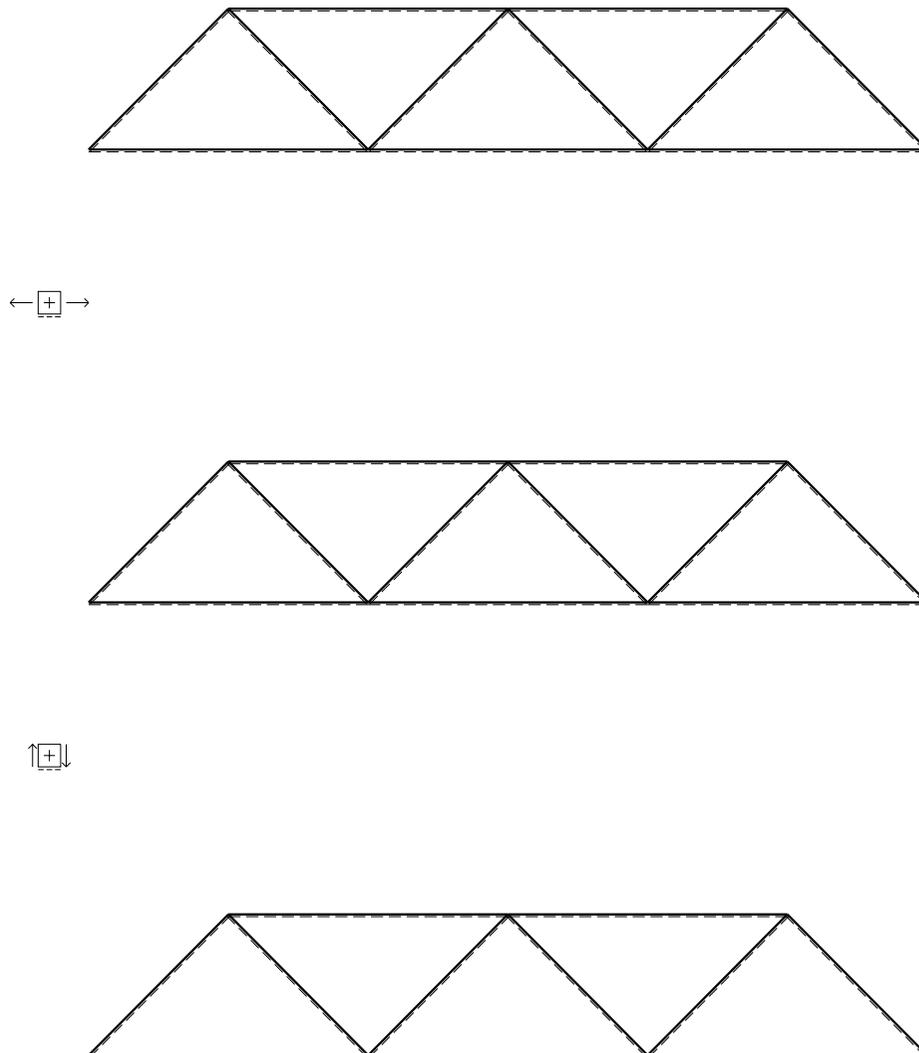
1 250 Fb/EA



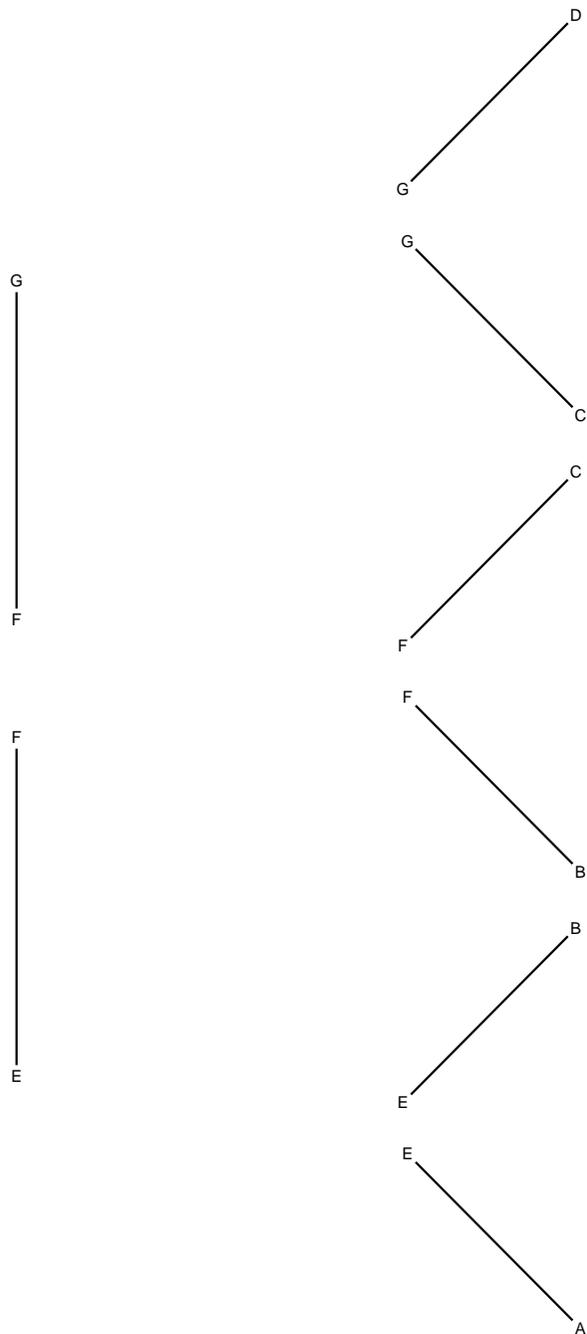
← ⊕ → 15 F



- | | | | |
|--|-----------------|----------------|----------------|
| $V_E = -3F$ | $V_F = ?$ | $EA_{FG} = EA$ | $EA_{CG} = EA$ |
| $V_F = 12F$ | $EA_{AB} = EA$ | $EA_{AE} = EA$ | $EA_{GD} = EA$ |
| $V_G = -3F$ | $EA_{BC} = 4EA$ | $EA_{EB} = EA$ | |
| $\varepsilon_{BC} = 2\alpha T = 2F/EA$ | $EA_{CD} = EA$ | $EA_{BF} = EA$ | |
| $u_F = ?$ | $EA_{EF} = EA$ | $EA_{FC} = EA$ | |



Svolgere l'analisi cinematica.
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 Allungamento termico assegnato ε su asta BC.
 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $V_D =$

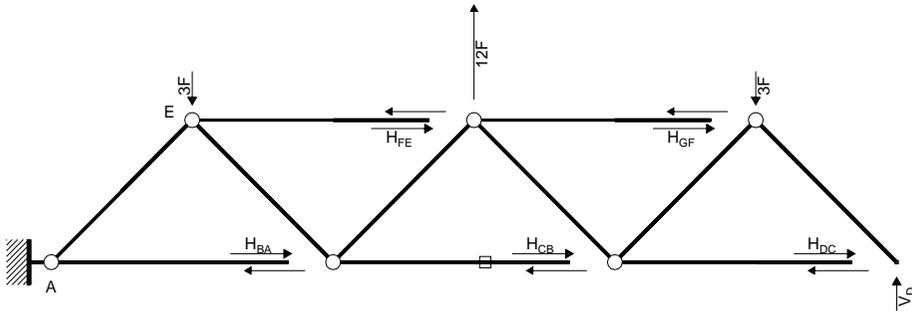
$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -18Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -12Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -3Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 6Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 3Fb$$

Rotazione intorno a G: aste GD

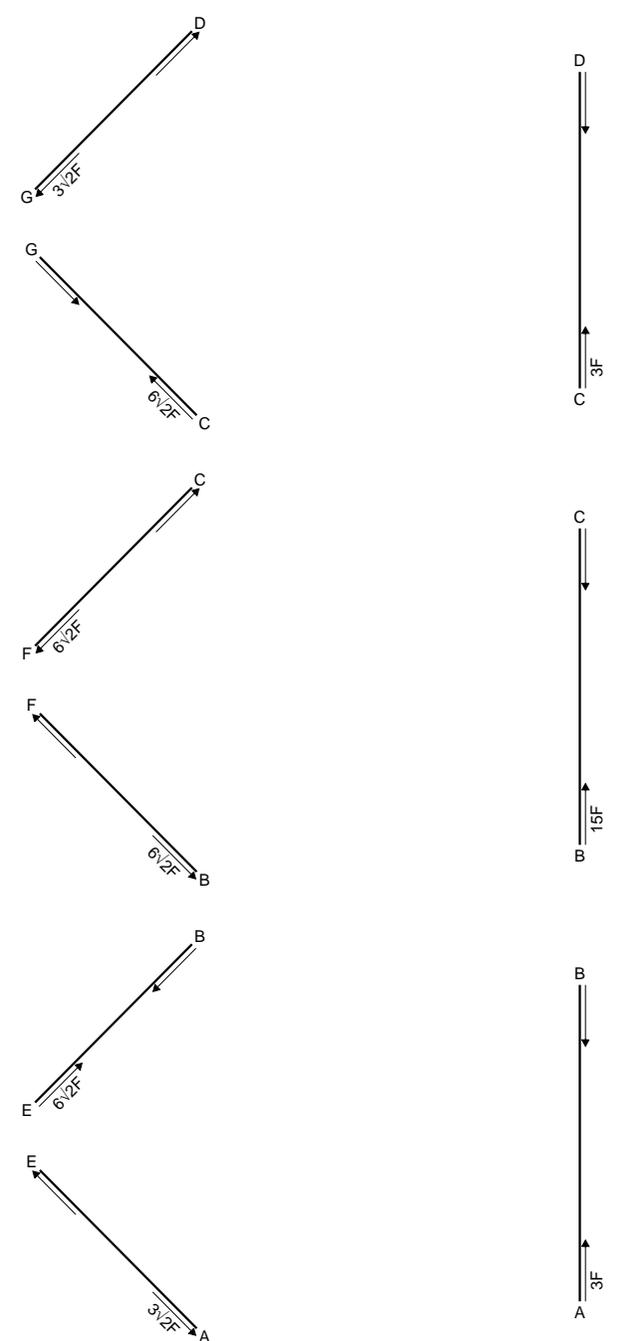
$$V_D b - H_{DC} b = 0$$

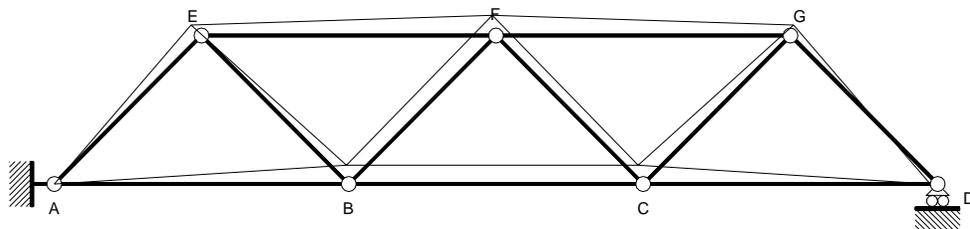
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} -18 \\ -12 \\ -3 \\ 6 \\ 3 \\ 0 \end{bmatrix} Fb$$

Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -3 \\ -3 \\ 9 \\ -15 \\ 9 \\ -3 \end{bmatrix} Fb$$





REAZIONI

$$H_A = 0 \quad V_A = -3F \quad V_D = -3F$$

$$N_{AB} = -3F \quad N_{BC} = -15F \quad N_{CD} = -3F \quad N_{EF} = 9F \quad N_{FG} = 9F \quad N_{AE} = 3\sqrt{2}F$$

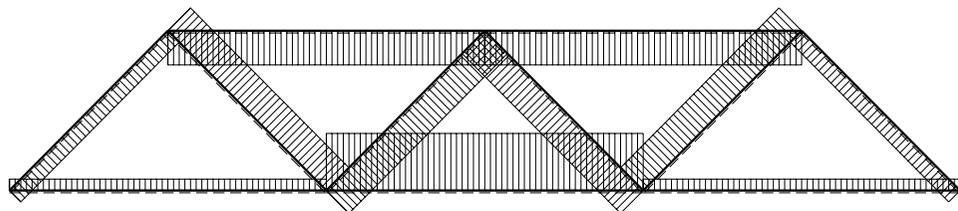
$$N_{EB} = -6\sqrt{2}F \quad N_{BF} = 6\sqrt{2}F \quad N_{FC} = 6\sqrt{2}F \quad N_{CG} = -6\sqrt{2}F \quad N_{GD} = 3\sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

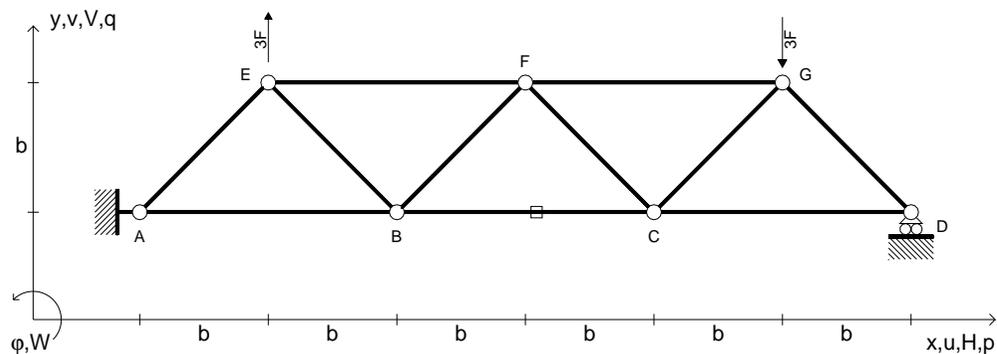
$$u_F = -31/4(Fb/EA)$$

$$v_F = (189+120\sqrt{2})/4(Fb/EA)$$

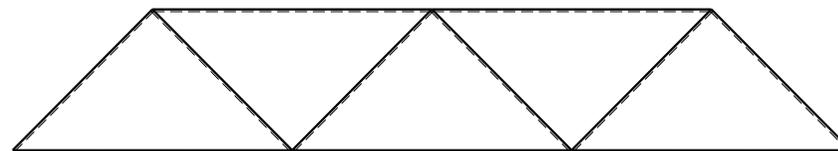
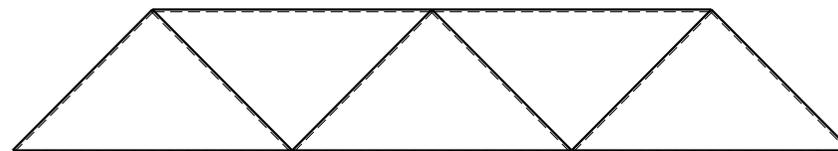
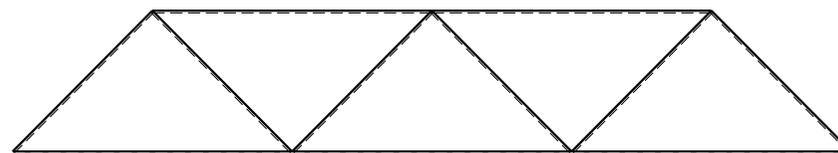
1 200 Fb/EA



← ⊕ → 1 20 F

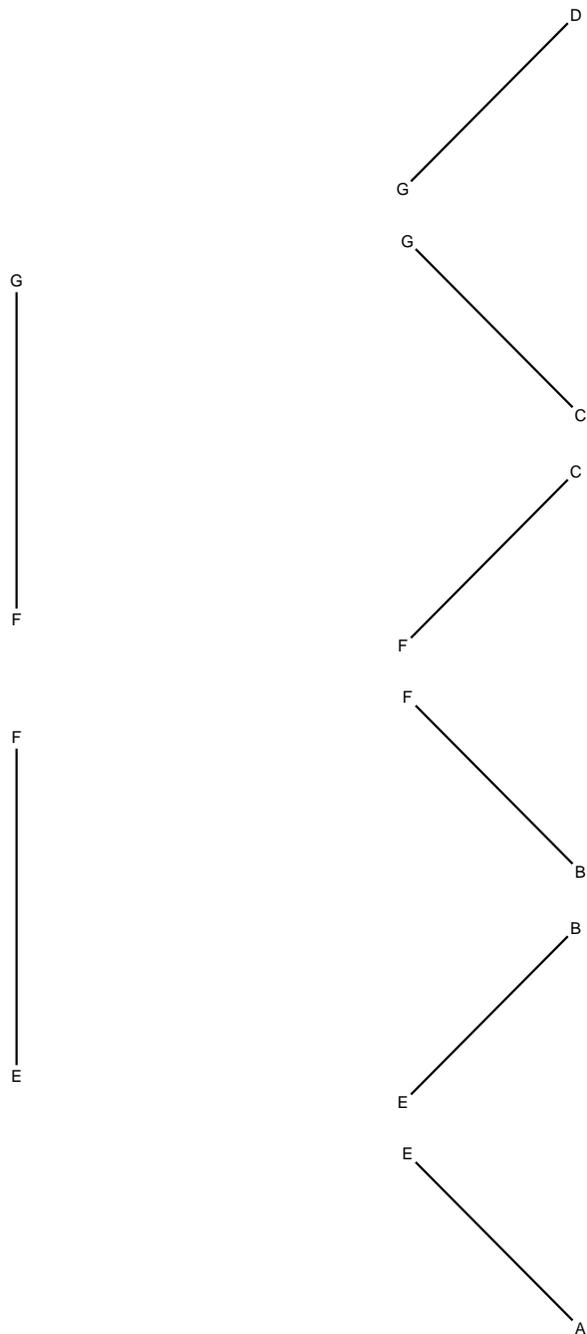


$V_E = 3F$	$v_F = ?$	$EA_{EF} = EA$	$EA_{BF} = EA$
$V_G = -3F$	$EA_{AB} = EA$	$EA_{FG} = EA$	$EA_{FC} = EA$
$\varepsilon_{BC} = 2\alpha T = 2F/EA$	$EA_{BC} = 1/4EA$	$EA_{AE} = EA$	$EA_{CG} = EA$
$u_F = ?$	$EA_{CD} = EA$	$EA_{EB} = EA$	$EA_{GD} = EA$



Svolgere l'analisi cinematica.
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 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_A =$ $V_A =$ $V_D =$

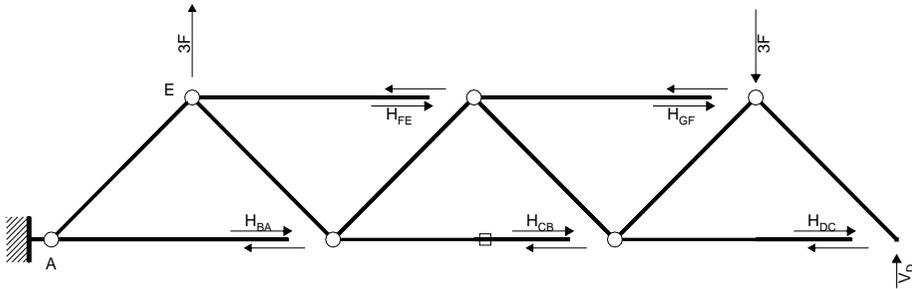
$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 12Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 12Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 9Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 6Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 3Fb$$

Rotazione intorno a G: aste GD

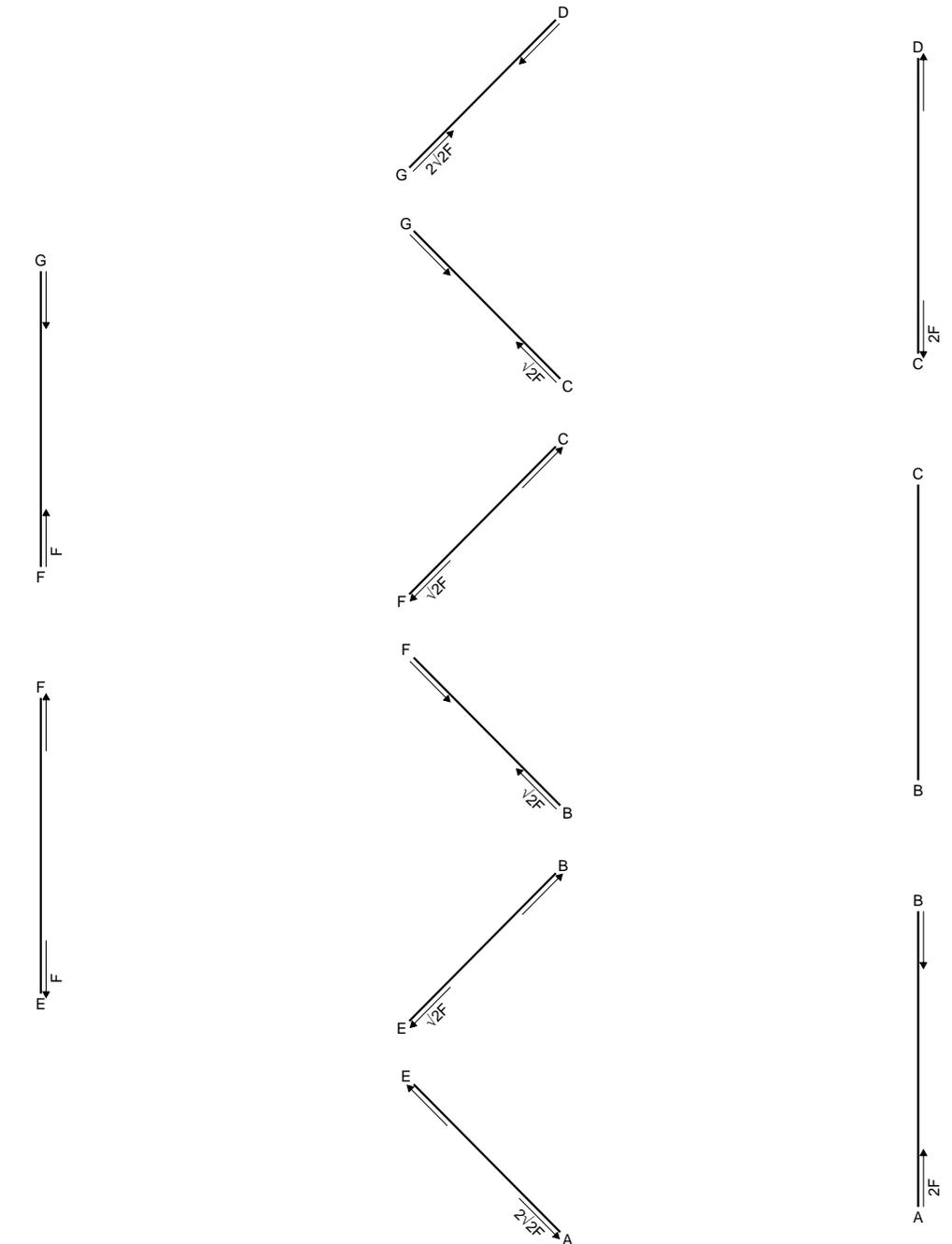
$$V_D b - H_{DC} b = 0$$

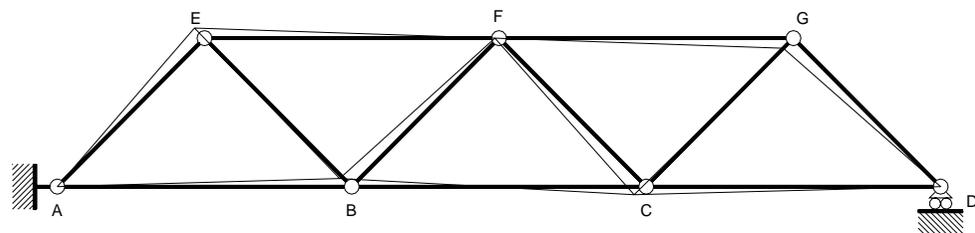
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} Fb \\ 12 \\ 9 \\ 6 \\ 3 \\ 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 2 \\ -2 \\ 1 \\ 0 \\ -1 \\ 2 \end{bmatrix}$$





REAZIONI

$$H_A = 0 \quad V_A = -2F \quad V_D = 2F$$

$$N_{AB} = -2F \quad N_{BC} = 0 \quad N_{CD} = 2F \quad N_{EF} = F \quad N_{FG} = -F \quad N_{AE} = 2\sqrt{2}F$$

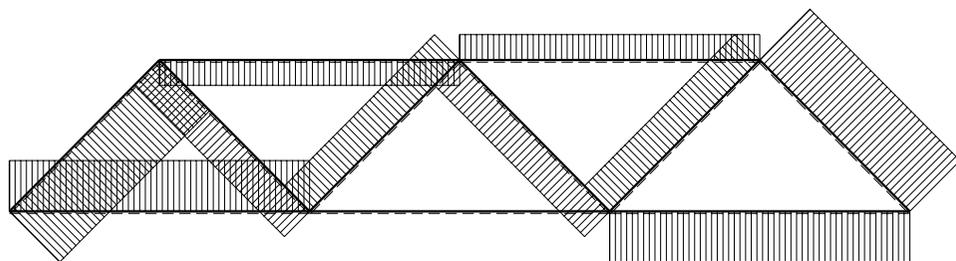
$$N_{EB} = \sqrt{2}F \quad N_{BF} = -\sqrt{2}F \quad N_{FC} = \sqrt{2}F \quad N_{CG} = -\sqrt{2}F \quad N_{GD} = -2\sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

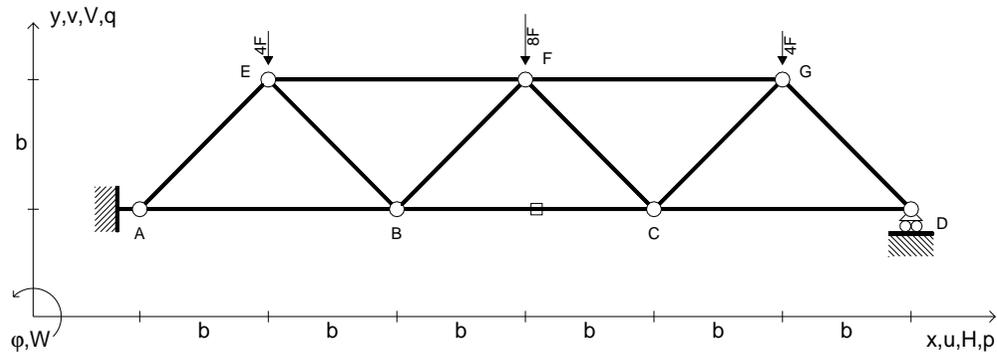
$$u_F = 2/3(Fb/EA)$$

$$v_F = -6(Fb/EA)$$

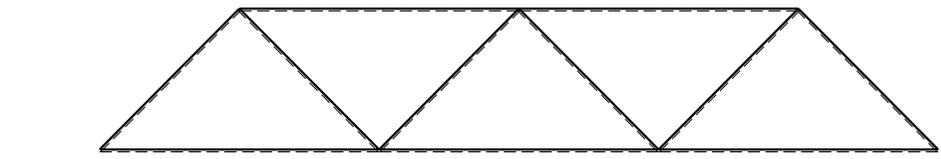
1 — 25 Fb/EA



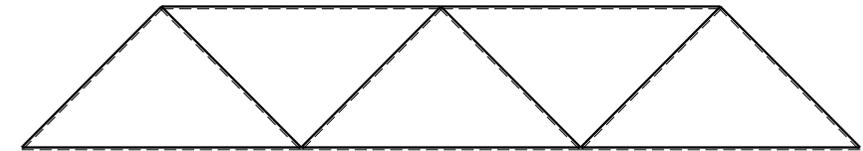
← ⊕ → 1 — 3 F



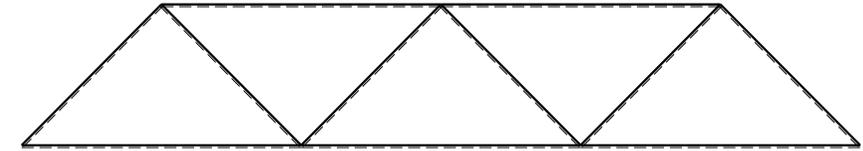
- | | | | |
|--|-------------------|----------------|----------------|
| $V_E = -4F$ | $v_F = ?$ | $EA_{FG} = EA$ | $EA_{CG} = EA$ |
| $V_F = -8F$ | $EA_{AB} = EA$ | $EA_{AE} = EA$ | $EA_{GD} = EA$ |
| $V_G = -4F$ | $EA_{BC} = 1/3EA$ | $EA_{EB} = EA$ | |
| $\varepsilon_{BC} = 2\alpha T = 2F/EA$ | $EA_{CD} = EA$ | $EA_{BF} = EA$ | |
| $u_F = ?$ | $EA_{EF} = EA$ | $EA_{FC} = EA$ | |



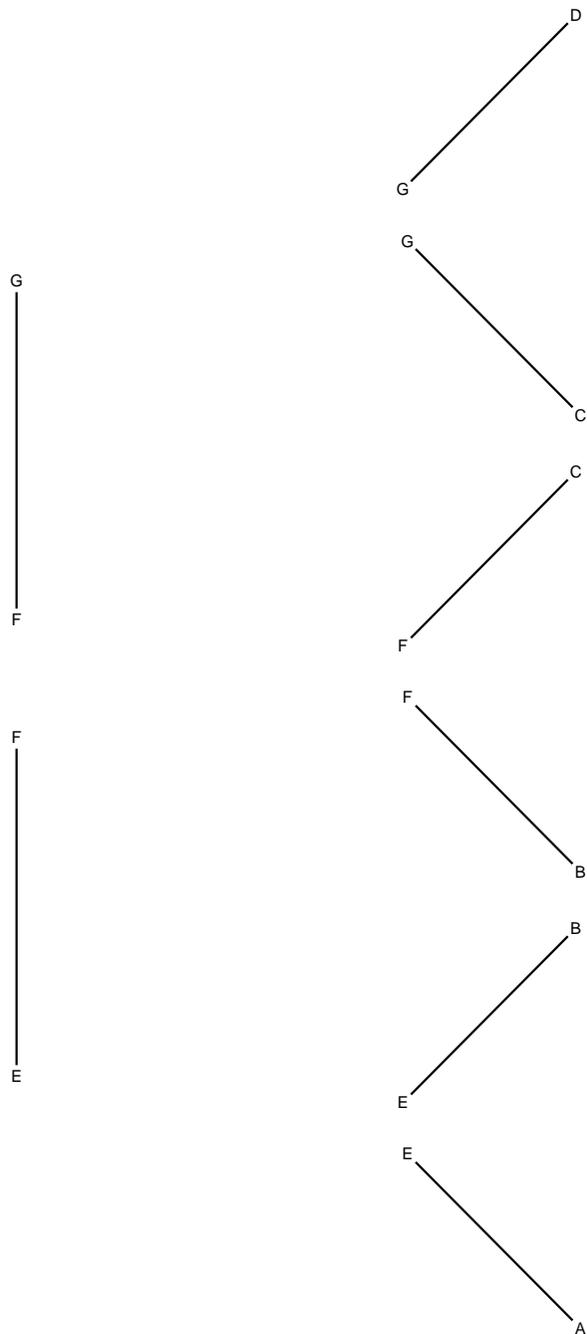
← ⊕ →



↑ ⊕ ↓



Svolgere l'analisi cinematica.
 Riportare la soluzione su questo foglio.
 Carichi e deformazioni date hanno verso efficace in disegno.
 Calcolare reazioni vincolari della struttura e delle aste.
 Tracciare i diagrammi delle azioni interne nelle aste.
 $A_{yZ} - x_{yZ} - \theta_{yZ}$ riferimento locale asta YZ con origine in Y.
 Allungamento termico assegnato ε su asta BC.
 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $V_D =$

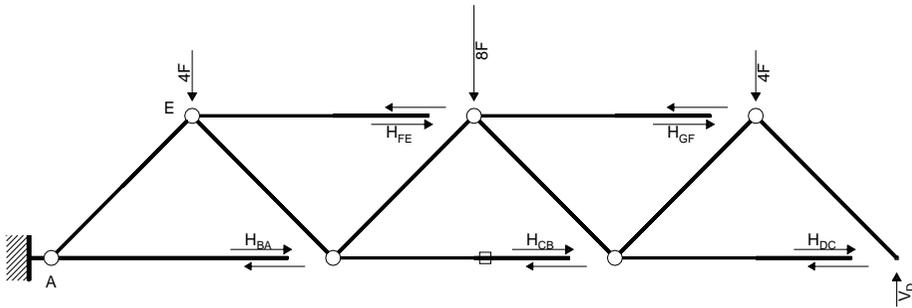
$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 48Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 32Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 20Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 8Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 4Fb$$

Rotazione intorno a G: aste GD

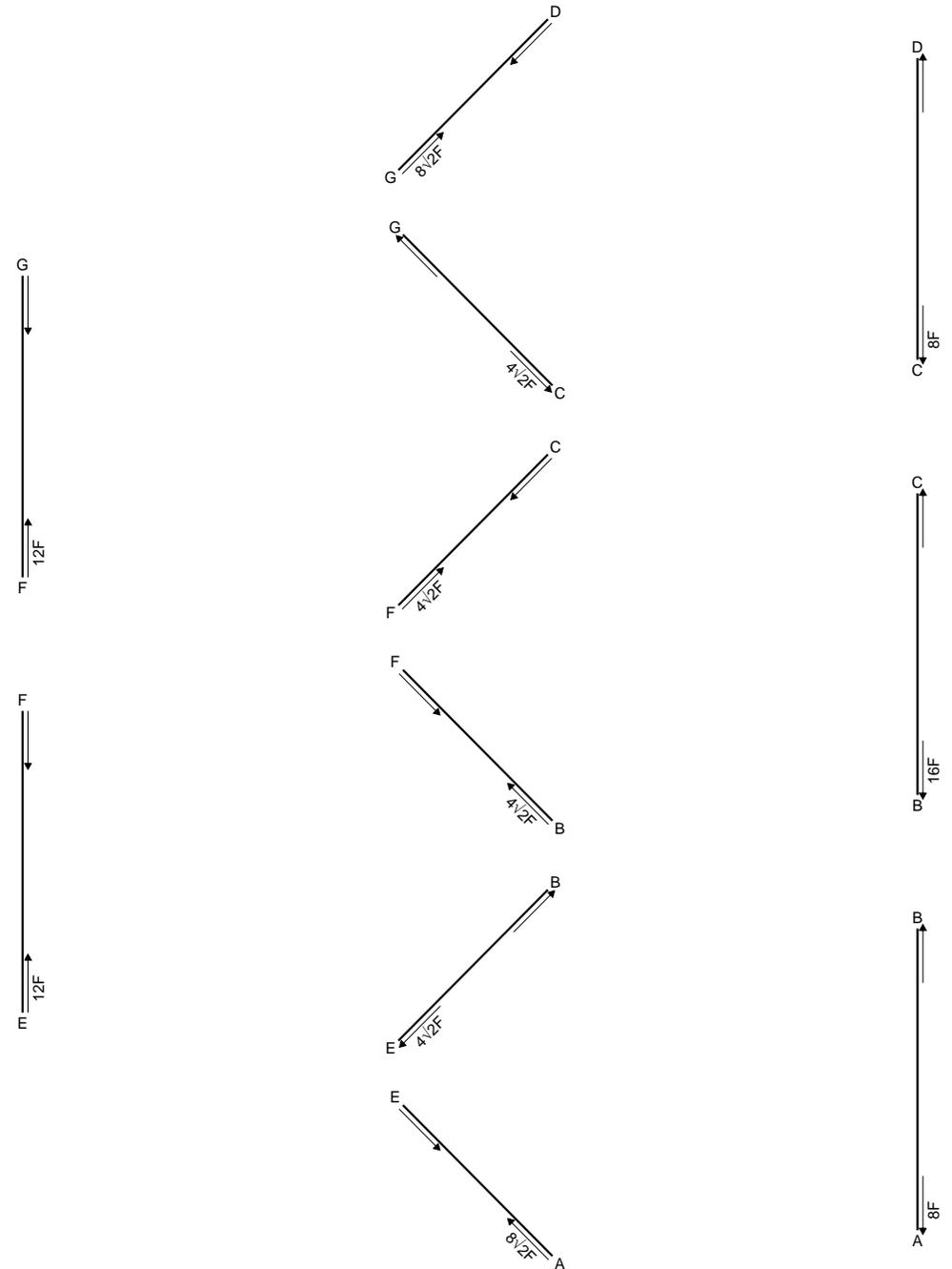
$$V_D b - H_{DC} b = 0$$

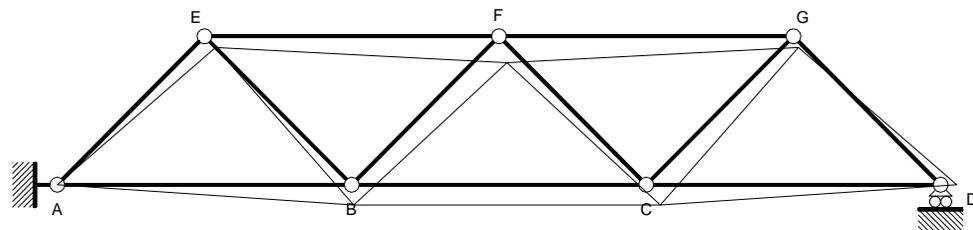
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 48 \\ 32 \\ 20 \\ 8 \\ 4 \\ 0 \end{bmatrix} Fb$$

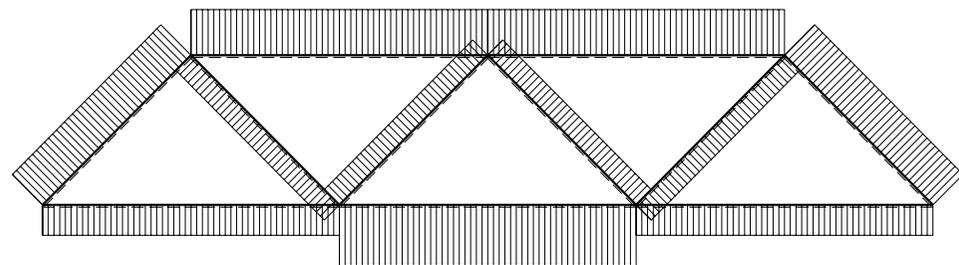
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 8 \\ 8 \\ -12 \\ 16 \\ -12 \\ 8 \end{bmatrix} Fb$$





← 600 Fb/EA



← ⊕ → | 20 F

REAZIONI

$$H_A = 0 \quad V_A = 8F \quad V_D = 8F$$

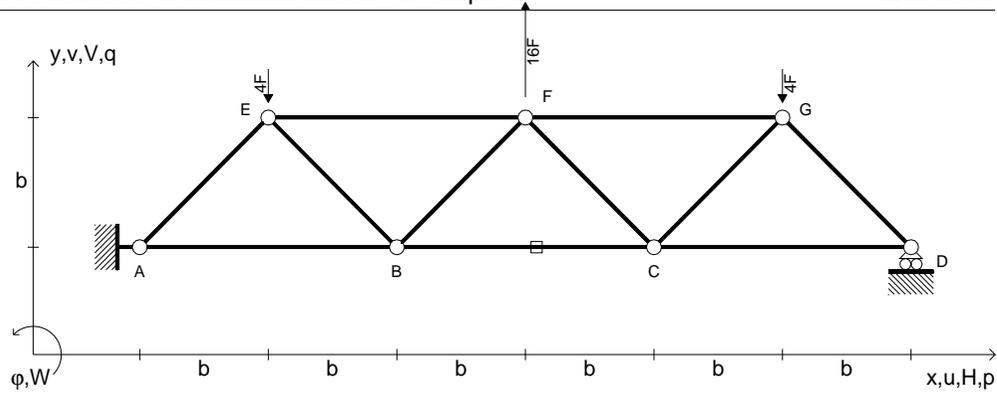
$$N_{AB} = 8F \quad N_{BC} = 16F \quad N_{CD} = 8F \quad N_{EF} = -12F \quad N_{FG} = -12F \quad N_{AE} = -8\sqrt{2}F$$

$$N_{EB} = 4\sqrt{2}F \quad N_{BF} = -4\sqrt{2}F \quad N_{FC} = -4\sqrt{2}F \quad N_{CG} = 4\sqrt{2}F \quad N_{GD} = -8\sqrt{2}F$$

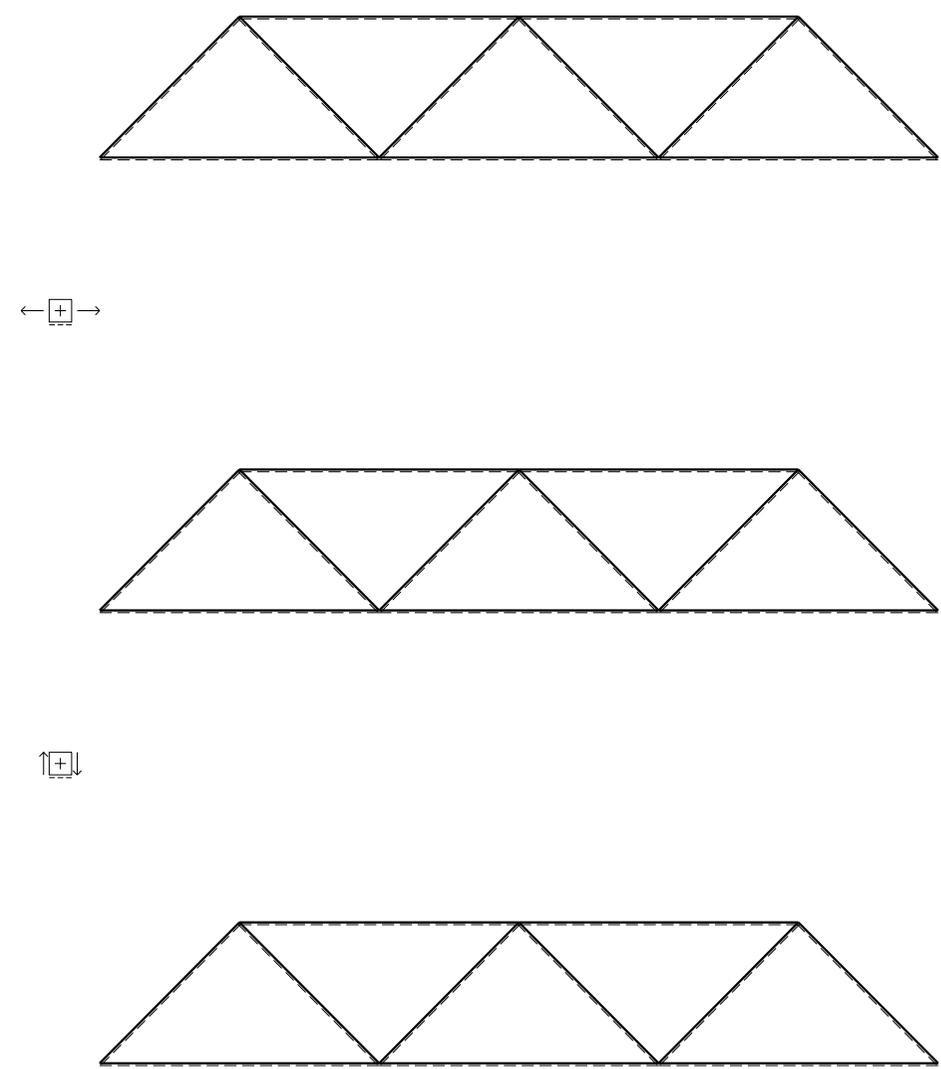
SPOSTAMENTI ASSOLUTI

$$u_F = 66(Fb/EA)$$

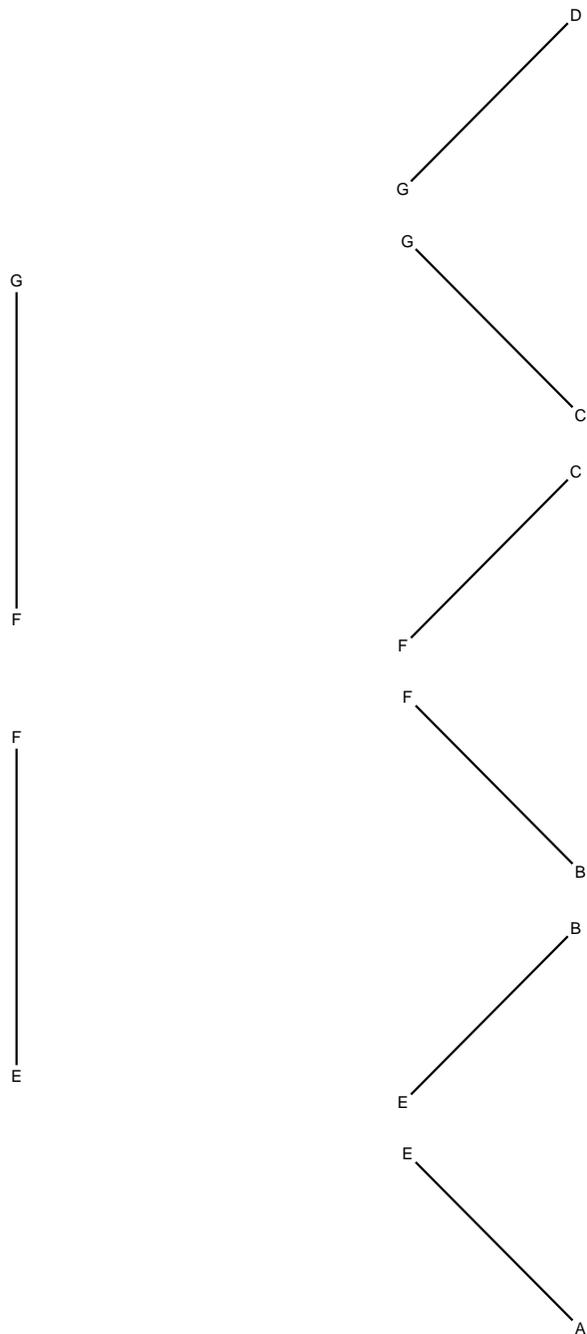
$$v_F = -(214+32\sqrt{2})(Fb/EA)$$



$V_E = -4F$	$v_F = ?$	$EA_{FG} = EA$	$EA_{CG} = EA$
$V_F = 16F$	$EA_{AB} = EA$	$EA_{AE} = EA$	$EA_{GD} = EA$
$V_G = -4F$	$EA_{BC} = 1/2EA$	$EA_{EB} = EA$	
$\varepsilon_{BC} = 2\alpha T = 2F/EA$	$EA_{CD} = EA$	$EA_{BF} = EA$	
$u_F = ?$	$EA_{EF} = EA$	$EA_{FC} = EA$	



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 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $V_D =$

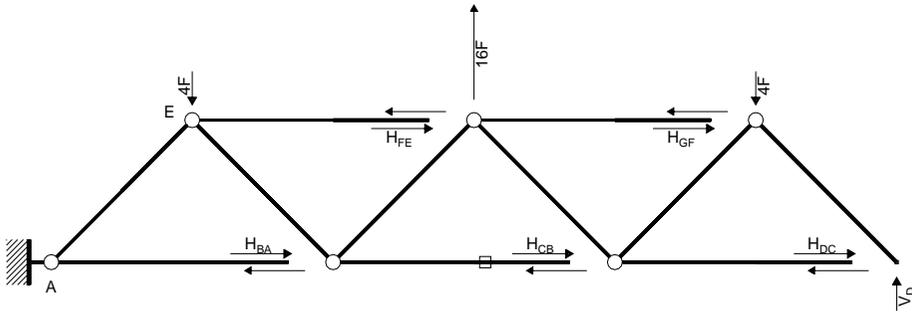
$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -24Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -16Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -4Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 8Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 4Fb$$

Rotazione intorno a G: aste GD

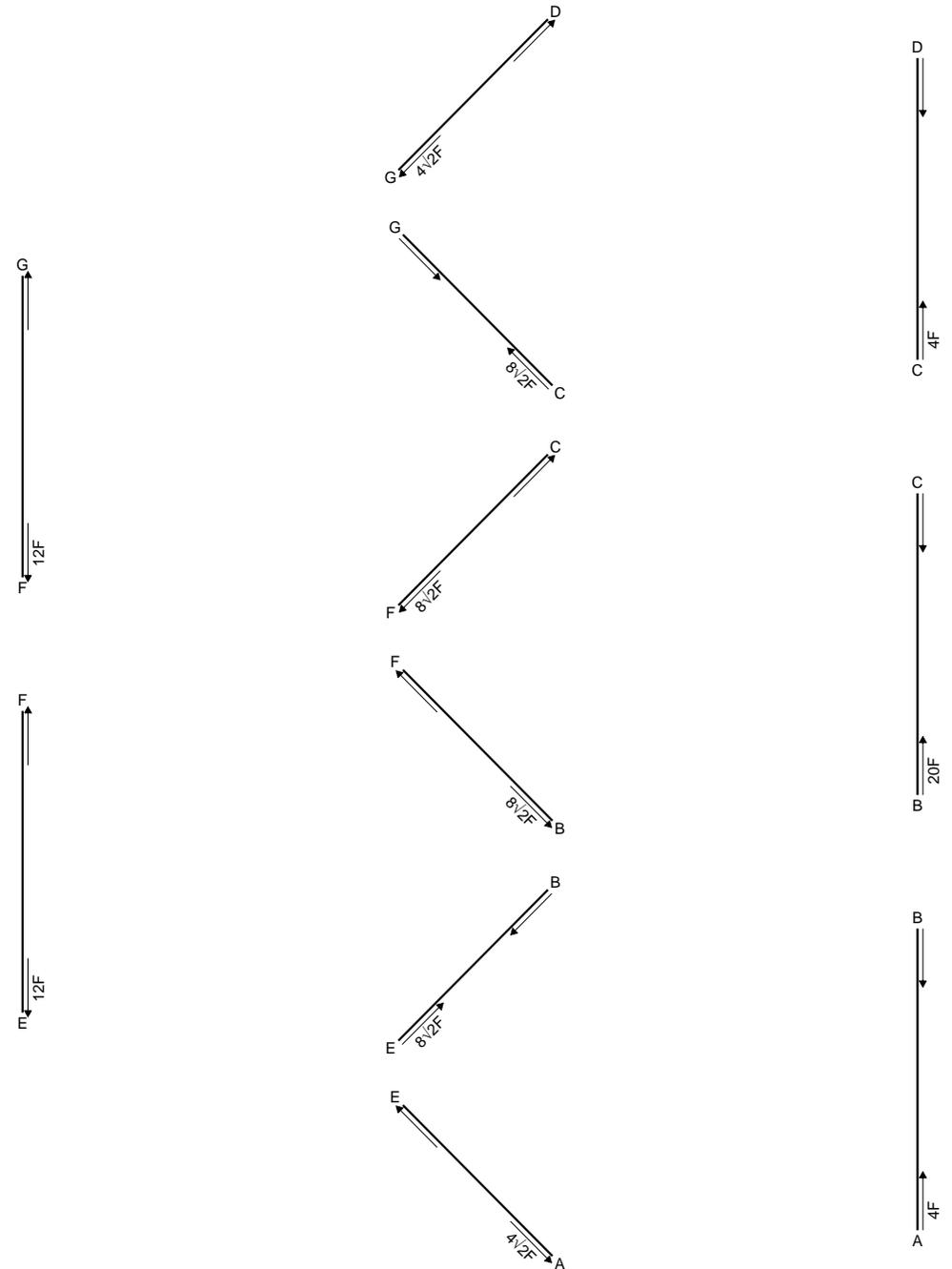
$$V_D b - H_{DC} b = 0$$

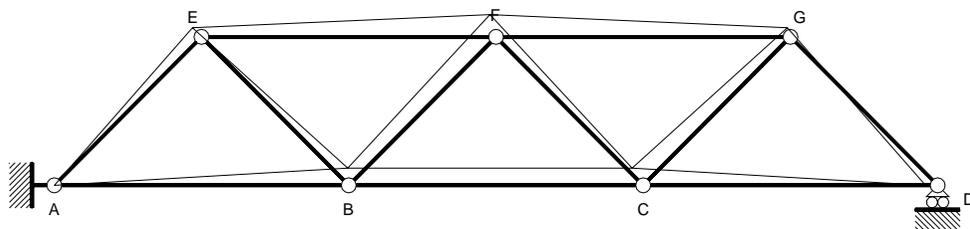
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} -24 \\ -16 \\ -4 \\ 8 \\ 4 \\ 0 \end{bmatrix} Fb$$

Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -4 \\ -4 \\ 12 \\ -20 \\ 12 \\ -4 \end{bmatrix} Fb$$





REAZIONI

$$H_A = 0 \quad V_A = -4F \quad V_D = -4F$$

$$N_{AB} = -4F \quad N_{BC} = -20F \quad N_{CD} = -4F \quad N_{EF} = 12F \quad N_{FG} = 12F \quad N_{AE} = 4\sqrt{2}F$$

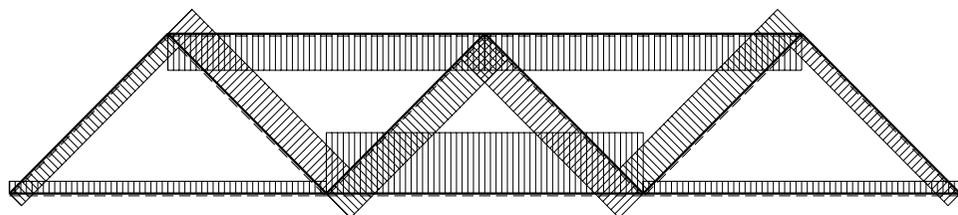
$$N_{EB} = -8\sqrt{2}F \quad N_{BF} = 8\sqrt{2}F \quad N_{FC} = 8\sqrt{2}F \quad N_{CG} = -8\sqrt{2}F \quad N_{GD} = 4\sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

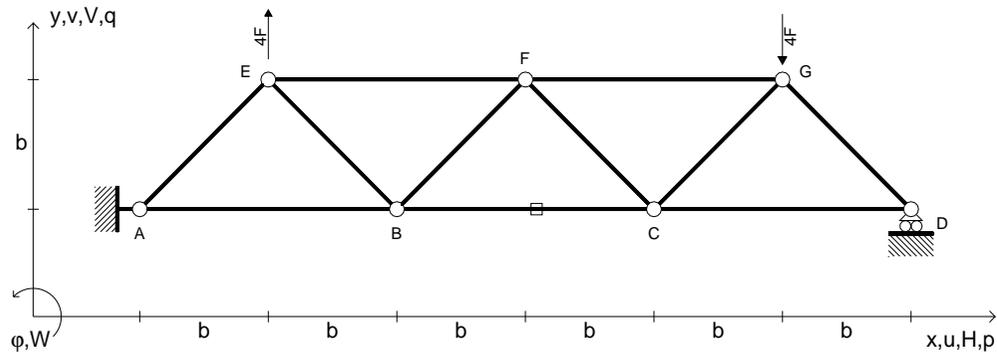
$$u_F = -46(Fb/EA)$$

$$v_F = (170+40\sqrt{2})(Fb/EA)$$

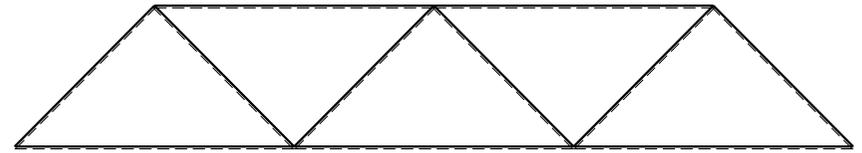
← 600 Fb/EA



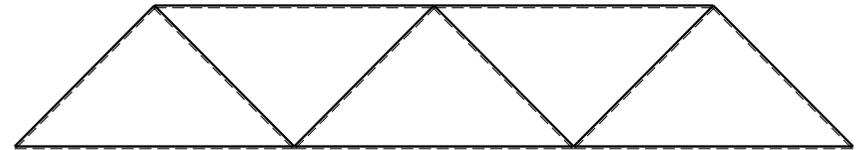
← ⊕ → ← 25 F



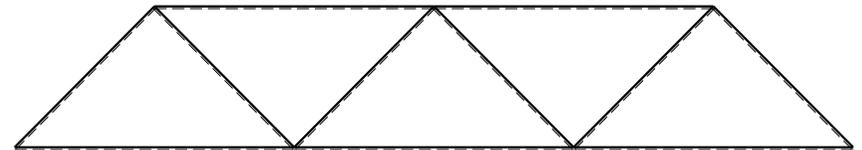
- | | | | |
|--|-------------------|----------------|----------------|
| $V_E = 4F$ | $v_F = ?$ | $EA_{EF} = EA$ | $EA_{BF} = EA$ |
| $V_G = -4F$ | $EA_{AB} = EA$ | $EA_{FG} = EA$ | $EA_{FC} = EA$ |
| $\varepsilon_{BC} = 2\alpha T = 2F/EA$ | $EA_{BC} = 2/3EA$ | $EA_{AE} = EA$ | $EA_{CG} = EA$ |
| $u_F = ?$ | $EA_{CD} = EA$ | $EA_{EB} = EA$ | $EA_{GD} = EA$ |



← ⊕ →

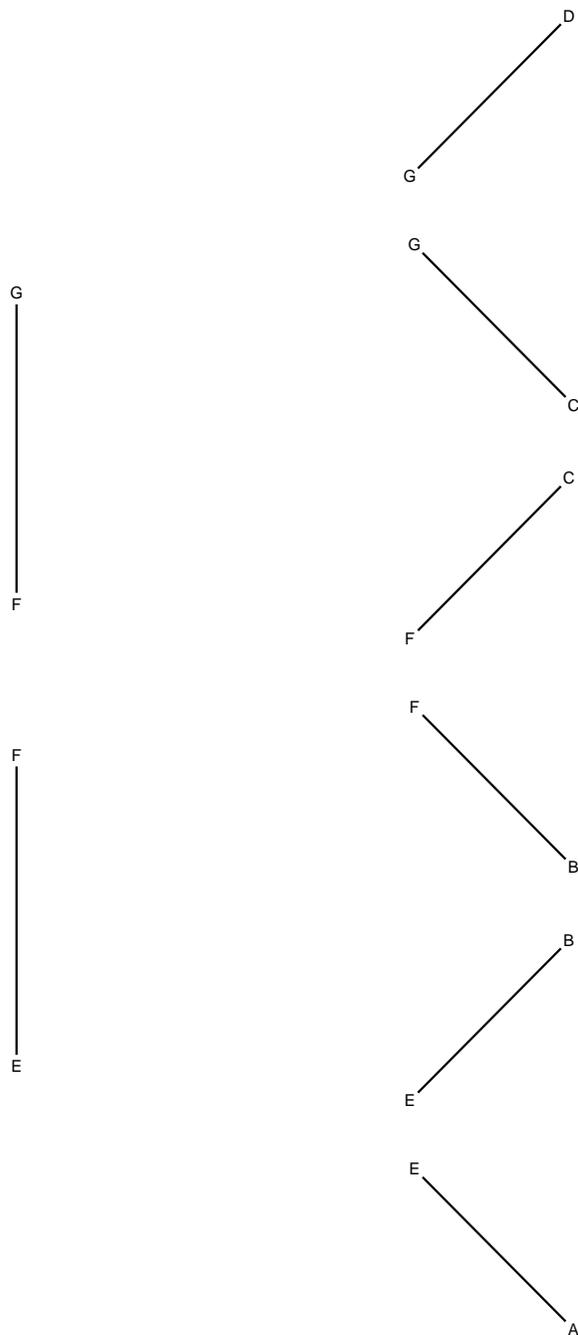


↑ ⊕ ↓



Svolgere l'analisi cinematica.
 Riportare la soluzione su questo foglio.
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 $A_{vz} - x_{vz} - \theta_{vz}$ riferimento locale asta YZ con origine in Y.
 Allungamento termico assegnato ε su asta BC.
 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano

⊕



REAZIONI

$$H_A = \quad V_A = \quad V_D =$$

$$N_{AB} = \quad N_{BC} = \quad N_{CD} = \quad N_{EF} = \quad N_{FG} = \quad N_{AE} =$$

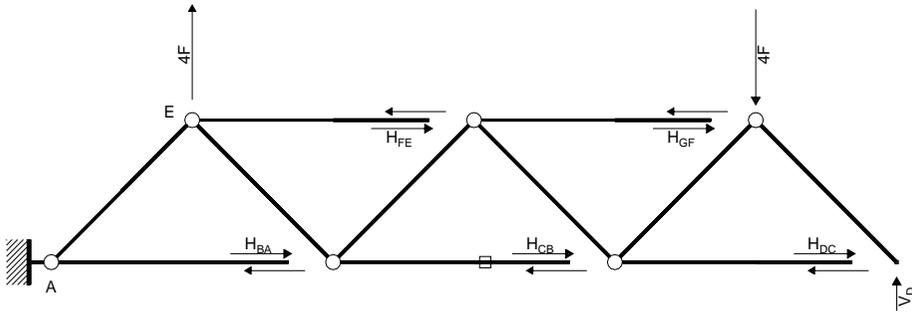
$$N_{EB} = \quad N_{BF} = \quad N_{FC} = \quad N_{CG} = \quad N_{GD} =$$

SPOSTAMENTI ASSOLUTI

$$u_F =$$

$$v_F =$$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 16Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 16Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 12Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 8Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 4Fb$$

Rotazione intorno a G: aste GD

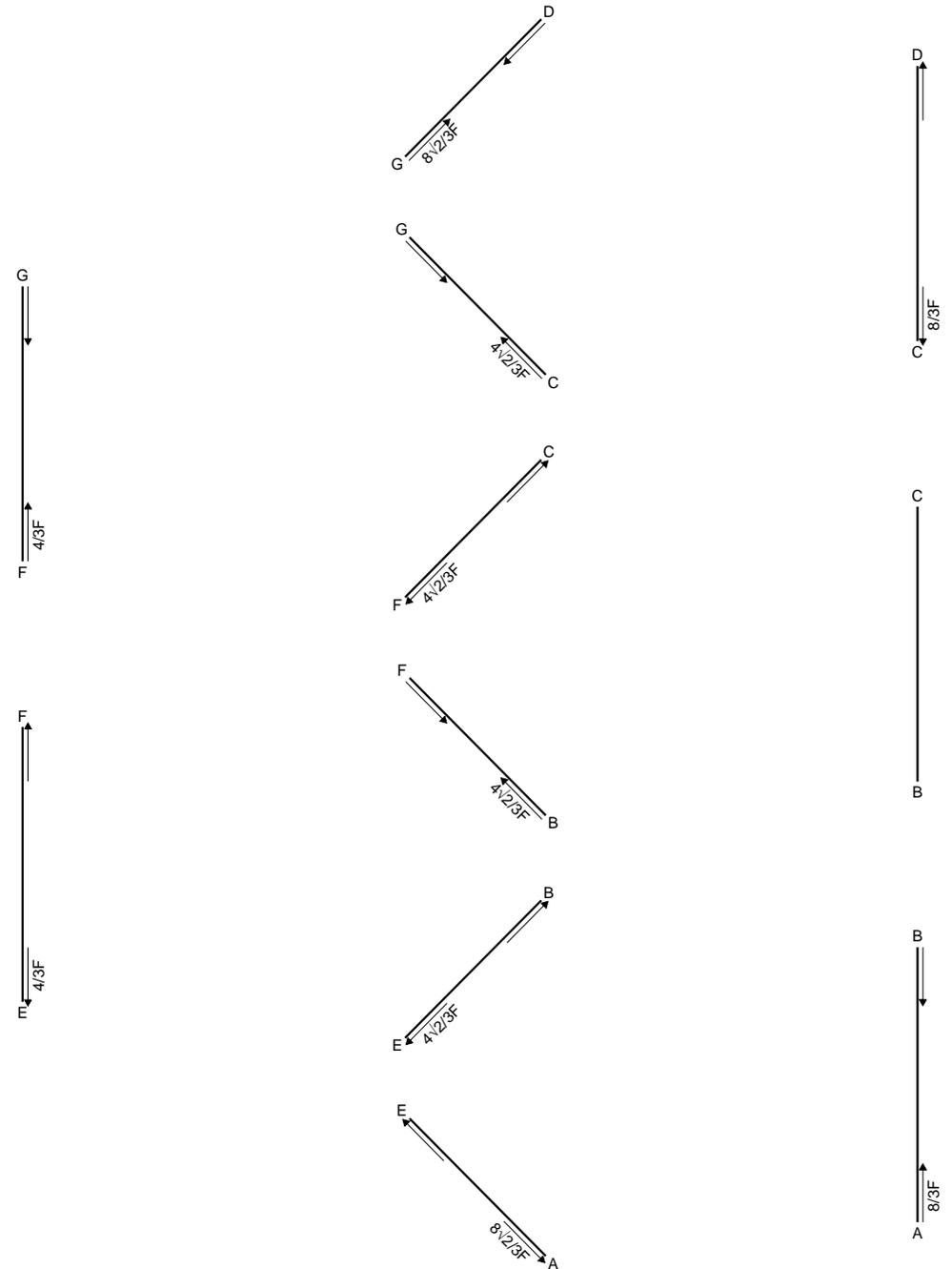
$$V_D b - H_{DC} b = 0$$

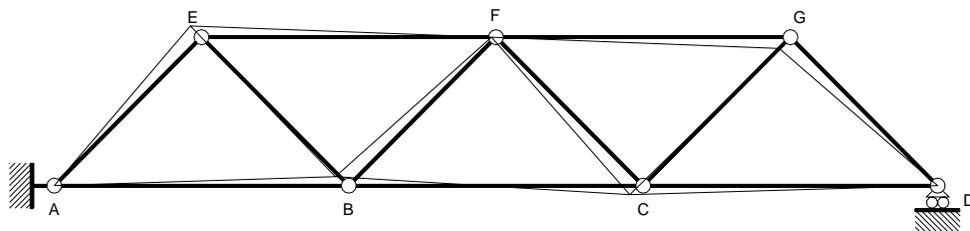
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 16 \\ 16 \\ 12 \\ 8 \\ 4 \\ 0 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 8/3 \\ -8/3 \\ 4/3 \\ 0 \\ -4/3 \\ 8/3 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$





REAZIONI

$$H_A = 0 \quad V_A = -8/3F \quad V_D = 8/3F$$

$$N_{AB} = -8/3F \quad N_{BC} = 0 \quad N_{CD} = 8/3F \quad N_{EF} = 4/3F \quad N_{FG} = -4/3F \quad N_{AE} = 8\sqrt{2}/3F$$

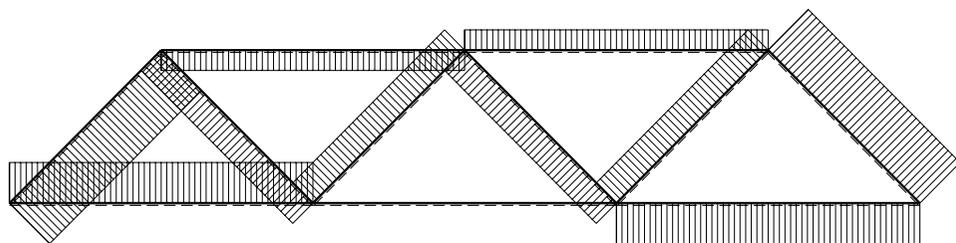
$$N_{EB} = 4\sqrt{2}/3F \quad N_{BF} = -4\sqrt{2}/3F \quad N_{FC} = 4\sqrt{2}/3F \quad N_{CG} = -4\sqrt{2}/3F \quad N_{GD} = -8\sqrt{2}/3F$$

SPOSTAMENTI ASSOLUTI

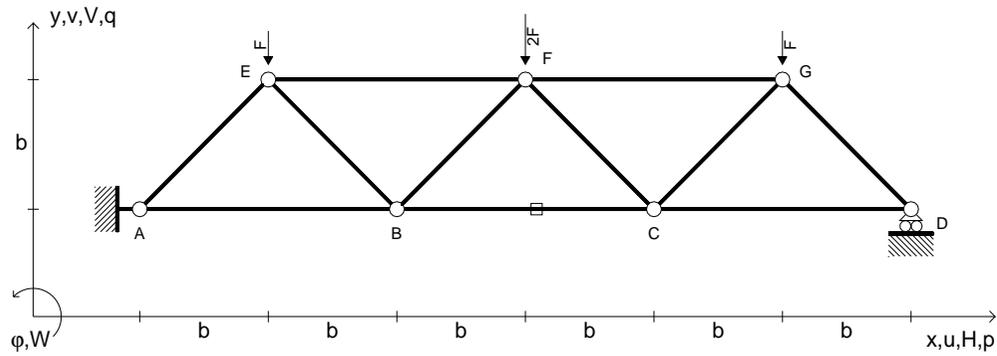
$$u_F = 2/9(Fb/EA)$$

$$v_F = -6(Fb/EA)$$

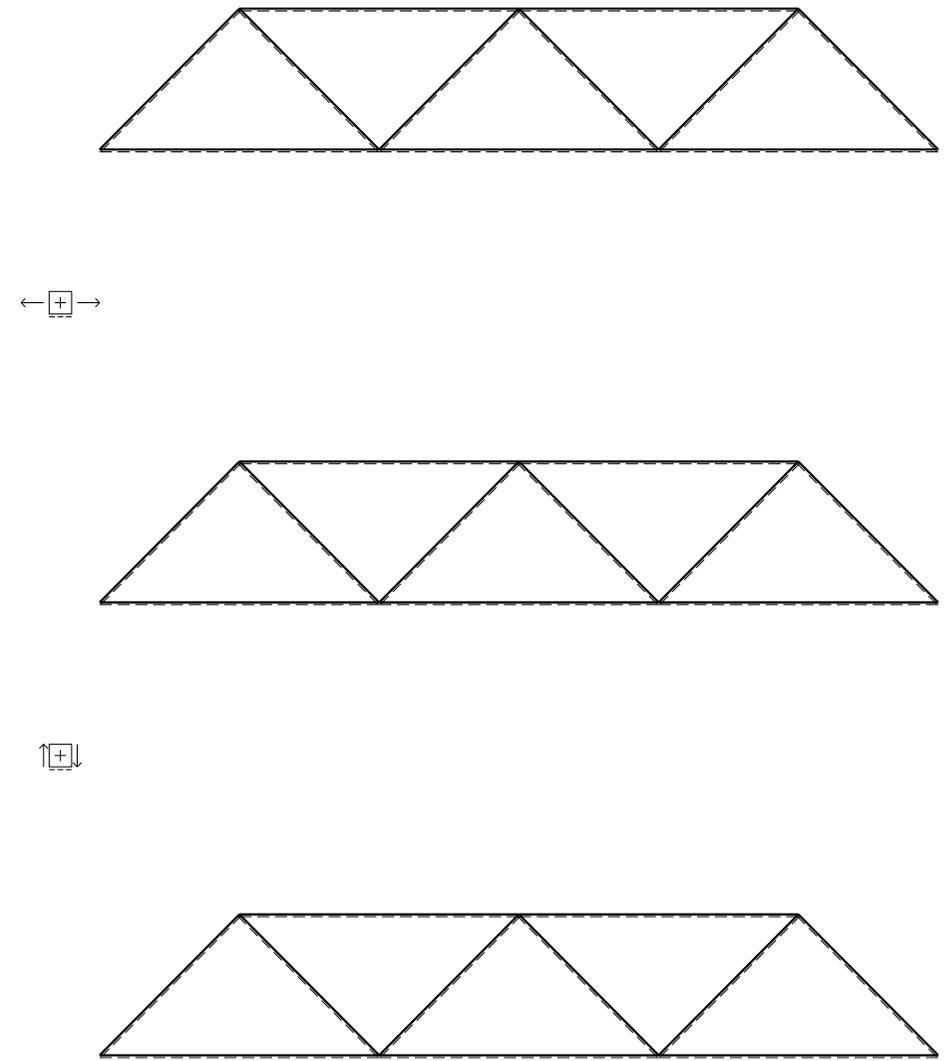
1 30 Fb/EA



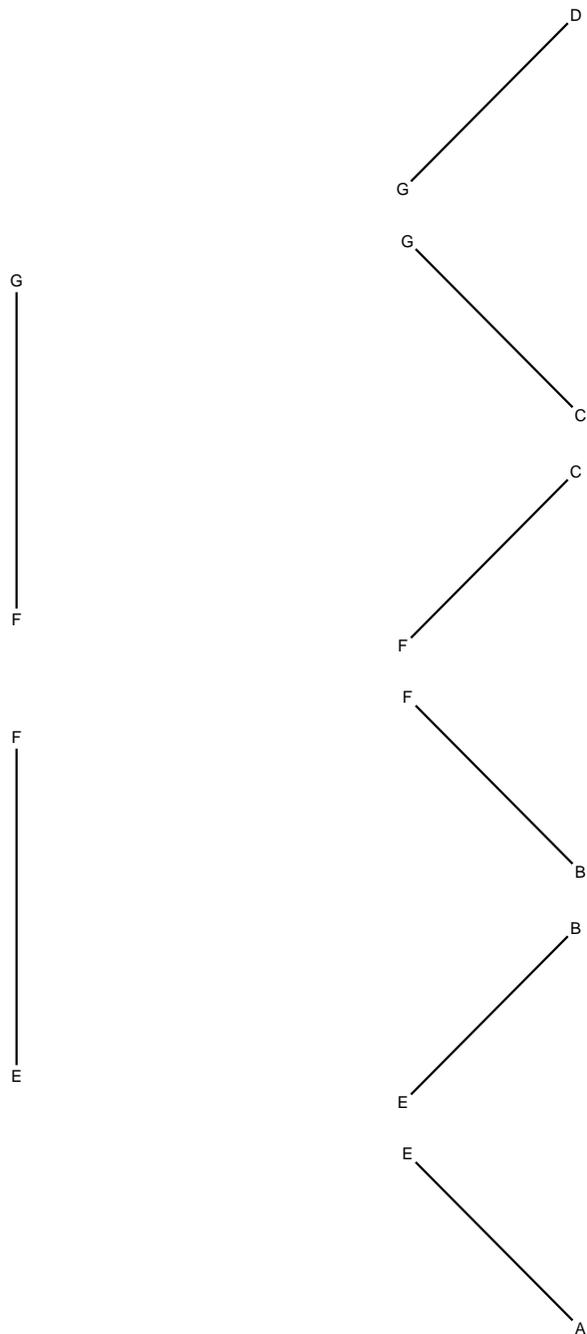
← ⊕ → 1 5 F



$V_E = -F$	$V_F = ?$	$EA_{FG} = EA$	$EA_{CG} = EA$
$V_F = -2F$	$EA_{AB} = EA$	$EA_{AE} = EA$	$EA_{GD} = EA$
$V_G = -F$	$EA_{BC} = 3/4EA$	$EA_{EB} = EA$	
$\varepsilon_{BC} = -3\alpha T = -3F/EA$	$EA_{CD} = EA$	$EA_{BF} = EA$	
$u_F = ?$	$EA_{EF} = EA$	$EA_{FC} = EA$	



Svolgere l'analisi cinematica.
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 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $V_D =$

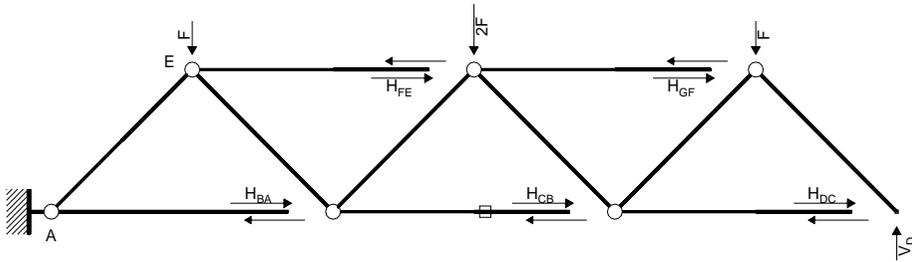
$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_{D,b} = 12Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_{D,b} - H_{BA,b} = 8Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_{D,b} + H_{FE,b} = 5Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_{D,b} - H_{CB,b} = 2Fb$$

Rotazione intorno a C: aste CG GD

$$2V_{D,b} + H_{GF,b} = Fb$$

Rotazione intorno a G: aste GD

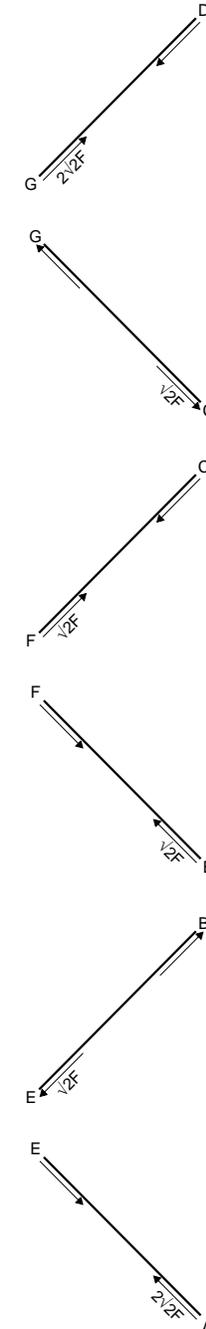
$$V_{D,b} - H_{DC,b} = 0$$

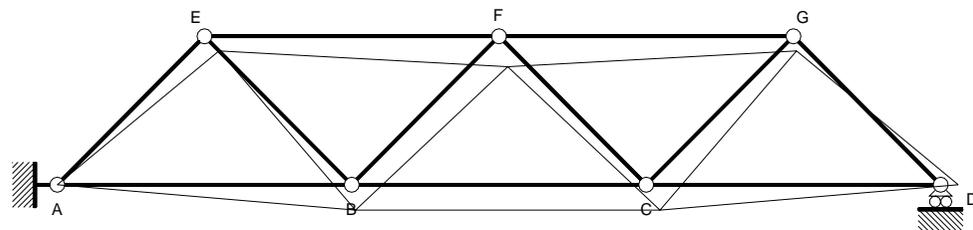
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} & \phi_{EB} & \phi_{BF} & \phi_{FC} & \phi_{CG} & \phi_{GD} \end{bmatrix} \begin{bmatrix} V_{D,b} & H_{BA,b} & H_{CB,b} & H_{DC,b} & H_{FE,b} & H_{GF,b} \end{bmatrix} = \begin{bmatrix} 12 \\ 8 \\ 5 \\ 2 \\ 1 \\ 0 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$

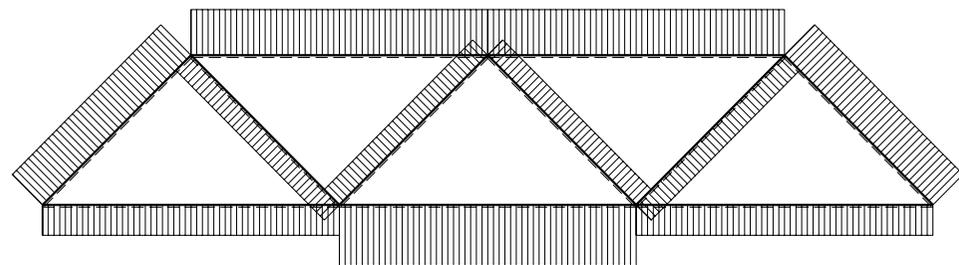
Soluzione del sistema

$$\begin{bmatrix} V_{D,b} \\ H_{BA,b} \\ H_{FE,b} \\ H_{CB,b} \\ H_{GF,b} \\ H_{DC,b} \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \\ -3 \\ 4 \\ -3 \\ 2 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$





← 80 Fb/EA



← ⊕ → | 5 F

REAZIONI

$$H_A = 0 \quad V_A = 2F \quad V_D = 2F$$

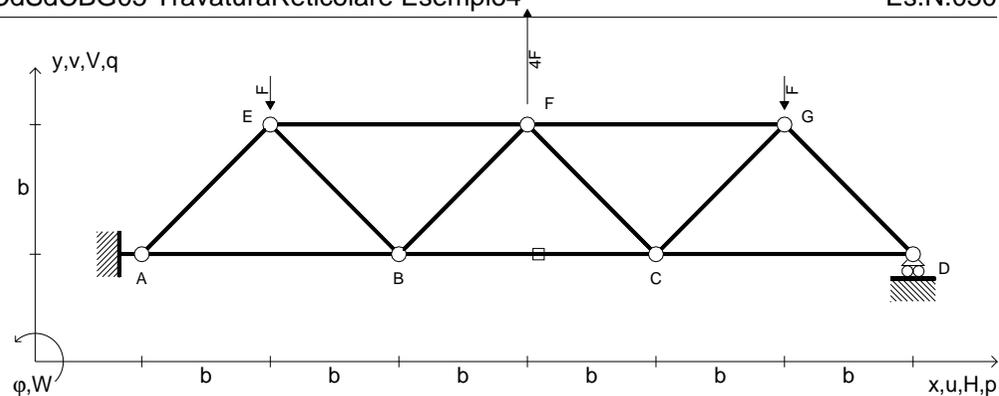
$$N_{AB} = 2F \quad N_{BC} = 4F \quad N_{CD} = 2F \quad N_{EF} = -3F \quad N_{FG} = -3F \quad N_{AE} = -2\sqrt{2}F$$

$$N_{EB} = \sqrt{2}F \quad N_{BF} = -\sqrt{2}F \quad N_{FC} = -\sqrt{2}F \quad N_{CG} = \sqrt{2}F \quad N_{GD} = -2\sqrt{2}F$$

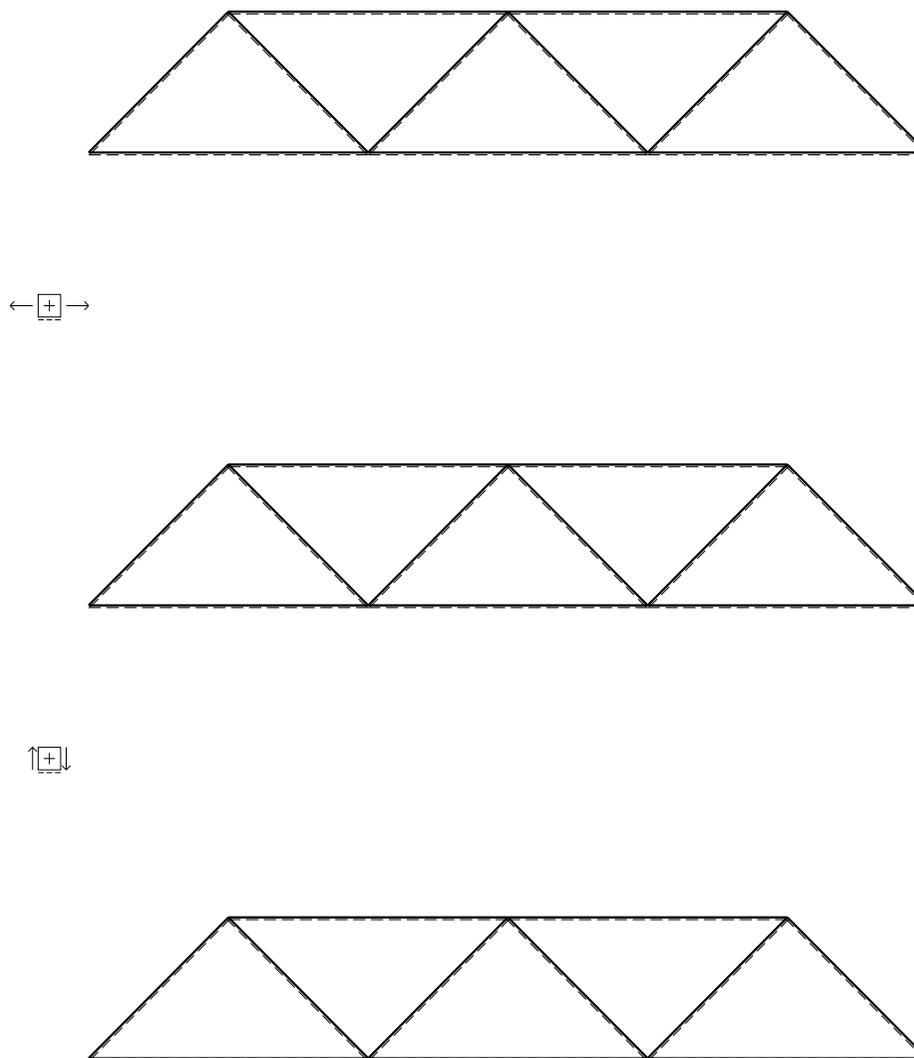
SPOSTAMENTI ASSOLUTI

$$u_F = 19/3(Fb/EA)$$

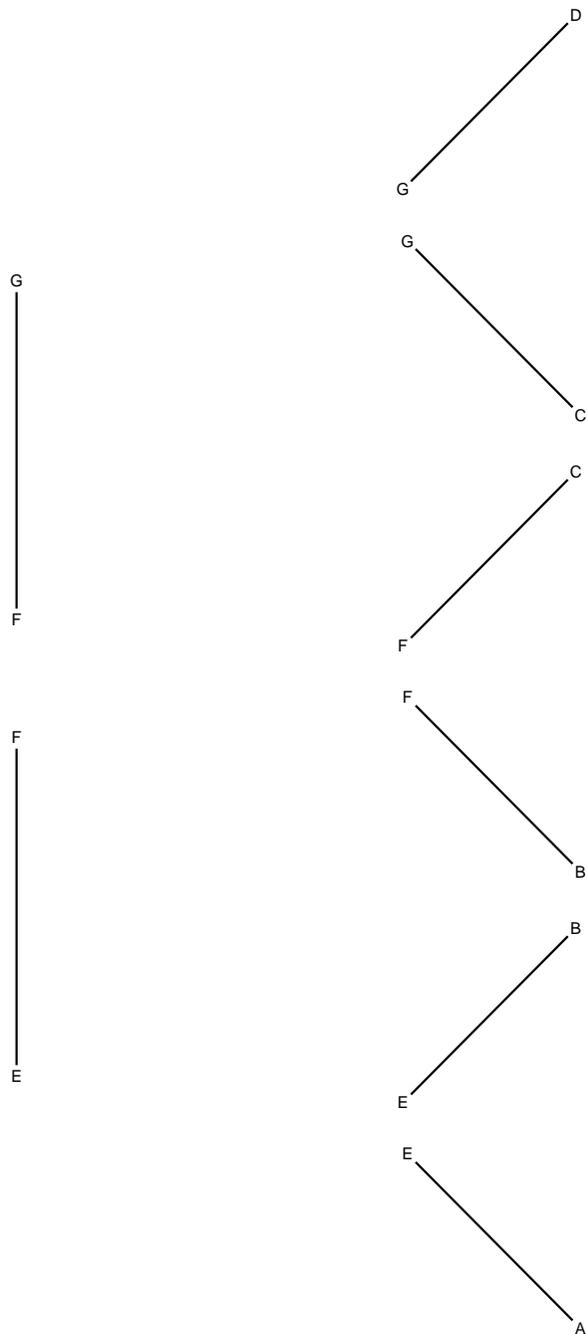
$$v_F = -(23+8\sqrt{2})(Fb/EA)$$



$V_E = -F$	$V_F = ?$	$EA_{FG} = EA$	$EA_{CG} = EA$
$V_F = 4F$	$EA_{AB} = EA$	$EA_{AE} = EA$	$EA_{GD} = EA$
$V_G = -F$	$EA_{BC} = EA$	$EA_{EB} = EA$	
$\varepsilon_{BC} = -3\alpha T = -3F/EA$	$EA_{CD} = EA$	$EA_{BF} = EA$	
$u_F = ?$	$EA_{EF} = EA$	$EA_{FC} = EA$	



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 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $V_D =$

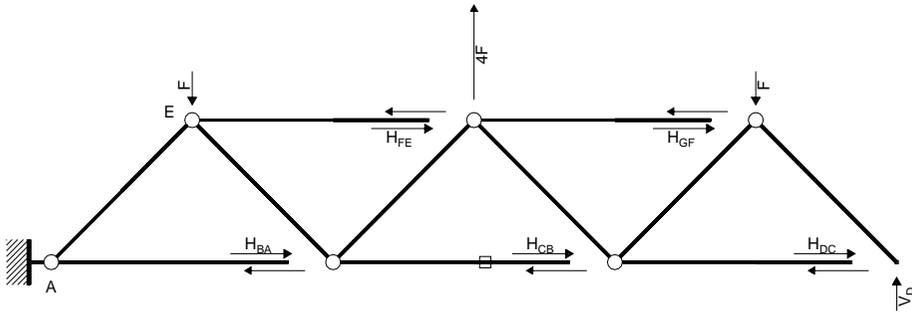
$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -6Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -4Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 2Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = Fb$$

Rotazione intorno a G: aste GD

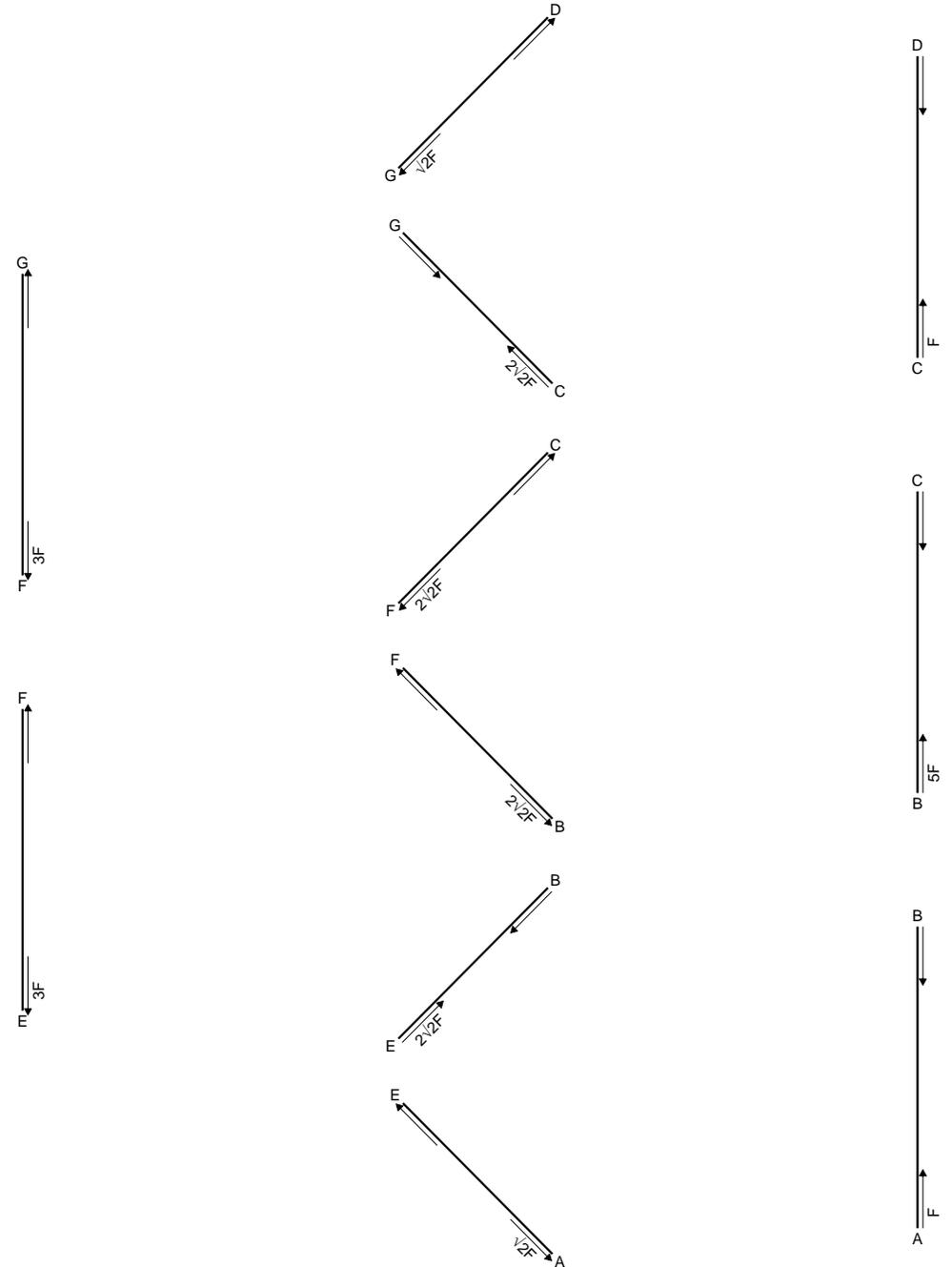
$$V_D b - H_{DC} b = 0$$

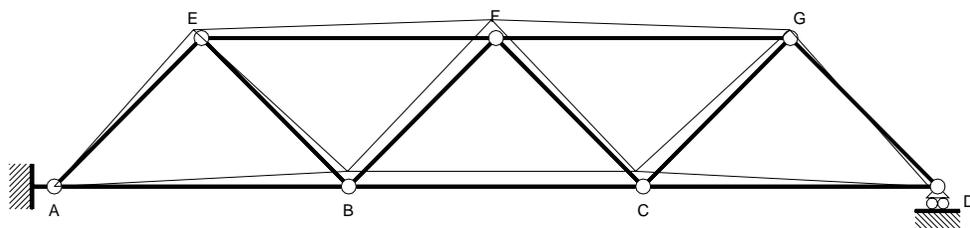
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} -6 \\ -4 \\ -1 \\ 2 \\ 1 \\ 0 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -1 \\ -1 \\ 3 \\ -5 \\ 3 \\ -1 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$





REAZIONI

$$H_A = 0 \quad V_A = -F \quad V_D = -F$$

$$N_{AB} = -F \quad N_{BC} = -5F \quad N_{CD} = -F \quad N_{EF} = 3F \quad N_{FG} = 3F \quad N_{AE} = \sqrt{2}F$$

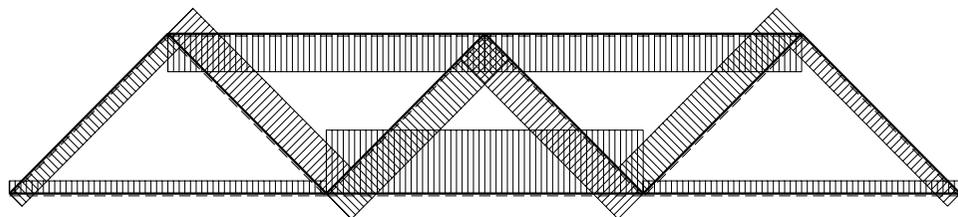
$$N_{EB} = -2\sqrt{2}F \quad N_{BF} = 2\sqrt{2}F \quad N_{FC} = 2\sqrt{2}F \quad N_{CG} = -2\sqrt{2}F \quad N_{GD} = \sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

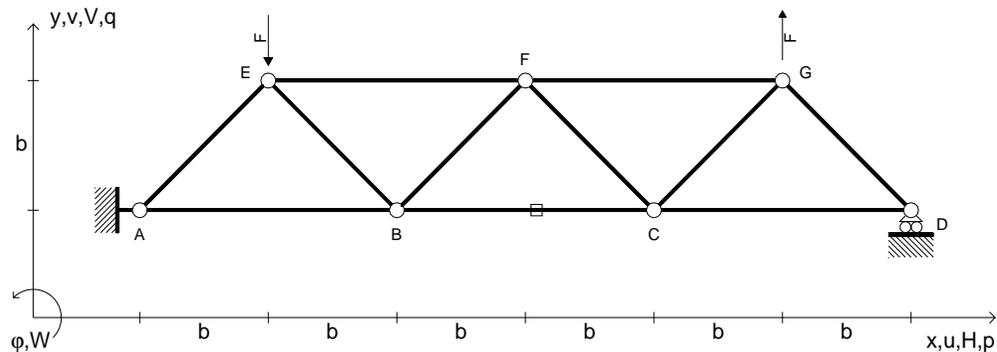
$$u_F = -10(Fb/EA)$$

$$v_F = (38+10\sqrt{2})(Fb/EA)$$

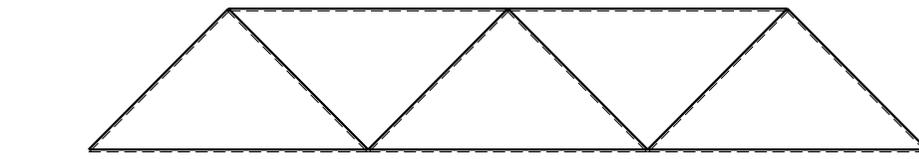
120 Fb/EA



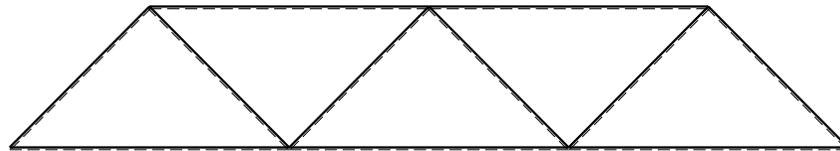
6 F



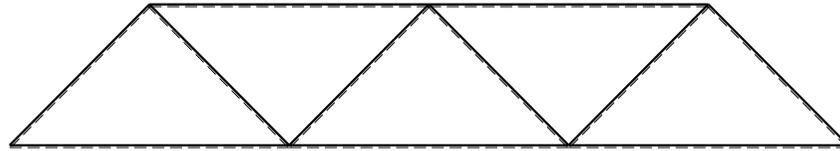
$V_E = -F$	$V_F = ?$	$EA_{EF} = EA$	$EA_{BF} = EA$
$V_G = F$	$EA_{AB} = EA$	$EA_{FG} = EA$	$EA_{FC} = EA$
$\varepsilon_{BC} = -3\alpha T = -3F/EA$	$EA_{BC} = 3/2EA$	$EA_{AE} = EA$	$EA_{CG} = EA$
$u_F = ?$	$EA_{CD} = EA$	$EA_{EB} = EA$	$EA_{GD} = EA$



← ⊕ →

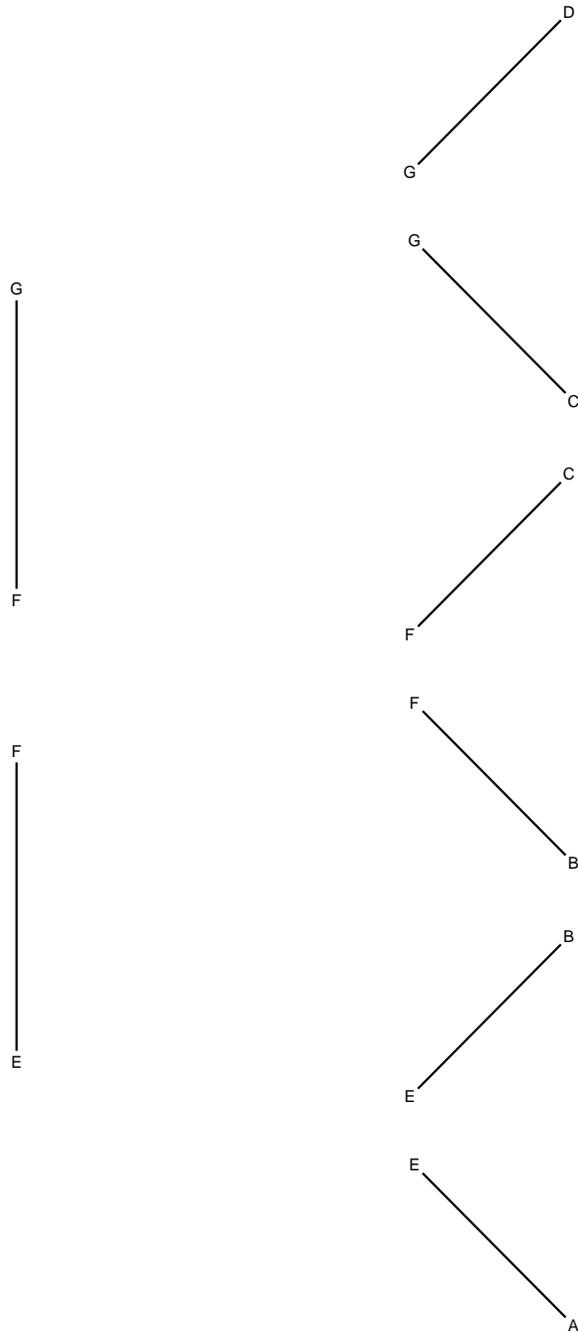


↑ ⊕ ↓



⊕ ↻

Svolgere l'analisi cinematica.
 Riportare la soluzione su questo foglio.
 Carichi e deformazioni date hanno verso efficace in disegno.
 Calcolare reazioni vincolari della struttura e delle aste.
 Tracciare i diagrammi delle azioni interne nelle aste.
 $A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.
 Allungamento termico assegnato ε su asta BC.
 Calcolare lo spostamento orizzont. del nodo F
 Calcolare lo spostamento verticale del nodo F
 @ Adolfo Zavelani Rossi, Politecnico di Milano

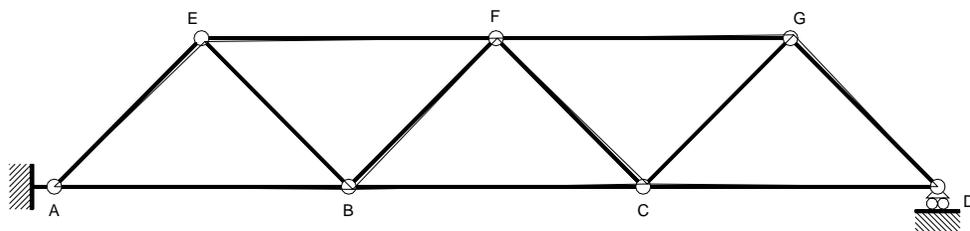


REAZIONI

$$\begin{array}{l}
 H_A = \quad V_A = \quad V_D = \\
 N_{AB} = \quad N_{BC} = \quad N_{CD} = \quad N_{EF} = \quad N_{FG} = \quad N_{AE} = \\
 N_{EB} = \quad N_{BF} = \quad N_{FC} = \quad N_{CG} = \quad N_{GD} =
 \end{array}$$

SPOSTAMENTI ASSOLUTI

$$\begin{array}{l}
 u_F = \\
 v_F =
 \end{array}$$



REAZIONI

$$H_A = 0 \quad V_A = 2/3F \quad V_D = -2/3F$$

$$N_{AB} = 2/3F \quad N_{BC} = 0 \quad N_{CD} = -2/3F \quad N_{EF} = -1/3F \quad N_{FG} = 1/3F \quad N_{AE} = -2\sqrt{2}/3F$$

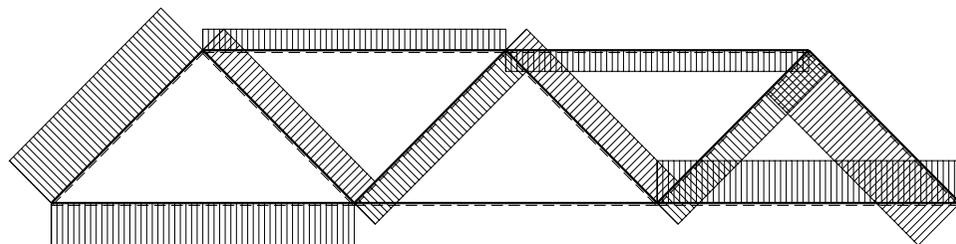
$$N_{EB} = -\sqrt{2}/3F \quad N_{BF} = \sqrt{2}/3F \quad N_{FC} = -\sqrt{2}/3F \quad N_{CG} = \sqrt{2}/3F \quad N_{GD} = 2\sqrt{2}/3F$$

SPOSTAMENTI ASSOLUTI

$$u_F = -23/9(Fb/EA)$$

$$v_F = 9(Fb/EA)$$

1 25 Fb/EA



← ⊕ → 1 1.2 F